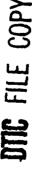
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Golden E. Lane, Jr.

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January 1982



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AIR FORCE WEAPONS LABORATORY
Air Force Systems Command
Kirtland Air Force Base, NM 87117



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#### 18. SUPPLEMENTARY NOTES

Appendixes B and C include work performed by the University of Colorado at Boulder and San Diego State University.

19. KEY WORDS (Continue on reverse side if necessary and identify by block number)

Reinforced Concrete

Displacement Control

Axial Load

Combined Loading

Shear Failure

Reinforced Concrete Beams

Flexural Load

D. ABSTRACT (Continue on reverse side if necessary and identify by block number)

Nine hinge-supported reinforced concrete beams were tested under displacement control with a proportional axial and symmetrical two-point lateral loading system. The nine beams were divided into three test series of three beams each. The beams in Series 1 contained shear reinforcement and were loaded monotonically to failure. Those in Series 2 contained no shear reinforcement and were loaded similarly to the first series. The Series 3 beams were shear reinforced and were loaded to failure under cyclic loading. Each beam had a

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# 20. ABSTRACT (Continued)

3.82-m span, a 229- by 381-mm cross section, and an effective depth of 317 mm. Reinforcement consisted of three No. 6 bars in tension and two No. 2 bars in compression. Shear reinforcement consisted of No. 2 stirrups at a spacing of 152 mm. Measurements consisted of steel and concrete strain, axial and lateral loads, pressure, displacement, and rotation. The Series 1 and 3 beams failed in flexural tension, and the Series 2 beams failed in shear compression. Also reported are the results of two companion plain concrete testing programs: (1) multiaxial testing of cubes, and (2) displacement-controlled cylinder tests.

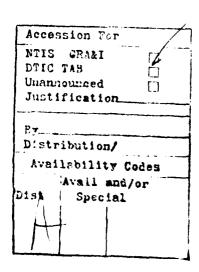
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#### I. INTRODUCTION

#### BACKGROUND

Although a significant amount of research has been directed toward the understanding of the behavior of reinforced concrete structures, there are some areas in which knowledge is incomplete. One such area is the mathematical modeling of the response of reinforced concrete structures under a wide variety of load conditions and ranges. Predicting the response of reinforced concrete structures loaded beyond the elastic range to collapse is an example of a case that cannot be adequately modeled. Specific areas that are not well understood include bond behavior between reinforcing steel and concrete, total multiaxial behavior of concrete, and strain rate effects on the behavior of concrete.

#### OBJECTIVE

This investigation was undertaken in an attempt to add to the basic understanding of the behavior of reinforced concrete members loaded to collapse. The specific objective of this research was to provide an elementary but well-defined data base of the material properties and the response of reinforced concrete beams subjected to combined flexural, axial, and shear forces. The resulting data are to be used in the development and verification of reinforced concrete behavioral models.

#### SCOPE

The experimental investigation consisted of three main areas of testing: static testing of reinforced concrete beams, multiaxial testing of plain concrete cubes, and displacement-controlled uniaxial tests on concrete cylinders.

The central area was the testing of nine reinforced concrete beams by the New Mexico Engineering Research Institute (NMERI). Nine hinge-supported reinforced concrete beams were tested under displacement control with a proportional axial and symmetrical two-point loading system. The nine beams were divided into three test series of three beams each. The beams in Series 1 contained shear reinforcement and were loaded monotonically to failure. Those in Series 2 contained no shear reinforcement and were loaded similarly to the first series. The Series 3 beams were shear reinforced and were loaded to

failure under cyclic loading. Data from these tests are presented in Appendix A.

Investigation of the other two areas was conducted by two universities under contract to NMERI. Multiaxial testing of 102-mm plain concrete cubes was performed at the University of Colorado. These cubes were cast from the concrete used for the beam fabrication. The results of this testing are reported in Appendix B. Displacement-controlled uniaxial compression tests were performed on 152-mm by 304-mm standard cylinders cast with the beams. This work was performed at San Diego State University. The results are reported in Appendix C.

## PREVIOUS COMBINED-LOAD BEAM TESTS

The beam testing program reported herein was an extension of a previous investigation conducted at the Eric H. Wang Civil Engineering Research Facility (CERF) in 1975 (Ref. 1). The geometry and material properties were the same in the two programs except for the absence of shear reinforcement in the present Series 2 beams.

In the previous investigation, 17 simply supported reinforced concrete beams were tested to collapse under combined flexural, axial, and shear forces. The beams were loaded laterally through a symmetrical two-point loading system and axially through the plastic centroid. Loads were applied by a single hydraulic system designed to provide a constant ratio between axial and lateral loads for the duration of the test. The two test parameters were axial-to-lateral-load ratio and shear-span-to-beam-depth ratio. Electrical measurements of beam behavior included steel strain on the longitudinal rebar, concrete strain, vertical deflections along the length of the beam, end rotations, and lateral and axial loads. In addition, a photoelastic coating sheet was bonded to one side of the beams and overlaid with a sheet of Polaroid film. The experimental results from the beam tests were compared with data calculated with an analytical behavioral model developed as part of this effort. The general beam behavior calculated from the analytical model agreed well with the measured results, especially in the region up to maximum load.

<sup>1.</sup> Lane, Golden E., Jr., Behavior of Reinforced Concrete Beams Under Combined Axial and Lateral Loading, AFWL-TR-76-130, Air Force Weapons Laboratory, Kirtland Air Force Base, New Mexico, May 1977.

#### II. BEAM TESTING PROGRAM

The beam testing program consisted of statically testing to collapse nine rectangular reinforced concrete beams. Four sets of three beams each were cast for the test program. One set, however, was used in shakedown tests of the loading apparatus. Table 1 presents the test matrix.

TABLE 1. TEST MATRIX

Concrete batch	Casting date	Beam test series no.	Load type	Remarks
1	6/20/80	1	Monotonic to failure	Contained shear reinforcement
2	6/26/80	Shakedown	Used for checking out testing apparatus	Two with and one without shear reinforcement
3	7/03/80	2	Monotonic to failure	Contained no shear reinforcement
4	7/09/80	3	Cyclic to failure	Contained shear reinforcement

The duration of the tests varied from 2 to 5 min. All beams had the same span length, cross section, hinged end supports, and point of load application. However, the Series 2 beams contained no shear reinforcement. The two test parameters considered were shear reinforcement and type of loading, i.e., monotonic or cyclic. Figure 1 shows the general loading scheme for the beams. The axial-to-lateral-load ratio, P/F, remained constant at approximately 3.2 for the duration of each test.

#### **GEOMETRY**

Figure 2 shows the beam specimen geometry. The beam span was 3.82 m from center to center of the pivoted shafts at the beam ends. Included in the length are the end reaction devices shown in Figures 2 and 3. Except for the lack of shear reinforcement in the Series 2 beams, the cross-sectional properties and geometry were the same for all specimens. The beams were 381 mm in

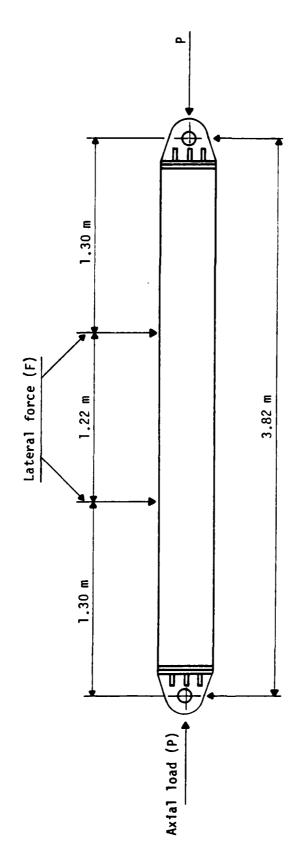
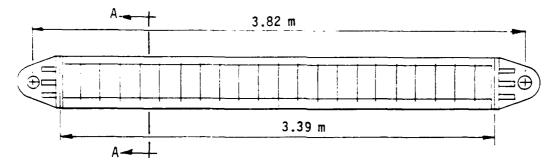
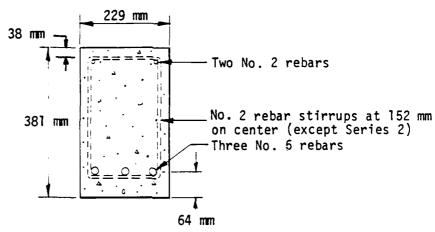


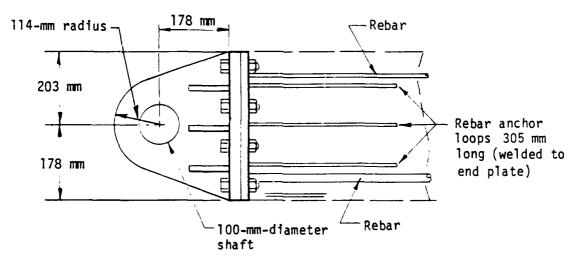
Figure 1. General loading configuration.



## a. Elevation.



## b. Section A-A.



c. End detail.

Figure 2. Beam geometry.

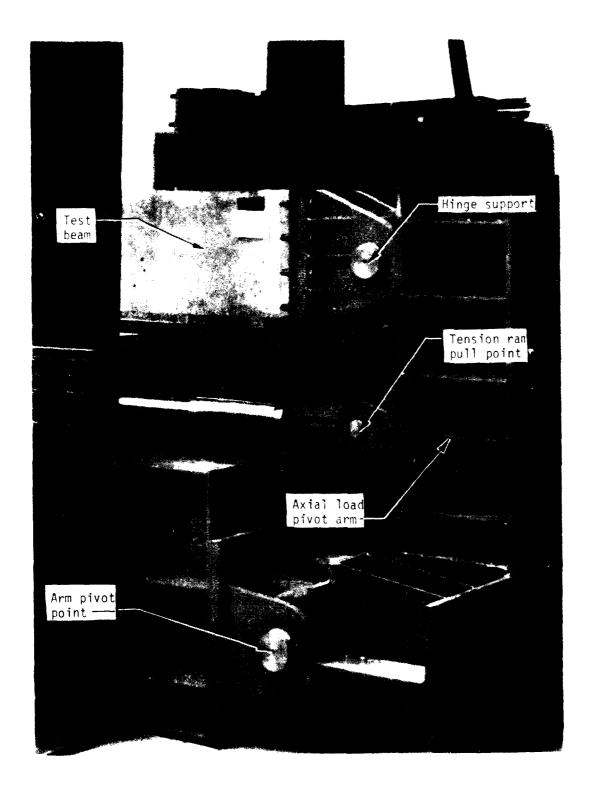


Figure 3. Axial load system.

overall depth and 229 mm wide, with a depth from the compressive face of the concrete to the centroid of the tensile steel of 317 mm. Tensile reinforcement consisted of three No. 6 reinforcing bars (rebar). The beams were considered to be singly reinforced in spite of the two No. 2 bars at the top of the beams. These two bars were included to assist in beam fabrication and to provide a means of making strain measurements in the compression zone.

To facilitate axial load application, the concrete portion of the beams was terminated at end bearing plates to which the end reaction devices were bolted. The longitudinal reinforcement was welded to the end bearing plates to assure adequate anchorage for the bars and to assure development of the full flexure and shear capacities of the beams. Additional reinforcement was also welded to the end plates to provide a mechanism for shear transfer between the concrete and the end supports. Figure 2 shows the detail of the end bearing plates.

#### REINFORCING STEEL

The principal longitudinal reinforcement, which consisted of three No. 6 bars, had a measured yield strength of 427 MPa and conformed to American Society for Testing and Materials (ASTM) specification A15-60. All of the steel was produced from the same heat to insure consistency among the beam specimens. A typical stress-strain curve is shown in Figure 4.

The stirrups and compression reinforcement were intermediate-grade steel conforming to ASTM specification A15 with a measured yield strength of 359 MPa. Although not covered by ASTM specification A305, the No. 2 bars had deformations similar to those of the No. 6 bars. Figure 5 shows a typical stress-strain curve for the No. 2 bars.

#### CONCRETE

The concrete used in the beams and in the other test specimens had a nominal compressive strength of 35 MPa and was produced with Type I/II portland cement and a maximum-size aggregate of 10 mm. The coarse aggregate was a crushed material of uniform gradation. The fine aggregate was a washed sand conforming to ASTM specification C-33 and had less than 2 percent by weight

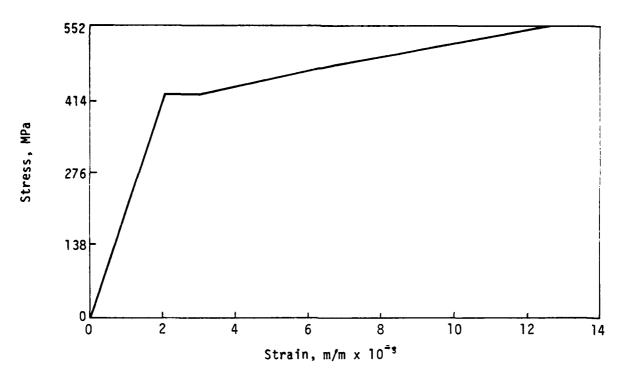


Figure 4. Stress-strain curve, No. 6 bars.

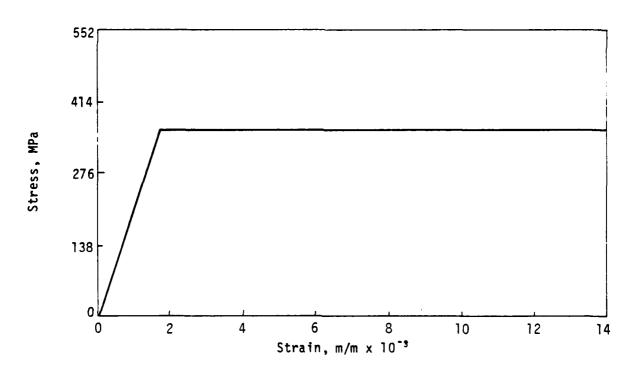


Figure 5. Stress-strain curve, No. 2 bars.

passing the No. 200 sieve. The fineness modulus of the sand varied from 2.6 to 3.1. The concrete mix is shown below.

Cement	289 kg
Fine aggregate	739 kg
Coarse aggregate (10 mm crushed)	576 kg
Water	175 kg
Admixture	
Master Builders Pozzolith 300 N	59 m1

The concrete was mixed in a Daffin mobile concrete mixer which produces the concrete by a continuous mixing process. The beams and auxillary specimens were cast in four batches. Each batch consisted of three beams, twenty 152-mm by 305-mm cylinders, twenty-four 102-mm cubes, and nine pullout specimens. The beam concrete was compacted with an electric vibrator probe. The other specimens were compacted by rodding. All specimens were cured under polyethylene plastic sheets. Results of tests on the concrete control cylinders are presented in Table 2.

#### INSTRUMENTATION

Instrumentation for all of the beams was generally similar. The main exception was the absence of stirrup strains for the Series 2 beams. Measurements made included vertical deflection along the beam, vertical and horizontal deflections at the support shafts, steel and concrete strain at various locations, rotation at the beam ends, and lateral and horizontal loads.

<u>Displacement</u>—Figure 6 shows the layout of the measurement stations and the location of displacement measurements. Vertical deflection measurements were made at seven locations along the beam (stations 0, 2, 3, 4, 5, 6, and 8). The measurements were made with Celsco linear potentiometers connected to the back of the beams at middepth. The same type of potentiometers were used to measure the horizontal movement of the end supports. Figure 7 shows the potentiometer attached to a beam.

Strain--Strain measurement locations are shown in Figure 8. Steel strain in the longitudinal tensile reinforcement was measured at stations 2 through 6. The measurements were made on the middle reinforcing bar. Strain measurements on the two compression steel bars were also taken at stations 2 through

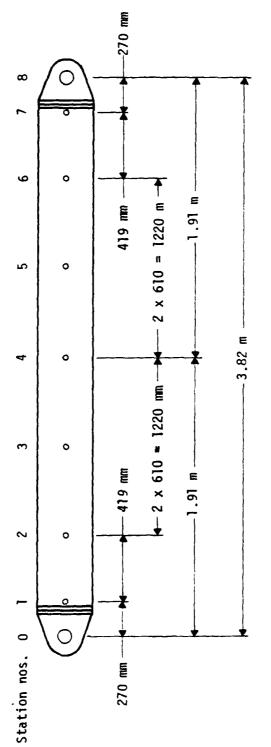
TABLE 2. BEAM TEST CONCRETE STRENGTH DATA

Batch	Test no.	Test date	Age at testing, days	Cylinder <sup>a</sup> test, MPa	Beam <sup>b</sup> test, MPa	Split cylinder test, MPa
1 Series 1 Cast 6/20/80 7 day - 26.3 MPa 14 day - 32.0 MPa 28 day - 34.6 MPa SDSU <sup>C</sup> - 34.0 MPa	1-1 1-2 1-3	10/16/80 10/17/80 10/21/80	118 119 123	37.4 38.2 38.9	3.59 3.50 3.76	
2 Shakedown Cast 6/26/80 7 day - 27.6 MPa 14 day - 29.0 MPa 28 day - 34.7 MPa SDSU - 36.1 MPa	1 2 3	9/23/80 10/07/80 11/06/80	89 103 138	36.3 37.9 31.9	3.21 5.32	5.62 3.93
3 Series 2 Cast 7/03/80 7 day - 24.1 MPa 14 day - 29.9 MPa 28 day - 33.5 MPa SDSU - 36.9 MPa	2-1 2-2 2-3	10/24/80 10/28/80 10/31/80	113 117 120	33.0 40.3 31.0	4.59 4.60 5.31	4.38 3.66
4 Series 3 Cast 7/09/80 7 day - 27.3 MPa 14 day 28 day - 34.1 MPa SDSU - 34.7 MPa	3-1 3-2 3-3	11/10/80 11/18/80 11/20/80	124 132 134	29.9 40.6 41.2	4.70 5.04 4.79	3.96 4.65 3.75

 $<sup>^{\</sup>rm a}$ 152- by 305-mm cylinder; average of three cylinders.

b<sub>152-</sub> by 152- by 533-mm beam; modulus of rupture.

 $<sup>^{\</sup>mathtt{C}}\mathsf{Tests}$  at San Diego State University; average of six cylinders.

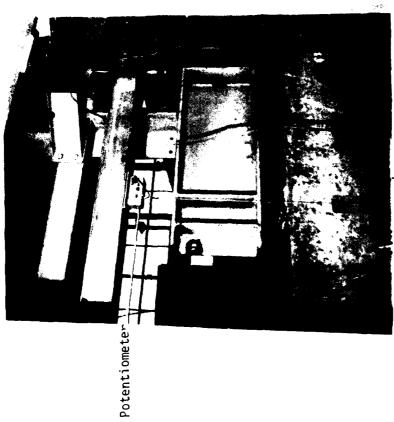


Measurements: Stations 0 and 8, horizontal and vertical displacement. Stations 1 and 7, rotation only. Stations 2 through 6, vertical deflection. Stations 2 through 6, strain (See Fig. 8).

Figure 6. Measurement station layout.

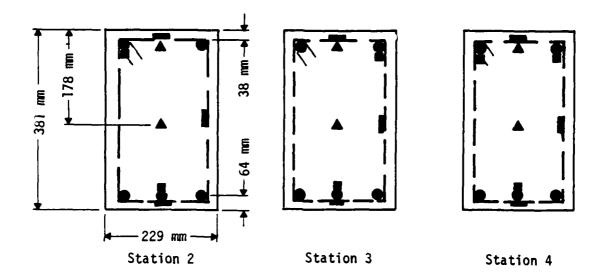
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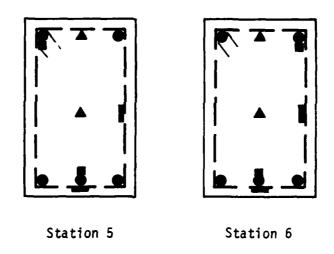




Connection to back of beam

Figure 7. Potentiometer attachment,





# Legend

- Longitudinal steel strain
- Vertical or transverse steel strain
- ▲ Embedded concrete strain

Figure 8. Strain measurement locations.

6. At station 4, the beam centerline, a strain gage was mounted on each bar. At the remaining stations, the measurements were taken on alternate sides of the beam. Vertical and transverse steel strains were taken on stirrups. For Series 1 and 3, vertical strains were measured on opposite sides of the beams at stations 2 through 6, and transverse strains were made alternately at the top and bottom of the beams at stations 2 through 6. For Series 2, which had no shear reinforcement in the shear span, vertical and transverse strains were made at stations 3, 4, and 5. Measurements were made with 350-\$\omega\$, epoxy-backed, foil strain gages which had a 13-mm gage length and a gage factor of 2.125.

Concrete strains were measured near the top and at the middle of the beams at stations 2 through 6. These strains were measured with epoxy-encapsulated,  $120-\Omega$ , embedded strain gages with a 30-mm gage length and a gage factor of 2.10.

Rotation—Rotation measurements were made at both ends of the beams with gages specially fabricated by NMERI. The rotation gages consisted of a pendulum suspended from the paddle portion of a DX-type velocity gage. The rotation of the pendulum relative to the gage body was measured by the variable inductance transducer of the velocity gage.

Load--Load measurements were made at the vertical ram providing the lateral load and at the two horizontal rams providing the axial load. These measurements were made with load cells fabricated and calibrated by NMERI. In-line hydraulic pressure was also monitored.

#### DATA ACQUISITION

The data were recorded, stored, and plotted on a Hewlett-Packard model 3052 data acquisition system. The voltage output from the system's digital multimeter was recorded on a floppy disk. The sampling rate was approximately two samples per second for every channel. The same system was used to reduce and plot the data.

#### TEST APPARATUS

Figure 9 shows a schematic drawing of the load application system. The loading device used in this investigation was the same test frame used in the

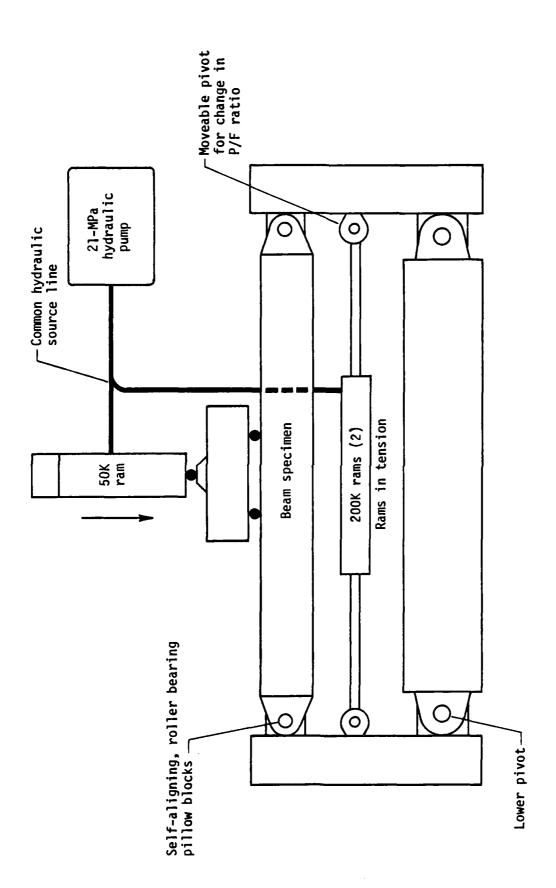


Figure 9. Schematic of beam loading system.

previous beam testing program reported in Reference 1. It was also the same frame used by Crist (Ref. 2) in a reinforced concrete deep beam study. The frame was modified to accommodate axial load application. Figure 10 shows the modified test frame which consisted of an upper portion that provided reaction for the lateral load and a lower portion that provided the axial load and support system. The two portions were tied together by five vertical structural T-sections.

Lateral load was applied by a 377-kN-capacity hydraulic ram with a 300-mm stroke. Axial load was applied by two 890-kN-capacity double-acting rams with 600-mm strokes, mounted in a horizontal position. A single hydraulic system was used to activate the rams to insure a constant P/F ratio throughout each test. The hydraulic system had a capacity of 21 MPa.

The total lateral load was divided into a two-point load by a steel distribution beam which imparted force to the beams through 64-mm-diameter rollers and 102- by 229- by 19-mm steel bearing plates. One end of the distribution beam was free to translate and rotate while the other end was only free to rotate. The bearing plates were seated to the beams with a thin layer of high-strength gypsum compound. The length of the shear span was established by the position of the lateral loads.

Axial load was applied to the beams with the two horizontal rams in tension; this resulted in compression on the beam because of the pivoting of the vertical reaction arms (Figs. 3 and 9). The P/F ratio was defined by the pull-point position of the rams on the reaction arms. To adjust the P/F ratio, the connection point of the tension rams to the pivot arm could be changed. The hinged condition at the ends of the beams was insured by transmitting the axial load through self-aligning, roller-bearing pillow blocks and 102-mm-diameter steel shafts. The axial force was applied through the plastic centroid of the beam cross section. The plastic centroid of a section, as defined by the 1977 ACI Building Code (Ref. 3), is the centroid of resistance to load

<sup>2.</sup> Crist, R. A., Shear Behavior of Deep Reinforced Concrete Beams, Vol. II: Static Tests, AFWL-TR-67-61, Air Force Weapons Laboratory, Kirtland Air Force Base, New Mexico, October 1967.

<sup>3.</sup> Building Code Requirements for Reinforced Concrete, ACI (318-77), American Concrete Institute, Detroit, Michigan, 1977.

Figure 10. Test frame.

computed under the assumption that the concrete is uniformly stressed to failure ( $f'_c$ ) and the reinforcing steel is uniformly stressed to yield strength ( $f'_v$ ).

To insure that the forces measured in the horizontal rams during the tests could be accurately converted to axial forces in the test beams, a series of calibration tests was conducted prior to actual beam testing. The calibration tests consisted of loading a dummy beam axially while measuring the forces in the hydraulic rams with force links and the axial load in the beam with a load cell. Under the assumption that all joints in the mechanical linkage between the horizontal rams and the dummy beam were frictionless, the calculated axial load in the beam was compared to the load indicated by the load cell. The agreement between calculated and measured forces in the dummy beam was within 10 percent; however, the corrections derived from the calibration tests were used to determine axial loads in the beams during the actual tests.

The displacement control feature of the tests was accomplished with a Datatrak programmer system. This entailed etching the desired deflection-time history onto a special metallic paper. The paper was then placed on a drum that rotated at a rate selected to produce the desired test duration. As the drum rotated, a servomotor moved a sensor on the paper, keeping it in contact with the upper surface of the etched program. The servomotor also positioned the wiper of a set of point potentiometers which provided an electrical analog signal proportional to desired beam displacement as a function of time. A linear potentiometer was used to monitor actual beam deflection. The difference between the actual and the desired potentiometer voltages formed an error signal. A current proportional to this error signal was supplied to a Moog servovalve which increased or decreased the pressure on the beam's hydraulic cylinders as needed to make the error signal zero. The control parameters for the monotonic tests, Series 1 and 2, were a 152-mm maximum centerline deflection at approximately 300 s. The displacement-time functions for all three series are shown in Figure 11. The five control points where the deflection was to drop off--13, 23, 32, 51, and 102 mm--were selected on the basis of the load-deflection behavior of the Series 1 beams. The points were selected to provide unload cycles midway in the linear region, near yield, in the flat portion of the curve, just into strain-softening, and late into strain-softening.

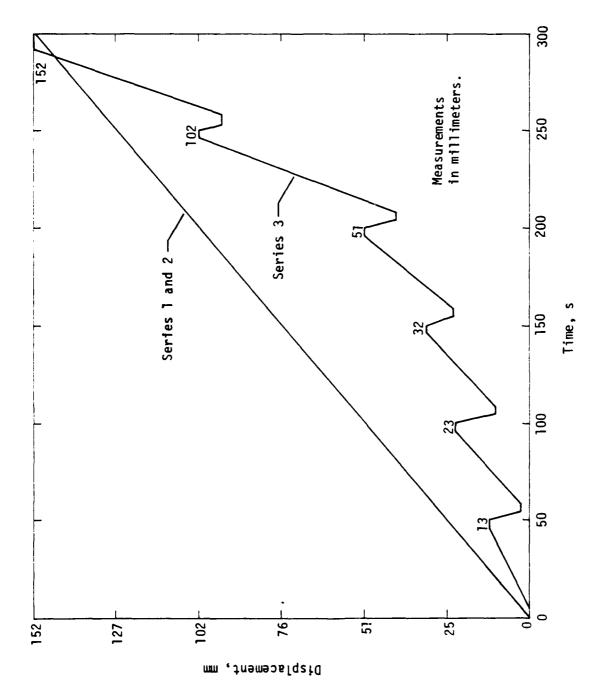


Figure 11. Displacement-time histories.

#### III. BEAM TESTING RESULTS

Table 3 presents a summary of the test results. The P/F ratios presented in Table 3 were calculated from measured loads, which is the reason for the variation in a parameter that should be constant.

Data from the beam tests are presented in Appendix A. For Series 1 and 2, where possible, data traces for symmetric locations were plotted on the same graph. Because of the cyclic loading in Series 3, representative plots of the symmetric measurement locations are presented.

Beam test designation	Test date	Concrete strength, MPa	Concrete age at testing, days	Maximum lateral load, kN	P/F ratio	Failure mode
1-1	10/16/80	37.4	118	235.7	3.24	Flexural tension
1-2	10/17/80	38.2	119	224.0	3.32	Flexural tension
1-3	10/21/80	38.9	123	222.5	3.40	Flexural tension
2-1	10/24/80	33.0	113	217.3	3.39	Shear compression
2-2	10/28/80	40.3	117	205.8	3.26	Shear compression
2-3	10/31/80	31.0	120	218.5	3.38	Shear compression
3-1	11/10/80	29.9	124	237.8	3.28	Flexural tension
3-2	11/18/80	40.6	132	231.0	3.04	Flexural tension
3-3	11/20/80	41.2	134	228.5	3.11	Flexural tension
	1	1	1	1	1	i

TABLE 3. SUMMARY OF TEST DATA

## GENERAL BEHAVIOR

The general response of the beams can be illustrated by their load-centerline deflection curves. Figure 12 shows the idealized load-deflection curve for the beams. The initial behavior is linear to about 10 percent of the maximum load. The concrete then cracks, and the curve is again fairly linear at a reduced stiffness. When the tension reinforcement begins to yield, the curve becomes very nonlinear and flattens out. When the concrete in the compression zone begins to crush and spall, the beam resistance decreases with increasing deflection. For beams failing in shear, the behavior is the same up to the maximum shear resistance of the beam. The shear failure then results in sudden collapse of the beam. The cyclically loaded beams have the same

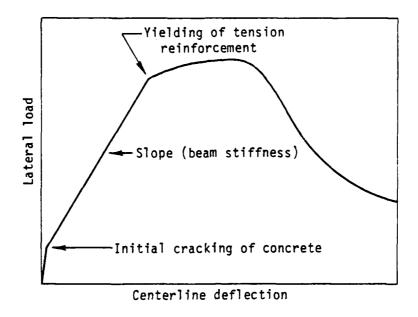


Figure 12. Idealized load-centerline deflection curve.

general behavior as the monotonically loaded beams except for the addition of the unloading and reloading hysteretic loops. The loops also progressively exhibit a stiffness reduction.

#### SERIES 1 BEAMS

The Series 1 beams were monotonically loaded to failure under a two-point lateral load and a proportional axial load. The Series 1 tests were conducted to determine the correlation between beams tested under load control and those tested under deflection control. Figure 13 presents the load-deflection curves for the three Series 1 beams along with the curve for beams 4-3-1 and 4-3-2 of the load control study (Ref. 1). The calculated curve is also included.

All of the beams exhibited the same behavior through the yielding of the tensile reinforcement and out to the maximum load capacity. The strain softening portions of the deflection control beams are similar, falling between the curves for the load control beams.

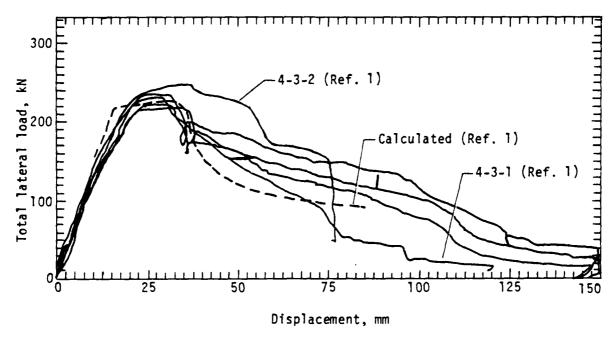


Figure 13. Load-centerline deflection, Series 1.

Also compared are the reinforcing steel strain data at the centerline of beam 4-3-1 (Ref. 1) and beam 1-1. Figures 14 and 15 present the tensile and compression strain plots, respectively. From the data presented, it appears there was little difference in the behaviors of the load controlled and the deflection controlled beams.

The mode of failure of the Series I beams was flexural tension; i.e., the tension reinforcement began yielding prior to crushing of the concrete. Because of the deflection control, the beams did not suddenly collapse, allowing measurement of the flexural resistance up to the maximum deflection of I50 mm. Because the load duration of the tests was relatively short, the concrete cracks were not marked at various load intervals, but were all marked and photographed at the conclusion of each test. Figure 16 shows the final crack patterns of all beams.

#### SERIES 2 BEAMS

These beams contained no web reinforcement in the shear span. The calculated maximum total lateral load for shear failure, based on the ACI code, was 180 kil. The calculated maximum lateral load for the flexural resistance was 225 kil. Figure 17 presents the load-deflection curves for the Series 2 beams.

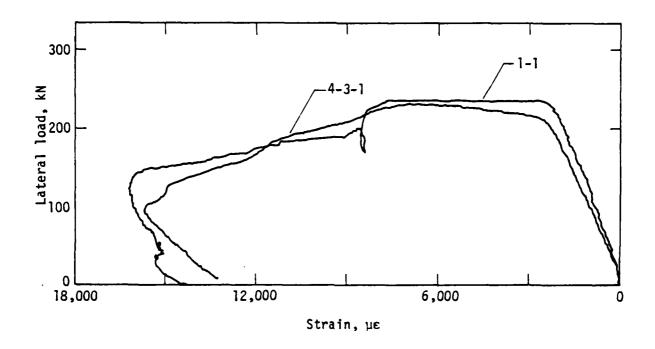


Figure 14. Centerline tensile steel strain.

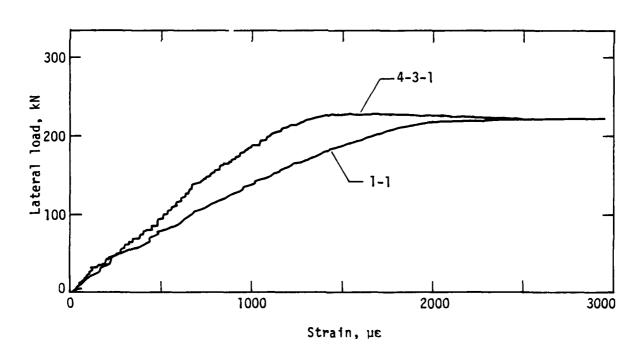


Figure 15. Centerline compression steel strain.



Figure 16. Final crack patterns for beams tested.

Series 3, Test 3

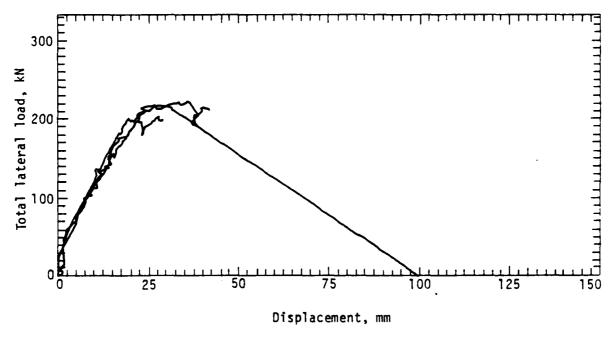
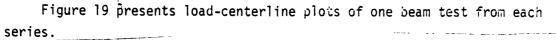


Figure 17. Load-centerline deflection, Series 2.

The general load-deflection behavior of the beams was the same as the Series 1 beams up to yield of the tensile reinforcement. After the tensile reinforcement began to yield, the shear crack became more apparent and widened. When the crack extended into the compression zone, the beams collapsed. The deflection control system was not sensitive enough to stop the beam from collapsing. The failure loads were only slightly less than the maximum beam resistance.

#### SERIES 3 BEAMS

The Series 3 beams were constructed in the same way as the Series 1 beams. However, they were loaded under five load-unload cycles. The programmed deflection-time history is shown in Figure 11. The history was intended to provide unload cycles at about midway in the linear range, near yield of the tensile reinforcement, in the flat portion of the curve, just into the strain-softening region, and late in the strain-softening region. The envelope of the load-deflection history generally coincides with the load-deflection curves for the Series 1 beams. The load-deflection curves for the beams are shown in Figure 18. Two significant aspects of the behavior are the hysteretic loops and the stiffness degradation at increasing deflection.



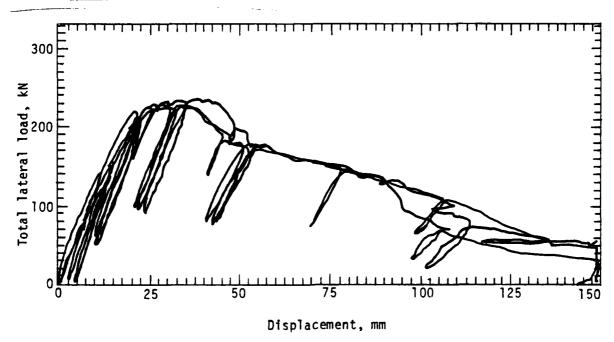


Figure 18. Load-centerline deflection, Series 3.

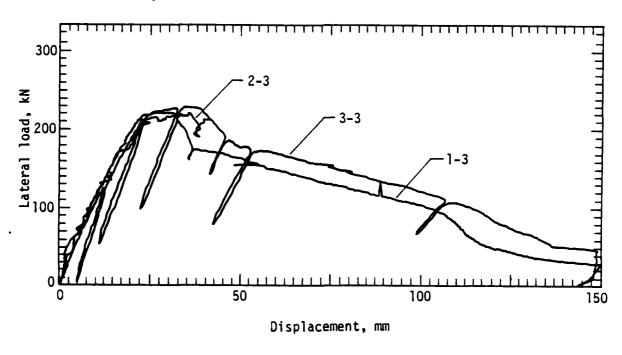


Figure 19. Load-displacement for three beams.

#### IV. BEAM TESTING CONCLUSIONS

Nine reinforced concrete beams were statically tested under combined axial and lateral load. The beams were laterally loaded by a symmetrical two-point load. The ratio of axial-to-lateral load was constant throughout the tests and had a value of approximately 3.2. Deflection control was used in the loading to failure of the beams. A closed loop system was used to provide the deflection control for the tests.

The beam tests consisted of three series of three beams each. The geometry and longitudinal reinforcement were the same for all beams. However, the Series 2 beams contained no web reinforcement in the shear span. The Series 1 beams were monotonically loaded to a maximum deflection of 150 mm with the failure being flexural tension. The Series 2 beams failed in shear-compression, at a load slightly less than the Series 1 beam. The Series 3 beams were tested under cycles of load-unload with the test being stopped at a maximum deflection of 150 mm. These beams also failed in flexural tension.

The behavior of the Series 1 beams was very similar to the 4-3-1 and 4-3-2 beams of the previous test program reported in Reference 1. The only difference in the two test series was the use of deflection control in this study versus the load control used in the previous study. The similarities in the behavior of the beams indicate that the loading apparatus was stiff enough in the previous test not to alter significantly the behavior at initial crushing of the concrete and into the strain-softening region.

The Series 2 beams, designed to fail in shear, exhibited essentially the same behavior as the Series 1 beams up to just beyond yielding of the tensile reinforcement. At that point, the beams suddenly collapsed as a result of shear-compression failure.

The Series 3 beams, which were loaded cyclically, produced the same envelope load-deflection behavior as the Series 1 beams. The load-unload cycles can be characterized by a slight amount of hysteretics and a degradation with increasing deflection.

# CONVERSION FACTORS FOR U.S. CUSTOMARY TO METRIC (SI) UNITS OF MEASUREMENTS

(Symbols of SI units given in parentheses)

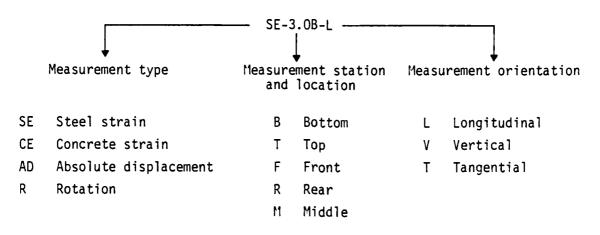
To convert from	to	Multiply by
angstrom	meters (a)	1.000 000 X E -10
atmosphere (normal)	kilo pescal (kPa)	1.013 25 X E +2
ber	kilo pescal (kPa)	1.000 000 X E +2
bern	mter <sup>2</sup> (a <sup>2</sup> )	1.000 000 X E -28
British thermal unit		1.000 000 2 2 -20
(thermochemical)	Joule (J)	1.054 350 X E +3
calorie (thermochemical)	Joule (J)	4.184 000
cal (thermochemical)/cm <sup>2</sup>	mega joule/m² (MJ/m²)	4.184 000 X E -2
curie	giga becquerel (68q)*	3.700 000 X E +1
degree (angle)	redien (red)	1.745 329 X E -2
degree Fahrenheit	degree kelvin (K)	t <sub>K</sub> = (t <sub>op</sub> + 459.67)/1.8
electron volt	joule (J)	1.602 19 X E -19
erg	Joule (J)	1.000 000 X E -7
erg/second	watt (H)	1.000 000 X E -7
foot	meter (m)	3.048 000 X E -1
foot-pound-force	Joule (J)	1.355 B18
gellon (U.S. liquid)	meter <sup>2</sup> (m <sup>2</sup> )	3.785 412 X E -3
inch	meter (m)	2.540 000 X E -2
jerk	joule (J)	1.000 000 X E +9
<pre>joule/kilogram (J/kg)(radiation dose absorbed)</pre>	Gray (Gy)**	1.000 000
kilotons	terajoules	4.183
kip (1000 lbf)	newton (N)	4.448 222 X E +3
kip/inch² (ksi)	kilo pascal (kPa)	6.894 757 X E +3
ktap	newton-second/m² (N-s/m²)	1.000 000 X E +2
micron	meter (#)	1.000 000 X E -6
mil	meter (s)	2.540 000 X E -5
mile (international)	meter (s)	1.609 344 X E +3
ounce	kilogras (kg)	2.834 952 X E -2
pound-force (1bf avoirdupois)	newton (N)	4.448 222
pound-force inch	newton-meter (N·m)	1.129 848 X E -1
pound-force/inch	newton/meter (M/m)	1.751 268 X E +2
pound-force/foot <sup>2</sup>	kilo pascal (kPa)	4.788 026 X E -2
pound-force/inch <sup>2</sup> (psi)	kilo pascal (kPa)	<b>6.894</b> 757
pound-mass (1bm avoirdupois)	kilogram (kg)	4.535 924 X E -1
pound-mess-foot <sup>2</sup> (moment of inertia)	kilogra <del>m-me</del> ter <sup>2</sup> (kg·m²)	4.214 011 X E -2
pound-mass/foot <sup>9</sup>	kilogram/meter <sup>2</sup> (kg/m <sup>2</sup> )	1.601 846 X E +1
rad (radiation dose absorbed)	Gray (Gy) ***	1.000 000 X E -2
roentgen	coulomb/kilogram (C/kg)	2.579 760 X E -4
Shake	second (s)	1.000 000 X E -8
slug	kilogram (kg)	1.459 390 X E +1
torr (mm Hg, 0° C)	kilo pascal (kPa)	1.333 22 X E -1

The becquerel (Bq) is the SI unit of radioactivity; 1 Bq = 1 event/s. The Gray (Gy) is the SI unit of absorbed radiation.

A more complete listing of conversions may be found in "Standard for Metric Practice," ASTM E-380-79, American Society for Testing and Materials.

## APPENDIX A. BEAM TEST DATA TRACES

Appendix A presents data from the nine beam tests. For Series 1 and 2, where possible, data traces for symmetric measurement stations are presented on the same graph. However, because of the cyclic nature of the Series 3 data, representative data plots are presented for the various stations. The measurement designation system is shown below.



## Sign convention:

Strain:

Compression = +

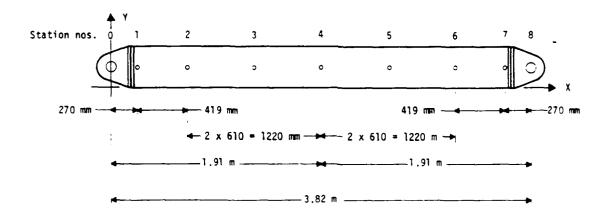
Tension = -

Displacement: Downward = +

## SUMMARY OF MEASUREMENTS

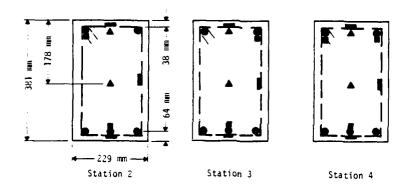
Measurement designation	Measurement type	Orientation	X-coordinate,	Y-coordinate,
AD-0.0-V	Displacement	Vertical	0	178
AD-2.0-V			689	203
AD-3.0-V			1299	203
AD-4.0-V			1910	203
AD-5.0-V			2520	203
AD-6.0-V			3130	203
AD-8.0-V		<b>↓</b>	3820	203
AD-0.0-H	₩	Horizontal	0	178

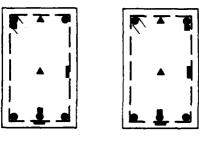
Measurement designation	Measurement type	Orientation	X-coordinate,	Y-coordinate, mm
AD-8.0-H	Displacement	Horizontal	3820	178
SE-2.0B-L	Steel strain	Longitudinal	689	64
SE-3.0B-L	1		1299	64
SE-4.0B-L			1910	64
SE-5.0B-L		Ì	2520	64
SE-6.0B-L	į į		3130	64
SE-2.OTF-L			689	343
SE-3.0TF-L			1299	343
SE-4.OTF-L			1910	343
SE-5.OTF-L		)	2520	343
SE-6.OTF-L	<b>↓</b>		3130	343
CE-2.OT-L	Concrete strain		689	343
CE-2.OM-L	(		689	203
CE-3.0T-L			1299	343
CE-3.011-L			1299	203
CE-4.OT-L			1910	343
CE-4.011-L			1910	203
CE-5.0T-L			2520	343
CE-5.011-L			2520	203
CE-6.OT-L			3130	343
CE-6.OM-L	↓	\	3130	203
SE-2.OF-V	Steel strain	Vertical	689	203
SE-3.0F-V			1299	203
SE-4.0F-V			1910	203
SE-5.OF-V		}	2520	203
SE-6.OF-V			3130	203
SE-2.0B-T		Transverse	689	64
SE-3.0B-T			1299	64
SE-4.OT-T	1		1910	343
SE-5.OT-T			2520	343
SE-6.OT-T	<b>↓</b>	] ↓	3130	343
R-0.0-A	Rotation	Angular	0	178
R-8.0-A	Rotation	Angular	3820	178



### Measurements:

Stations 0 and 8, horizontal and vertical displacement.
Stations 1 and 7, rotation only.
Stations 2 through 6, vertical deflection.
Stations 2 through 6, strain.



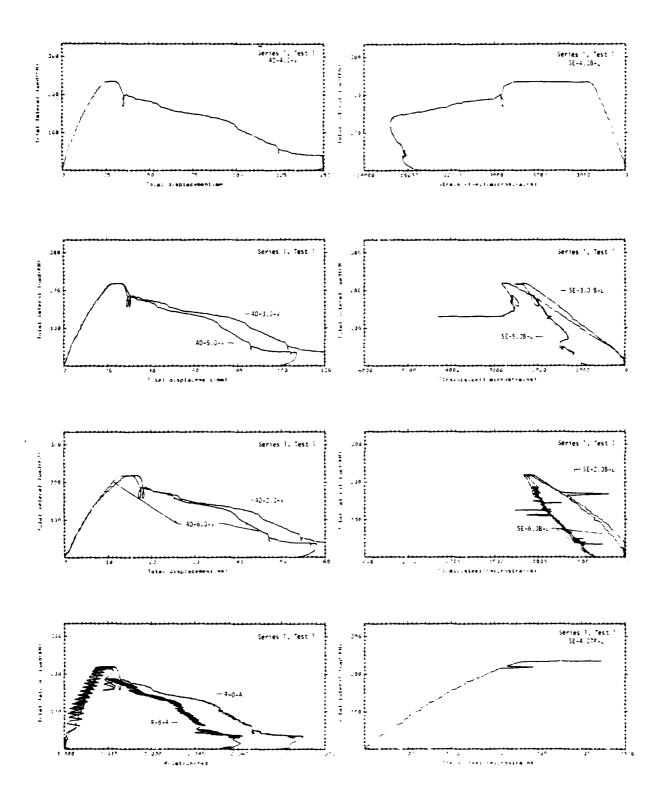


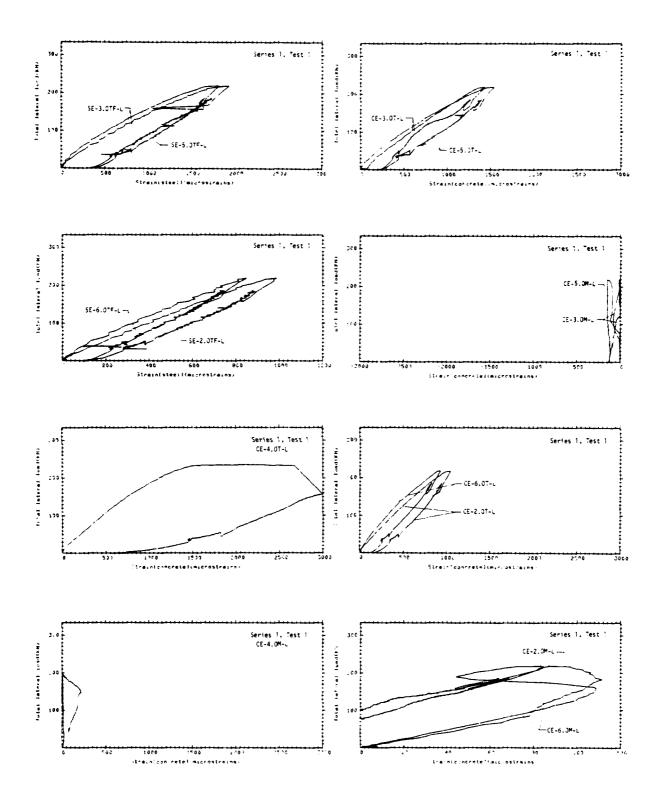
Station 5

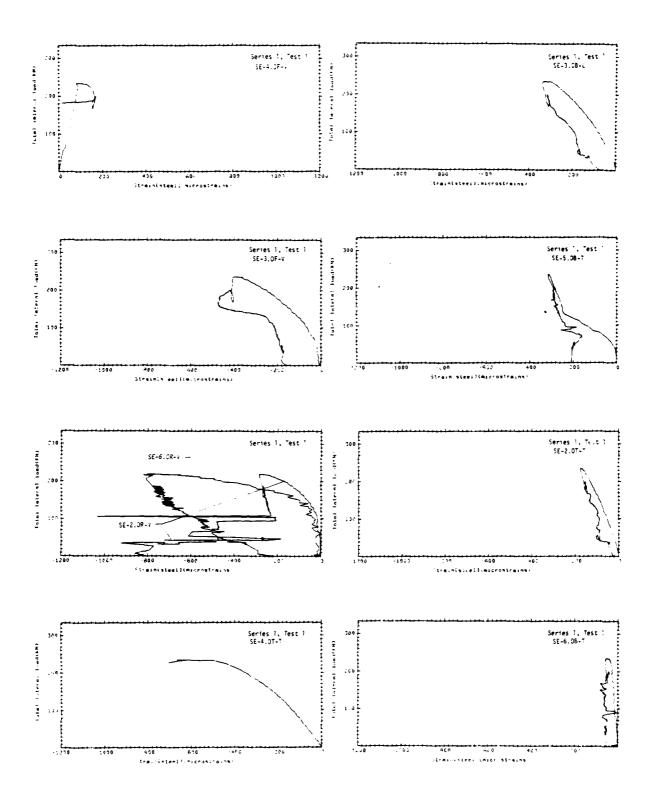
Station 6

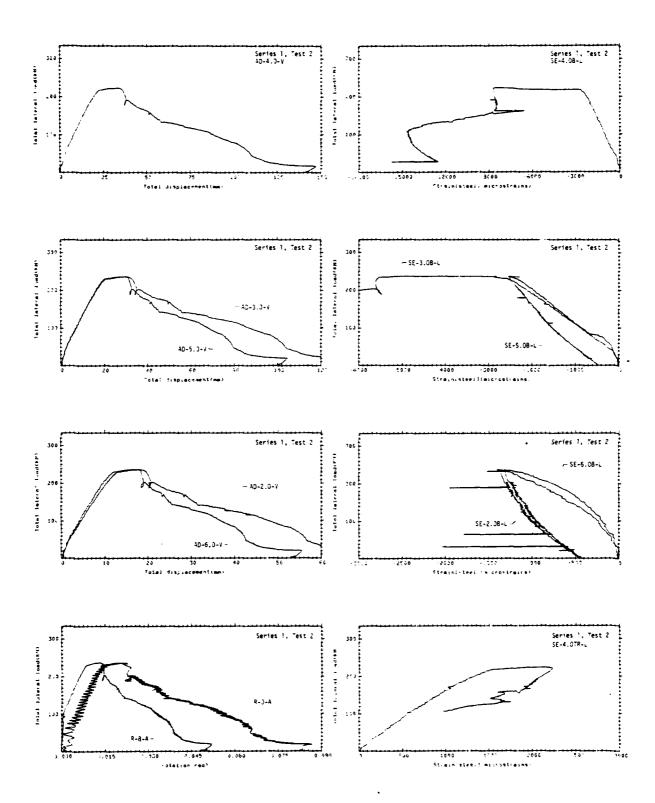
# Legend

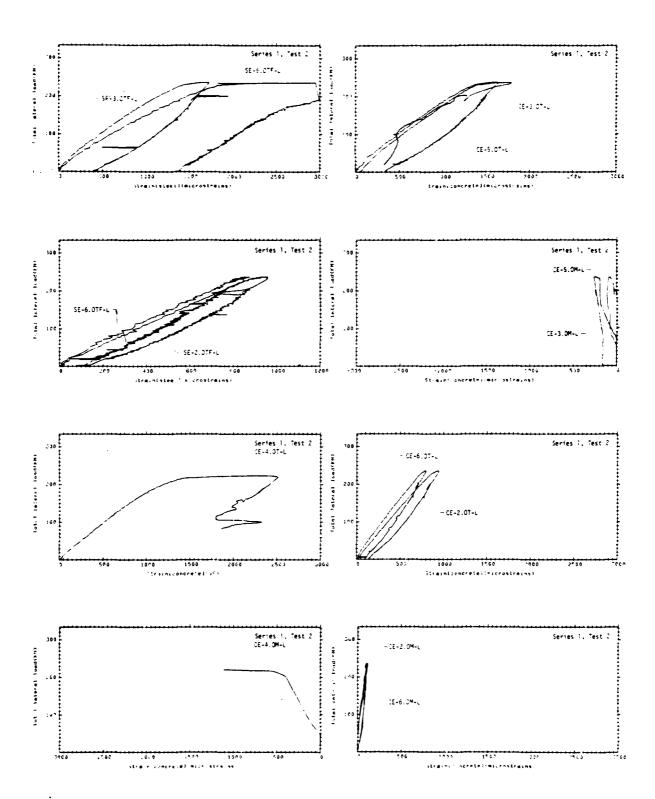
- Longitudinal steel strain
- Vertical or transverse steel strain
- ▲ Embedded concrete strain



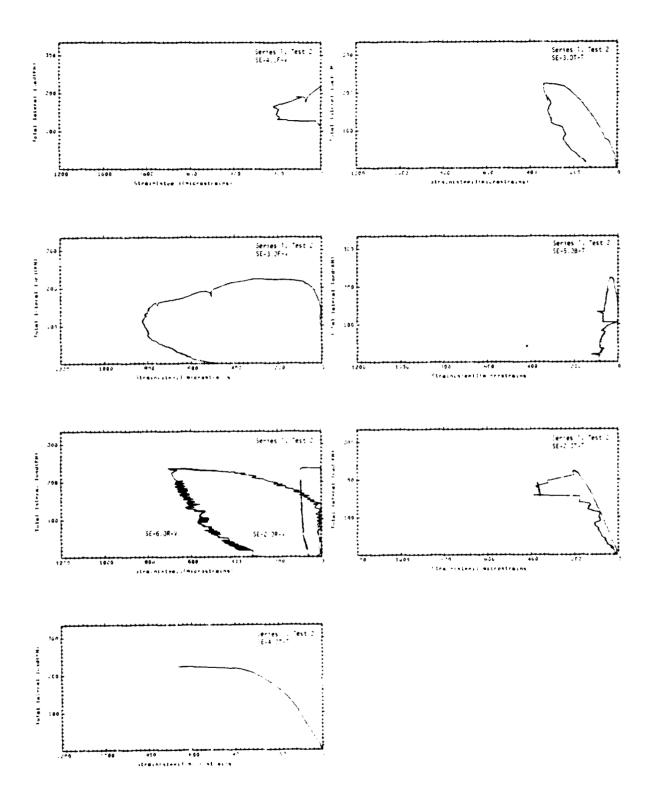




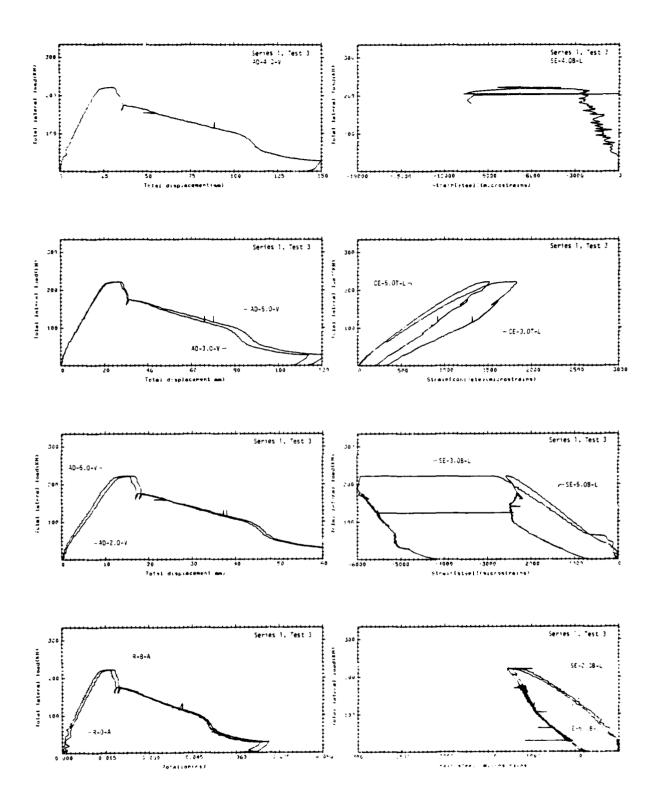




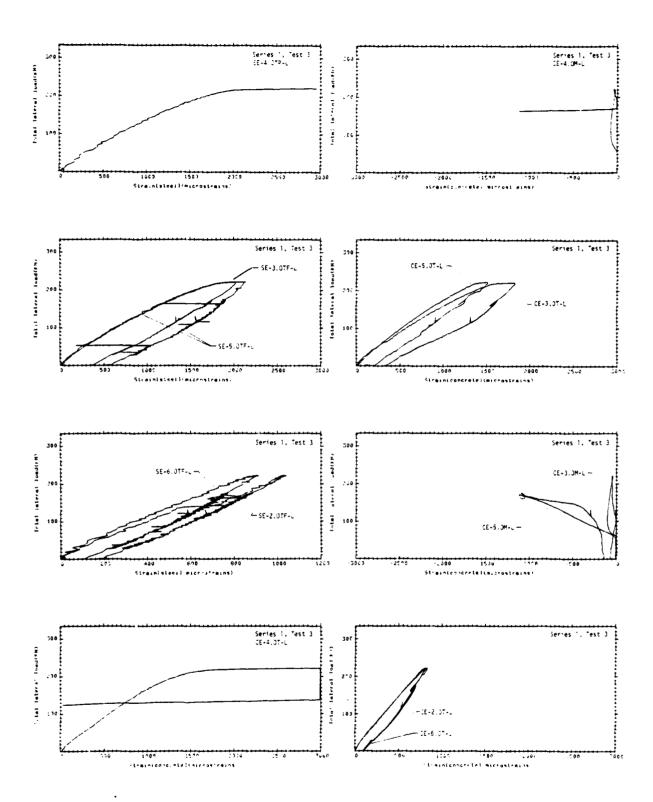
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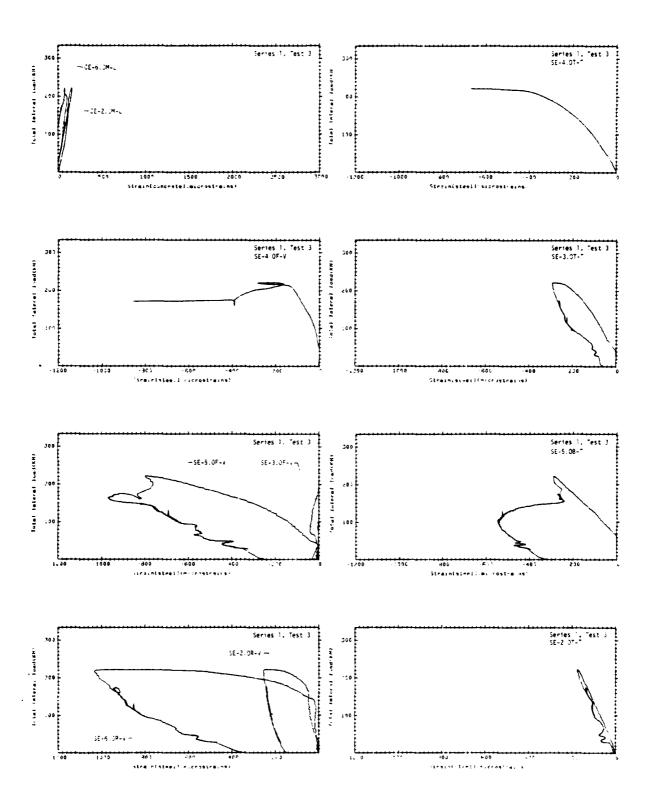


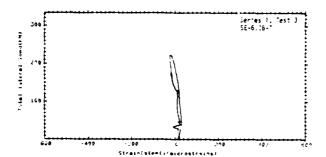
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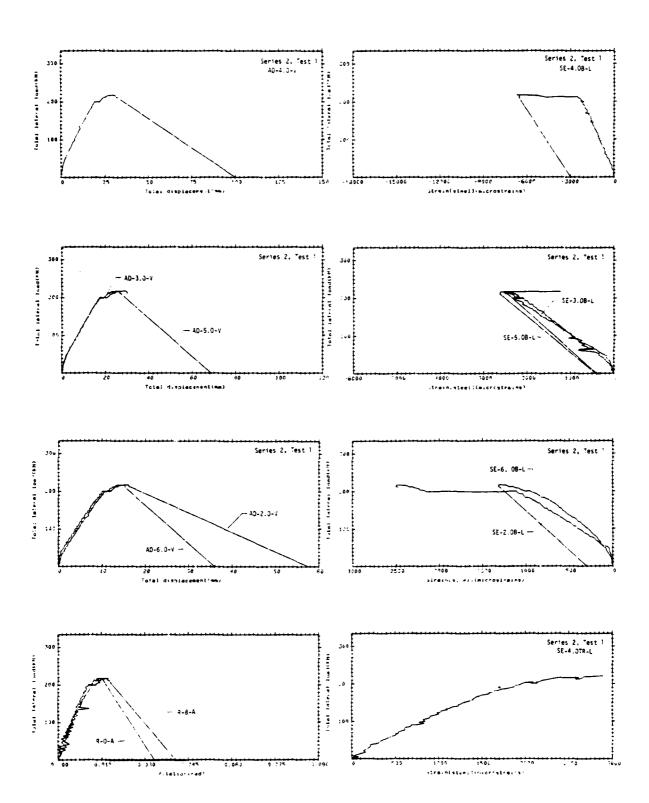


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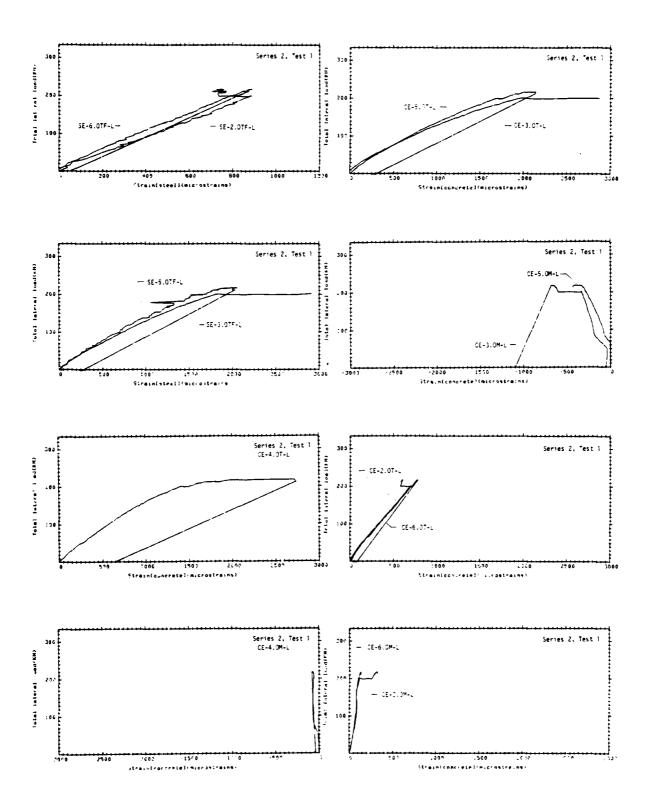


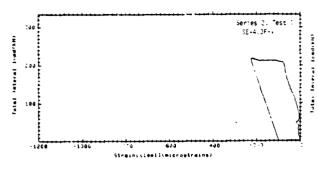


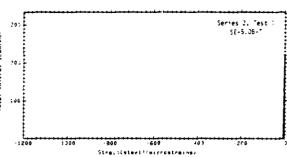


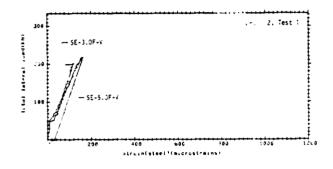


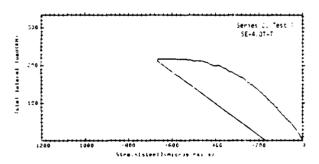
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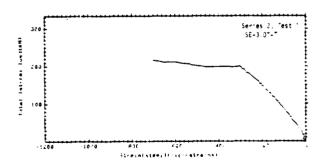




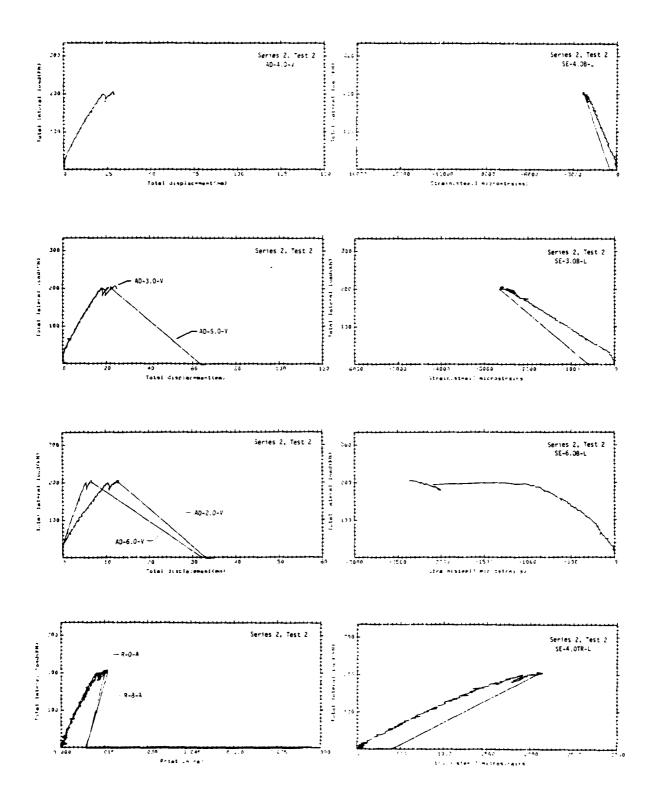


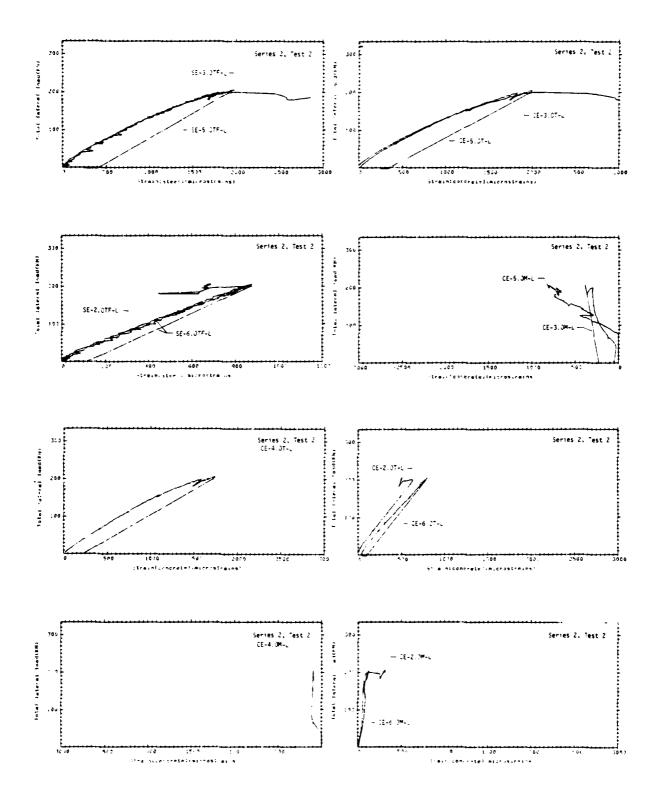




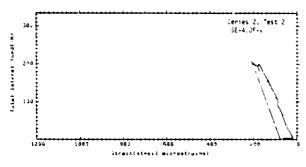


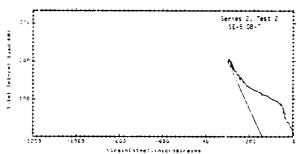
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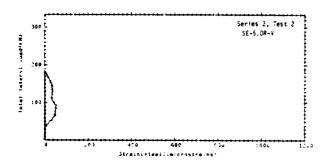


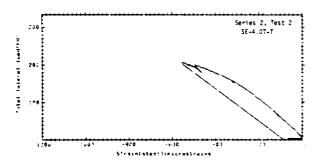


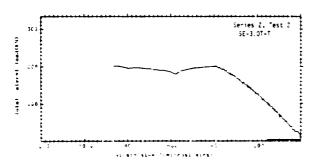
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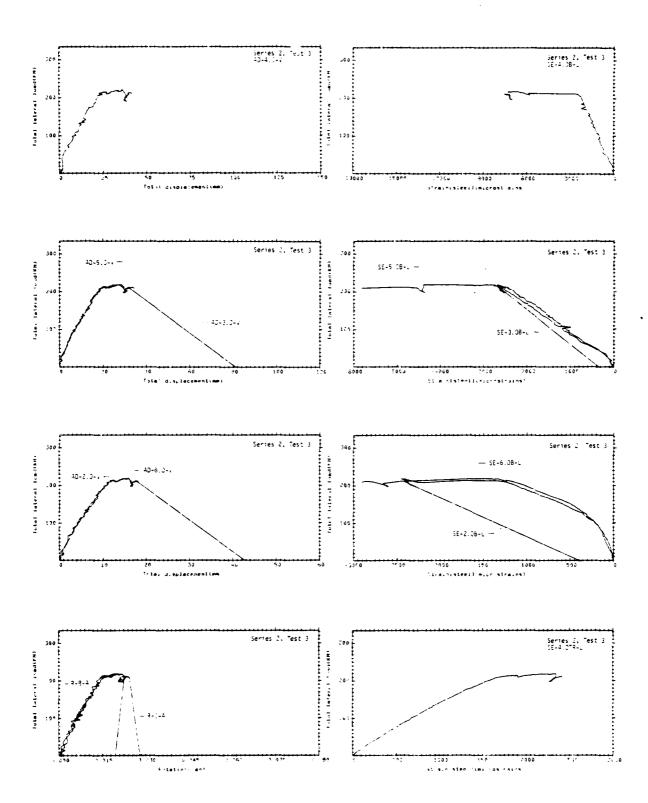


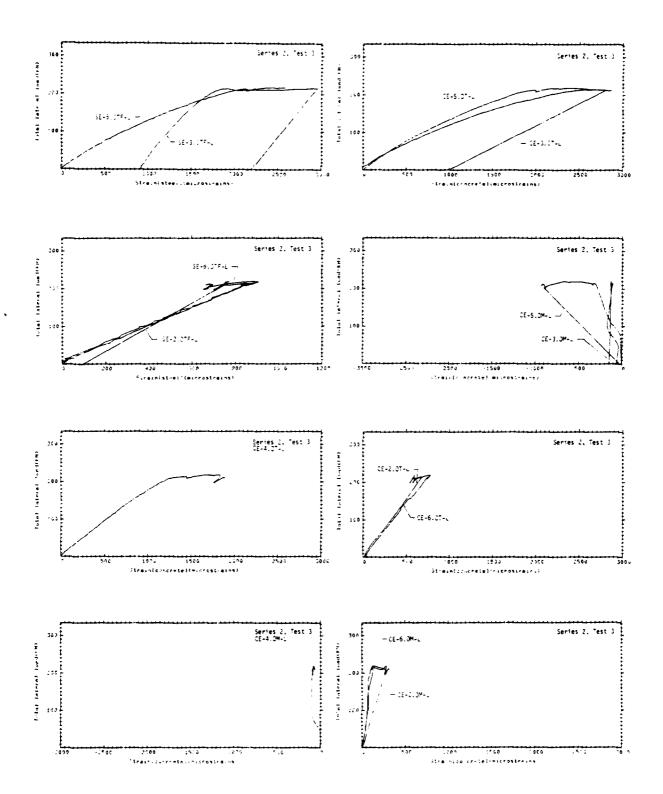


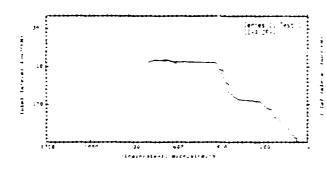


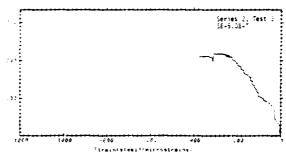


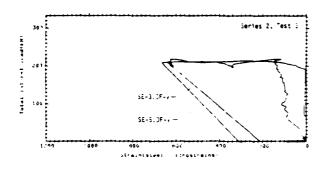


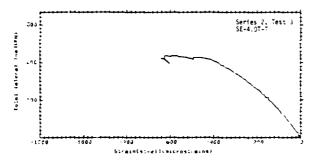


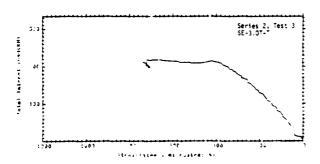


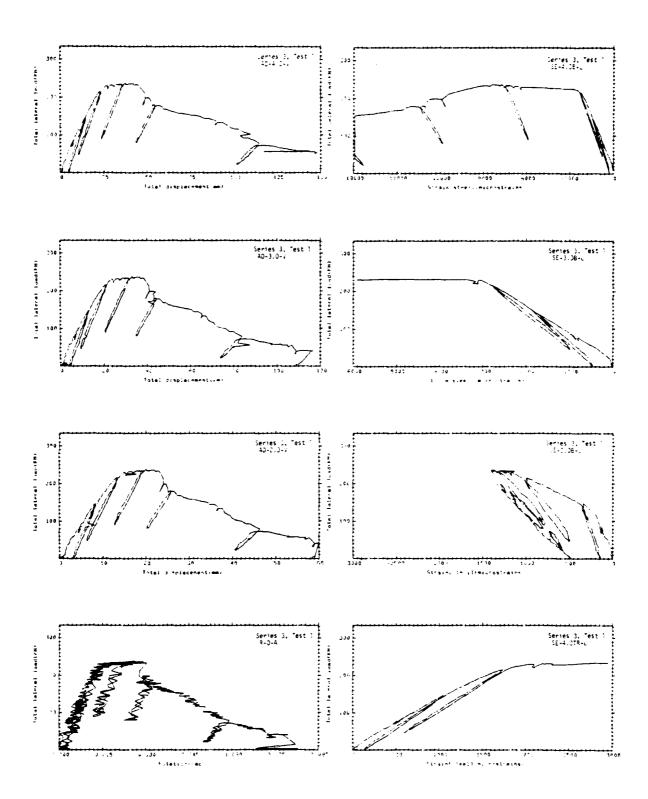


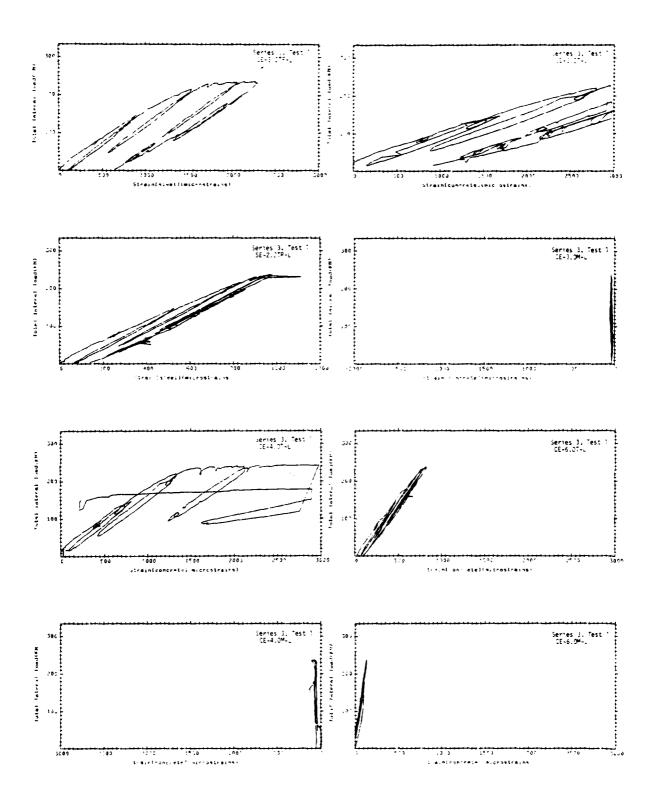


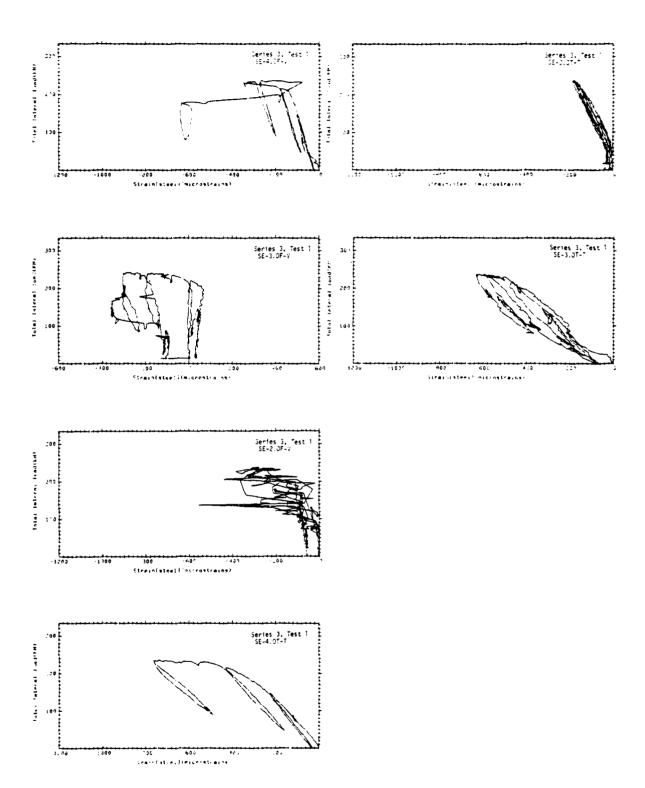


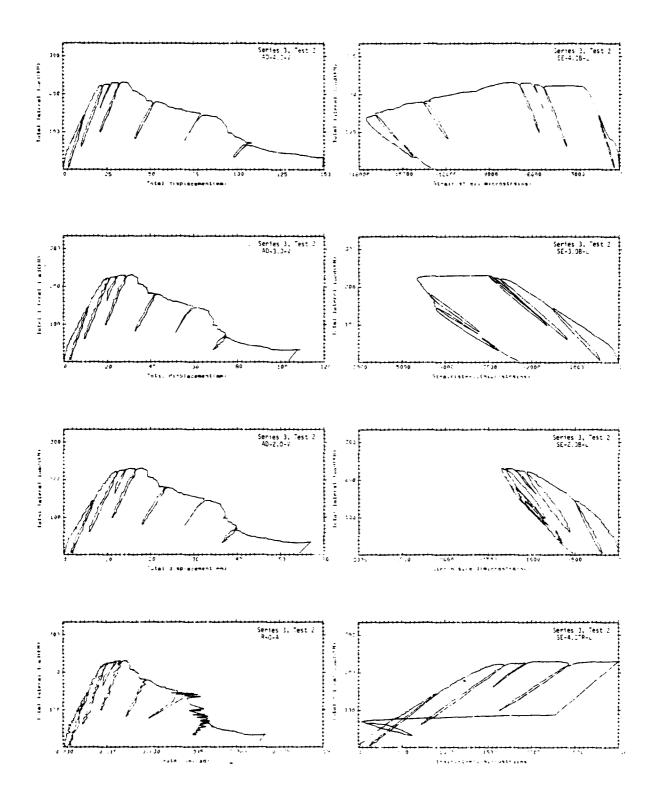


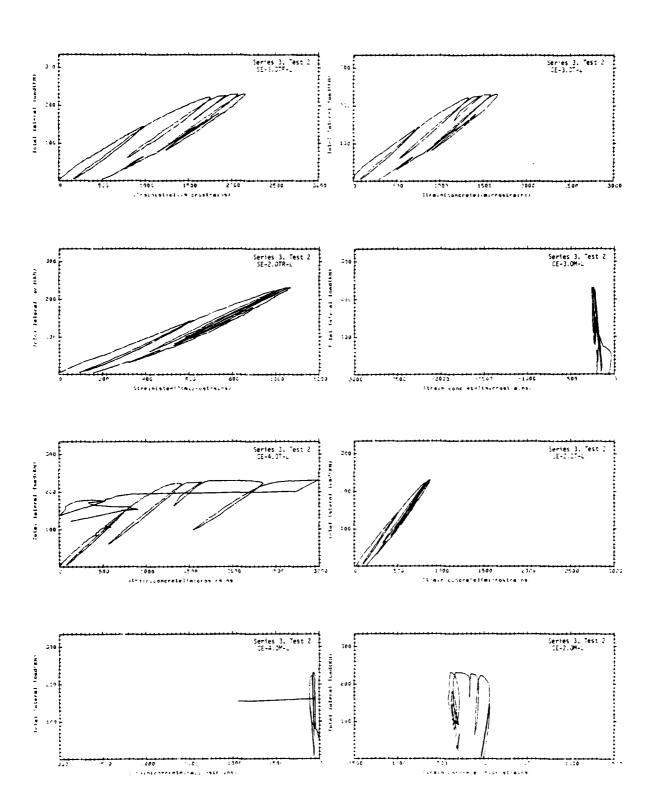


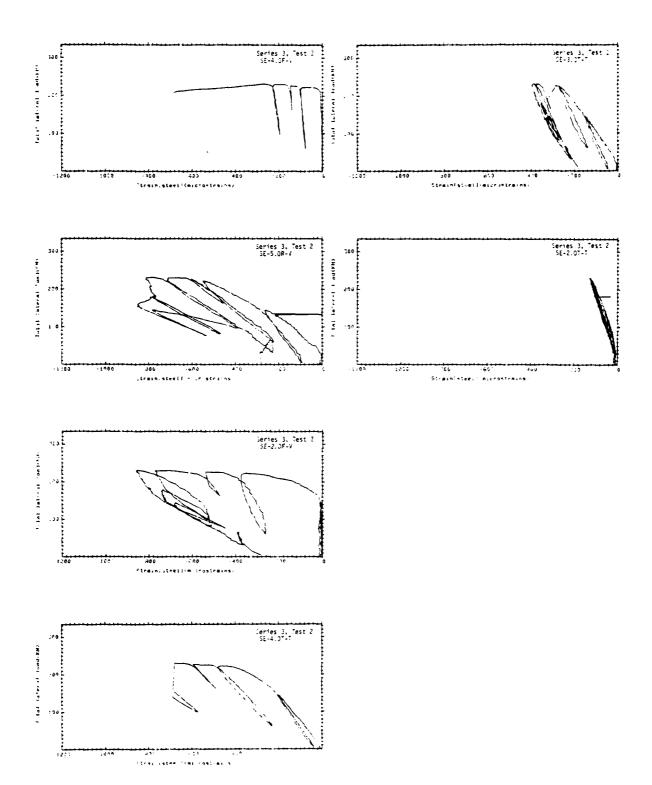




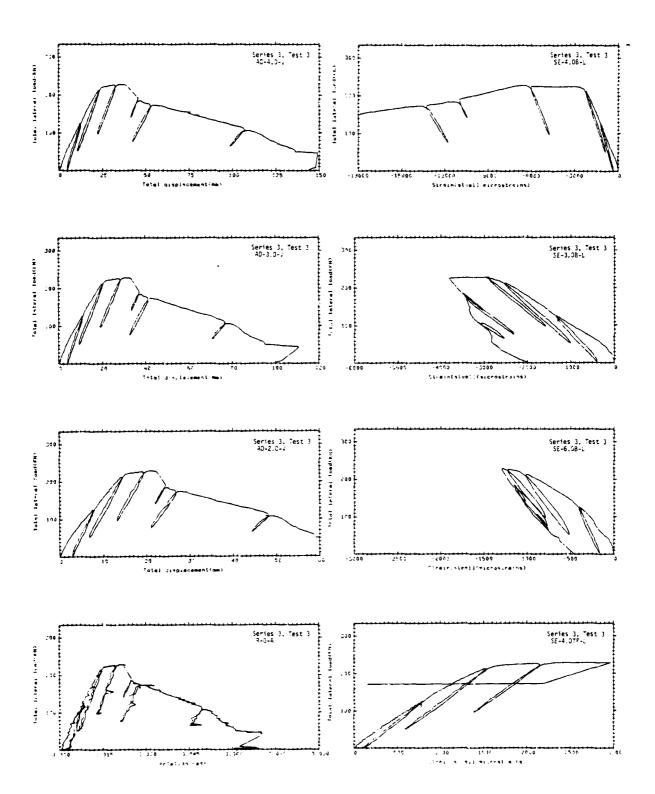


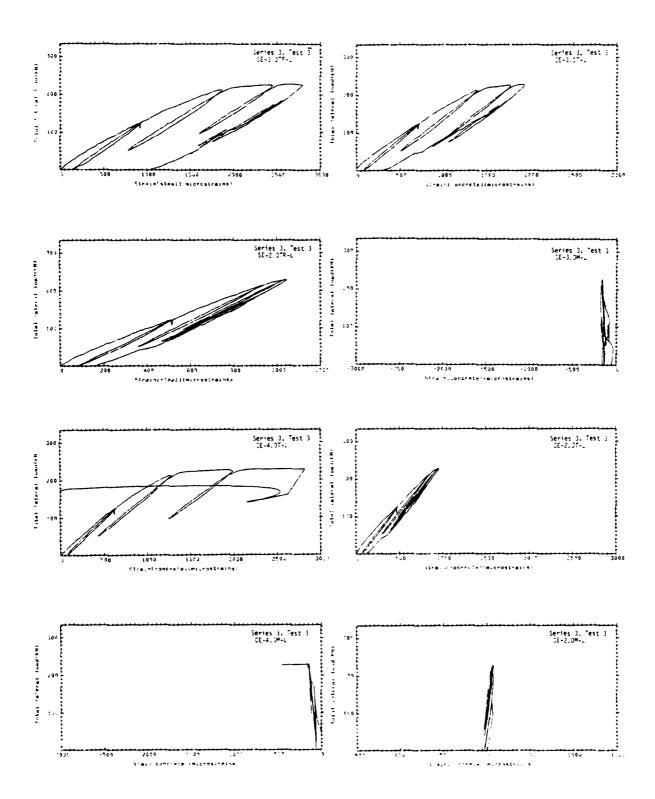


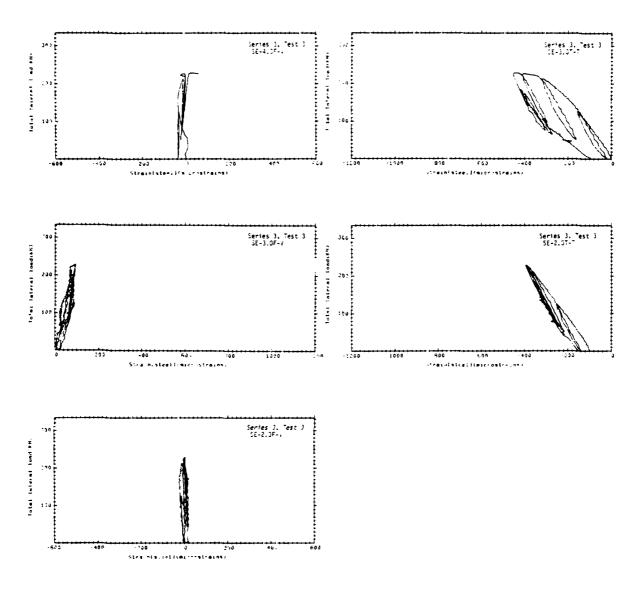


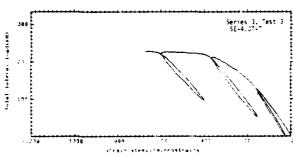


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# APPENDIX B

# THE EFFECTS OF MULTIAXIAL COMPRESSIVE LOADING ON THE RESIDUAL TENSILE STRENGTH OF PLAIN CONCRETE

by

Roger W. Meier

Kurt H. Gerstle

Hon-Yim Ko

University of Colorado, Boulder, Colorado

Submitted to

New Mexico Engineering Research Institute
University of New Mexico, Albuquerque, New Mexico

June 1981

Note: This appendix is a self-contained document, provided for the reader's information, with its own figures, tables, and appendixes.

## INTRODUCTION

A test program had been designed by others to verify general analytical formulation and prediction of the behavior of plain and reinforced concrete under general stress states. This test program consisted of tests on a series of reinforced concrete beams, carried out at the University of New Mexico, and tests on a number of plain concrete specimens cast of identical concrete, carried out at the University of Colorado, in order to obtain the material parameters required for the description of the response of the constituent plain concrete under multi-axial stress states. The results from the plain concrete test program are described herein.

## TEST PROGRAM

This test program is intended to dovetail with earlier tests (1, 2, 3) in which a concrete whose strength is similar to that of the concrete used here was tested in both biaxial and triaxial compression using a variety of different stress paths. By duplicating selected stress paths used in the previous study, the results of this test program can be compared to those of the previous program. This makes available a wealth of information which could not be obtained from the present test program alone.

This test program, as well as a portion of the previous program, was performed using a fluid-cushion cubical test cell designed to apply a uniform, homogenous stress state with a minimum of boundary constraint. The test cell, described later in this report and in Ref. 4, is capable of applying three totally independent principal stresses ( $\sigma_1 \neq \sigma_2 \neq \sigma_3$ ).

A total of 24 specimens from each of 4 batches of concrete were available for testing. Originally, four of the specimens from each batch were to be subjected to biaxial compression, six tested triaxially, and two subjected to triaxial load histories which would terminate in a biaxial stress state at failure which duplicated two of the four biaxial tests. Due to a number of complications, enumerated elsewhere in this report, specimens from two of the batches could not be used. With the loss of half of the available specimens, the last two test types had to be dropped from the program.

Table 1 summarizes the loadings used. The four biaxial compression tests include proportional loadings with stress ratios of 0:3, 1:3, 2:3, and 3:3 as shown in Figure 1. The triaxial tests consist of hydrostatic compression to two different levels, which correspond approximately to the uniaxial compressive strength and three-quarters of the uniaxial compressive strength, followed by deviation along three different stress paths at constant mean stress. These are shown in Figure 2. Path 1 is a triaxial compression in the octahedral plane (constant mean stress), Path 2 is a simple shear in the octahedral plane, and Path 3 is a triaxial extension in the octahedral plane. These stress paths will be referred to throughout this report as TC, SS, and TE, respectively.

Failure of specimens in the fluid cushion (cubical) test cell leave a sufficient portion of the specimen intact so that NX-size cores (2-1/8 inch

diameter) can be obtained from the failed specimens for split-cylinder tests to determine the residual tensile strength of the concrete following the compressive load histories in Table 1. The cores are cut into disks which are loaded diametrically to failure along one of two axes as shown in Figure 3. By testing disks from the same core in different directions,

Table 1.

Compressive Test Program

TEST	TEST TYPE	LOAD HISTORY		
NUMBER	IEST TIPE	PART 1	PART 2*	
1	Proportional	$\frac{\sigma_2}{\sigma_1} = 0/3$		
2	Blaxial to	1/3		
3	Fallure	2/3		
4		3/3		
5	Triaxial:		Path 1	
6	Hydrostatic	o <sub>o</sub> = 3.75 ksi	Path 2	
7	Compression		Path 3	
8	to o <sub>o</sub> , then		Path 1	
9	Deviatoric to	σ <sub>o</sub> = 5.00 ksi	Path 2	
10	Failure		Path 3	

Note: Three-fold replication of all tests.

\* Path 1: 
$$\Delta \sigma_1 = \Delta \sigma_2 = -\frac{1}{2} \Delta \sigma_3$$

Path 2: 
$$\Delta \sigma_3 = -\Delta \sigma_1$$
,  $\Delta \sigma_2 = 0$ 

Path 3: 
$$\Delta \sigma_3 = \Delta \sigma_2 = -\frac{1}{2} \Delta \sigma_1$$

stress-induced anisotropy may be detected. Comparison of these splitting strengths with the strengths of virgin disks cored from untested secimens will also indicate the tensile strength reductions caused by previous compressive loading.

# MULTIAXIAL TEST APPARATUS1

The multiaxial test apparatus consists of a rigid cubical space frame and six walls (faces) as shown in Figure 4. The openings in the frame form six identical cavities which, together with the adjoining walls and a pressure seal arrangement, act as six pressure vessels. The 4-inch cubical specimen is placed in the central cavity of the space frame and sealed in by the six walls, which bolt onto the frame. Loads are applied by a hydraulic pressure system which supplies silicone fluid to fluid cushions (membranes) located on the inner face of each wall. Each set of opposing walls is connected to an individual pumping system which regulates the stress level on that axis. By means of a series of valves located on a control panel, the pumping systems can be connected together such that any two axes or all three axes can be controlled by a single pump or the systems can be separated from each other completely to provide three independent principal stresses ( $\sigma_1 \neq \sigma_2 \neq \sigma_3$ ). Proximity-type transducers (probes) are used to measure the deformations in the three principal directions. The test data is monitored and plotted in real time by a microcomputer so the specimen behavior can be observed while the test is in progress. This allows the tests to be stopped exactly at failure (the definition of which is presented later in this report).

This section is rewritten in part from Ref. 4 which includes a more detailed description of the apparatus.

The walls of the test apparatus are composed of two parts. The main frames of the walls serve as the lids of the pressure vessels and include the pressure seals and hydraulic fluid ports. One of the two fluid ports serves as a pressure inlet and the other as an outlet to bleed entrapped air from the pressure vessels. The probe blocks, which bolt on the inside face of the walls, serve as bases for the displacement probes.

Details of the pressure sealing system are shown in section in Figure 5. Two O-ring grooves form the pressure seal between the wall and the frame. The inner groove seats an O-ring which seals the pressure vessel to prevent fluid from escaping outside the apparatus. The outer groove houses the O-ring built into the fluid cushions to prevent fluid from leaking into the sample cavity. Because the aluminum faces expand sideways due to Poisson's effects when fluid pressure is applied in the cavity between the wall and the specimen, the sealing capacity of this arrangement increases with cell pressure.

A polyurethane pad and a leather pad transmit the fluid pressure from the membrane to the specimen. They are flexible enough to follow minor differential distortions on the specimen surface yet provide membrane support to prevent an extrusion from occurring when a large deviator stress is present between two adjacent pressure vessels. The membrane, polyurethane pad, and leather pad are shown in Figure 6. The leather pads are made from 1/4-inch shoe leather to the approximate specifications given in Figure 7. Leather was chosen because it is pervaded by tiny air cells which absorb deformations, thereby reducing the Poisson's effects. This helps to minimize tangential stresses which could be transferred to the specimen. The hole in the center of the pad is to prevent interference between the probes and the specimen, and the 45° bevel along the edges of

the pad prevent interference between the leather pads of adjacent pressure vessels. Because the leather pad is slightly narrower than the cavity, the polyurethane pad, which is built up along its edges, is used to prevent a membrane extrusion into the space between the leather pad and the sides of the cavity.

The deformation measurement system is composed of 18 Bentley-Nevada proximitar probes (three on each face) and their supporting electronics. Each probe, operating on an induction principal, measures the width of the gap between a conductive metal target in contact with the specimen surface and a coll embedded in its tip, without requiring physical contact between itself and the specimen. Each probe is driven by its own external 18 Vdc power supply operating at 25 ma. A signal emitted by the probe is reflected by the metal target and returned to the probe. This signal varies with the distance it travels to the target and back. A data acquisition system, of which the probe drivers are a part, scans through each of the 18 probe channels and rectifies the returning signals into DC voltages. These voltage outputs are equated to gap widths by means of a calibration curve. The calibration curve is stored in the microcomputer memory and, as the voltage readings are transferred to the computer through an interface with the data acquisition system, they are automatically transformed into gap widths.

The probe targets are 4-inch square sheets of 0.012 in. thick brass shim stock. To reduce the transverse stiffness of these sheets so they can conform to the shape of the deformed specimen surfaces, the targets are cut in the pattern shown in Figure 8. The dotted circular areas show the regions at which the proximeter probes are aimed. Note that no slits enter

these regions as they would scatter the signal and cause erroneous deformation readings.

The proximeter probes are positioned so that the probe arrangement on each wall is a mirror image of that on the opposing wall. By comparing the outputs of opposing probes as a test progresses, the deformations of the specimen-spparatus system are determined. Because the probes are mounted on the faces, which deform during a test, the deformations of the apparatus must be subtracted out before the actual specimen deformations can be found. This is discussed in detail in the section titled "Box Calibration". The advantage of using opposing probes to determine deformations is that rigid body translations are automatically eliminated from the calculations. In addition, because the three probes on each face are equidistant from the center of the face and located 120° apart, rigid body rotations can also be eliminated by averaging the three probe readings.

#### SAMPLE PREPARATION

Concrete specimens to be used in the cubical test cell are cast in steel molds with inside dimensions of 4 inches square by either 4 inches or 4-1/8 inches in height. The concrete is placed without floating or trowelling in order that concrete remains above the tops of the mold. This excess concrete is cut off using a diamond-bladed masonry saw to ensure a specimen height of  $4.00 \pm 0.02$  inches and a completely planar surface.

Because small voids near the surface of the concrete will allow penetration of the flexible membranes, resulting in the rupture of the fluid cushion, the central portion of all six faces are sandblasted to expose these voids. The sandbiasted areas are then filled with a plastic wood filler material (Durham's Rock Hard Water Putty) and smoothed out as much as possible with a 1-inch putty knife and 5-inch broad knife. After drying for 24 hours, the puttied surfaces are belt-sanded. Any holes uncovered by the sanding are reputtled and the surfaces are finished with hand sanding using 400-grit paper. A typical specimen, finished and ready for testing, is shown in Figure 9.

## CUBICAL CELL CALIBRATION

An essential component of the data reduction process is the correction for the deformations of the cubical cell itself during a test. These deformations arise from the reaction forces to the fluid pressure on the specimen and the lateral expansion of the cavity which contains the fluid cushion and are of a comparable order of magnitude as the deformations of the concrete specimen.

The cubical cell is calibrated by applying an incremental, monotonically-increasing uniaxial stress to an aluminum specimen with known stress-strain response. Each axis of the cubical cell is loaded separately as the response differs slightly from axis to axis. The pressure is generally increased in load steps of 500 psl up to the maximum stress which can be expected during the test program. For this test program, the maximum expected stress was 15,000 psl which corresponds to the limiting stress state  $\frac{1}{1} = 15000$ ,  $\frac{1}{2} = \frac{1}{3} = 0$  in the 5000 psl octahedral plane. Each axis is loaded a minimum of three times using the same load steps each time to ensure that the observed response is truly representative. During the calibration test, at the end of each load step, the total deformation

in terms of changes in gap widths is measured in each of the three axis directions of the cubical cell. By subtracting the calculated response of the aluminum cube from the observed total deformations, the deformations of the cubical cell are computed. For each stress level, s, at which measurements are taken, a calibration array is compiled in the form

$$\begin{bmatrix} d_{xx} & d_{xy} & d_{xz} \\ d_{yx} & d_{yy} & d_{yz} \\ d_{zx} & d_{zy} & d_{zz} \end{bmatrix}$$

where  $d_{i,j}$  denotes the deformations of the cubical cell in the i-direction due to an applied stress, s, in the j-direction.

During a test, the cubical cell deformations in any direction, j, are computed by superposition of the terms  $d_{jx}^r$ ,  $d_{jy}^s$ , and  $d_{jz}^t$  where r, s and t represent the stress levels in the x, y, and z directions, respectively. Because the response of the cubical cell is nonlinear, superposition is not strictly valid. Triaxial tests on an aluminum specimen with known elastic parameters, however, have shown this method of computing cubical cell deformations to be reasonably accurate. Above approximately 10,000 psi, the cubical cell response is linear and the validity of superposition is no longer in question; thus, the accuracy of the corrected specimen deformations is improved as the stresses approach the failure state.

The cubical cell was calibrated immediately before proceeding with this testing program and during this time, it was observed that the response of the cubical cell at low pressures (below 1000 psi) varied with successive loadings. The variation in the deformations within this stress range is attributed to movement of the probe target before it becomes firmly seated against the specimen, and thus represents neither

deformations of the specimen nor of the cubical cell. Because strain calculations are made using the relative changes in gap width since the start of the test, this initial uncertainty as to the distance from the proximitor probes to the face of the specimen would affect the calculated response of the specimen during the entire test by presenting a false starting point on the stress-strain curve and errant initial moduli.

In order to eliminate these false initial gap width measurements, the cubical cell was completely recalibrated using the gap widths at 100 psi as the reference point for subsequent deformation calculations. It was felt that 100 psi would be sufficient to seat the targets firmly against the specimen and that the continued application of at least 100 psi on all axes (regardless of test type) throughout a test would preclude target movements which were independent of the movement and deformation of the specimen. Furthermore, the deformations of a concrete specimen under a hydrostatic stress of 100 psi are negligible in comparison to the total deformations experienced by the concrete during the rest of a test; thus the gap widths as measured at 100 psi can be assumed to be equal to the gap widths which would have been measured in a completely unloaded state.

It is apparent in the stress-strain curves of Appendix B that most but not all of the uncertainty has been eliminated. Some of the tests show a virtual expansion of the specimen upon first loading. This results from less cubical cell deformation than is allowed for in the calibration array and can be eliminated, when necessary, by shifting the stress-strain curve along the strain axis by the amount required to eliminate the anomaly. It was felt that any attempts to further eliminate these discrepancies by beginning the tests at a stress in excess of 100 psi would not be prudent. Although the results of triaxial tests should not be affected by the use of

a nonzero stress to represent the unloaded condition, the results of blaxial tests might be suspect. Because the minimum pressure of 100 psi must be maintained throughout the test, even on what should be the unloaded axis, a truly blaxial state of stress cannot be achieved. Because the 100 psi reference state on the unloaded axis of a blaxial test is at most only 4 percent of the maximum deviator stress at failure, it was assumed that little effect would be noticed.

#### STRESS-STRAIN-STRENGTH BEHAVIOR

At the outset of this testing program, it was decided that the specimens should be tested in such a manner that inherent anisotropy may be identified. To this end, a method of labeling the specimens was devised such that the concrete batch as well as the mold used and the orientation of the specimen in the mold could be determined. The first batch of concrete was cast in New Mexico prior to receipt of the labeling instructions, hence Batch 1 specimens were eliminated from the testing program.

Shortly after starting the testing program, some concern arcse as to variations in the properties of the remaining three batches of concrete. Because two TE 3750 tests had already been performed which showed a marked dissimilarity in stress-strain behavior between a specimen from Batch 3 and a specimen from Batch 4, a series of TE 3750 tests was begun to investigate the the possibility of a systematic difference. The series was to consist of six tests using two specimens from each of Batches 2, 3, and 4. It soon became apparent that a systematic difference did exist between those specimens taken from Batch 3 and the specimens from Batches 2 and 4. One

of the tests on a specimen from Batch 2 was unsuccessful due to an equipment malfunction, however the very close agreement between tests on the two specimens from Batch 4 and the successful test on one specimen from Batch 2 was deemed sufficient to preclude a third test on a specimen from Batch 2. A third test was performed, however, on another cube from Batch 3 to provide a better statistical average of the stress-strain behavior of specimens from that batch.

Figures 10 and 11 show the results of the three tests on specimens from Batch 3 and the three tests on specimens from Batches 2 and 4, respectively. Although the tests on Batch 3 specimens exhibit considerably more scatter than the tests on Batch 2 and 4 specimens, a comparison of the average response of the two test groups, as shown in Figure 12, indicates the differences in behavior. The specimens from Batch 3 appear to have lower moduli and more ductility (defined here by the maximum deviator strains near failure) than the specimens from Batches 2 and 4, which have nearly identical responses. In addition, specimens from Batch 3 consistently failed at lower values of the maximum principal stress. Table 2 these differences are quantified as the maximum deviator stress at failure and the maximum deviator strains at  $\sigma_1$  = 5225 psi,  $\sigma_2$  =  $\sigma_3$  = 800 psi, which is the stress state with the greatest deviator stess which all six tests had in common prior to failure. From the averages of these few tests, it appears that the specimens from Batch 3 have approximately 20 percent greater ductility (deviator strains at a given stress level) and 10 percent less strength than the remaining specimens.

Table 2.

<del></del>			
BATCH	SPECIMEN	( <sup>0</sup> 1 - <sup>0</sup> 3) <sub>f</sub> (psi)	(mils/in)
2	C4	5175	1.464
4	D2	5175	1.450
4	<b>A</b> 6	5100	1.270
Aver	age	5150	1.395
3	B5	4650	1.767
3	B6	4200	1.688
3	C2	4875	1.648
Average		4575	1.701
	<del></del>	<del></del>	

<sup>\*</sup> at  $\sigma_1$  = 5225 psi,  $\sigma_2$  =  $\sigma_3$  = 800 psi.

Based on these findings, specimens from Batch 3 were also eliminated from further consideration. It should be noted that three other specimens from Batch 3 were used in tests prior to the decision to eliminate that batch. Now that sufficient data has been accumulated on the test types involved, it can be seen that the Batch 3 specimens exhibited greater ductility and lower strengths during these tests as well. The tests involved were a TC 3750, a TC 5000, and a TE 5000. The results of these tests as well as the TE 3750 tests are included in Appendices A and B.

With only two remaining batches from which to obtain test specimens, the goals of the testing program were changed to require only two-fold replication of each test type. Since no systematic differences could be detected between the properties of specimens from Batches 2 and 4, further

testing was performed on cubes selected at random rather than using a cube from each batch for the two-fold replication. In order to compensate for the change in the degree of replication, attempts were made to obtain two tests for each test type for which the results were as nearly identical as possible. In the attempt, three tests were sometimes performed with the result that two tests exhibit quite similar stress-strain behavior while a third test exhibits behavior which is similar but not in as close agreement. Given the statistical nature of concrete, those test types for which three tests were performed can be considered to have the three-fold replication which was originally required. Given the limitations on the number of specimens available, however, some tests resulted in close enough behavior agreement that a third test was unwarranted.

In order to investigate the possibility of inherent anisotropy in the specimens, a standard convention was established whereby the z-axis of the cubical cell (the vertical axis) was always the major principal stress axis. In this way, the orientation of the specimen in the cubical cell would determine which axis of the specimen was loaded with the major principal stress. In a similar manner, the x-axis of the cubical cell was always the minor principal stress axis. With this method, any strain anomalies which arose due to inaccurate calibration of the equipment could be seen (for example, if the z-axis of the cell always resulted in the largest strain regardless of cube orientation) and any systematic anisotropy in the specimens could be detected.

Because of the statistical nature of concrete, any quantification of anisotropy must be viewed relative to the overall scatter of results.

Table 3 shows the variation in the tangent bulk modulus at a hydrostatic stress of 3500 psi, which is the highest hydrostatic stress common to all

of the triaxial tests. By using the bulk modulus, which in effect averages the strains, the variability of properties from cube to cube can be estimated. The standard deviation of the bulk modulus with respect to the mean is  $\pm 15.6$  percent. Table 4 shows the greatest difference between any principal strain  $\epsilon$  and the average strain  $\overline{\epsilon}$  at the same hydrostatic stress of 3500 psi for each of the tests. This quantity is expressed as a percentage relative to the mean and can be equated to the greatest amount of anisotropy exhibited by the specimen. The average degree of anisotropy is 9 percent. From this it can be assumed that no systematic anisotropy exists since the scatter of strain values within the individual cubes is far exceeded by the scatter of data among all of the cubes. The values listed in Table 4 occurred on various axes of the cubes with no one axis showing a predominance. Therefore these specimens can be considered to be isotropic and the stress-strain behavior of different tests can be compared without regard to specimen orientation.

Table 3.

TEST	K <sub>†</sub> * (10 <sup>6</sup> psi)	TEST	K <sub>†</sub> * (10 <sup>6</sup> psi)
5A	1.538	8A	1.483
5B	2.201	8B	1.580
5C	2.355	8E	1.925
6A	1.840	9A	1.994
6B	2.222		
6C	1.890	9C	2.009
7B	1.881	10A	1.519
7 <b>F</b>	1.556	10B	1.389
7G	1.609	1 OC	1.721

Average:  $1.807 \times 10^6$  psi Standard Deviation:  $\pm 0.28\% \times 10^6$  psi (15.6% of mean)

<sup>\*</sup>Tangent Bulk Modulus at  $\sigma_{\rm oct}$  = 3500 psi

Table 4.

TEST	( € <del>-</del> € ) * <del>=</del> (\$)	TEST	$\frac{(\varepsilon - \overline{\varepsilon})^*}{\overline{\varepsilon}}$
5A	9.39	8.8	6.40
5B	15.44	8B	4.97
5C	18.34	8E	17.89
6A	6.48	9A	6.38
6B	13.18		
6C	10.26	9C	7.08
7B	13.18	10A	3.41
7F	6.00	108	4.00
7G	2.93	1 OC	6.05

Average: 8.9%

Standard Deviation: ± 4.8%

(54% of mean)

\*at  $\sigma_{\text{oct}}$  = 3500 psi

# TRIAXIAL TEST RESULTS

Prior to the presentation of the failure results, it is important to define the criterion used in this study. Because of the need to obtain intact cores from the failed specimens, the tests could not be continued to the point at which uitimate strength was reached, i.e., the stress state at which physical separation along a shear surface occurs. Instead, the definition of failure used by Bieniawski (5) to describe brittle failure of rocks and Newman (6) to describe the failure of concrete was applied.

These investigators describe the failure mechanisms of brittle materials (which includes concrete) in three stages. The first stage consists of a nearly linear stress-strain response associated with very small amounts of propogation of pre-existing bond cracks at the mortaraggregate interface. The second stage, the beginning of which is reflected in a deviation of the stress-strain curve from linearity, is characterized by an increase in the number and length of the bond cracks which propogate in a stable (stress-dependent) manner. This stage proceeds up to approximately 80 percent of the ultimate load. The third stage begins when the bond cracks become unstable, continuing to propogate without an increase in stress, and join together to form mortar cracks. The stress state at the start of this third stage, called the "discontinuity point" by Newman, is taken to be the failure state. The reason for this is that the unstable growth of cracks beginning at this stress level can conceivably continue until enough cracks join that the specimen is physically separated; all without a further increase in stress. As these cracks propogate, separating more and more material, the specimen expands. This expansion is reflected in a reversal of the volumetric strain curve. Therefore, the "discontinuity point" is synonymous with the point at which the volumetric curve changes directions. Because this reversal is generally gradual, a more rigorous definition of the discontinuity point is the point at which the volumetric strain curve achieves an instantaneous vertical slope.

Since a stress-strain curve is plotted in real time during a test, the discontinuity point is fairly easily identified and the test can be stopped in order to prevent further damage to the specimen. In order to ensure that this point had actually been reached, the tests were actually taken

one or two load steps (stress increments) further. If the volumetric strain curve continued to show expansion after these load steps, the test was stopped.

The results of the triaxial test series (which can be found in their entirety in Appendix B) are summarized in Figures 13a through 13f. The solld lines in these figures represent the average stress-strain response for each test type up to the point of failure. The shaded regions indicate the range of strains actually observed in the tests. It is evident that a fairly high degree of reproducibility was achieved for every test type.

Tables 5 and 6 summarize the stress states at failure in terms of the octahedral normal stress (whose value is included in the path designation) and two commonly used measures of shear stress — the deviator stress ( $\sigma_1$  —  $\sigma_3$ ) and the octahedral shear stress  $\tau_{oct}$ . This data is also presented in Figure 14a as failure envelopes in the two octahedral planes investigated. Because the tests were performed using incremental loading, the failure stresses can only be defined to the nearest 100 psi in most cases; thus the deviator stresses are accurate to within 2 percent of the octahedral normal stress values.

It was mentioned earlier that the stress paths and octahedral planes were chosen so as to coincide with a previous test program which included cubical cell testing of a concrete with a uniaxial compressive strength similar to that of the concrete used in this study. The results of standard uniaxial compression tests on 6 in. by 12 in. cylinders performed as part of the testing program undertaken by Gerstle, et al. indicate a strength of 4600 psi. From the results of uniaxial compression tests performed at the University of New Mexico on cylinders cast from Batches 2

Table 5.
(All units are in psi.)

TEST	PATH	σ <sub>1</sub> - σ <sub>3</sub>	<sup>T</sup> oct
5B		8400	3842
5C	TC 3750	8250	3889
Aver	age	8325	3866
6A		7000	2858
6B	SS 3750	7100	2899
6C		7200	2939
Aver	age	7100	2899
7B		5100	2404
7F	TE 3750	5175	2440
7 <b>G</b>		5175	2440
Aver	age	5150	2428

Table 6.
(All units are in psi.)

		<del></del>	
TEST	PATH	σ <sub>1</sub> - σ <sub>3</sub>	T oct
8B	TO	10200	4808
8E	TC 5000	10350	4879
Aver	age	10275	4844
9 <b>A</b>	SS 5000	8800	3593
9C		9200	37 56
Aver	age	9000	3675
10A	TE	6750	3182
1 0C	5000	6975	3288
Average		6850	3235

and 4, a uniaxial strength of 5215 is indicated. Figure 14b shows the failure envelopes in the 5000 psi octahedral plane resulting from the present study (identified as AFWL) and the previous study. The octahedral shear stresses at failure for the concrete used by Gerstle, et al. appear to be approximately 15 percent greater. Some of this difference is due to the slightly greater strength of the concrete, indicated by the higher uniaxial compression strengths, while a portion of the difference is undoubtedly the result of the slightly different definition of failure used in the previous study. Although Starovisky (3) recognized the discontinuity point as an indication that failure had occurred, the data acquisition system did not provide for real time plotting of the stressstrain response when she was doing her testing. With no indication of the strain behavior, she relied on a sudden drop in pressure, which was most likely due to a sudden increase in strain in one direction, to define failure. Although the sudden increase in strain is usually accompanied by a reversal in the volumetric strain curve, the results of many of her tests, once plotted, showed that the discontinuity point had not yet been reached. This could account for much of the remaining difference.

# BIAXIAL TEST RESULTS

The results of the biaxial test series, which can be found in Appendices C and D, show much less reproducibility than those of the triaxial tests. This is most evident in the scatter of failure stress states shown in Figure 15. A large amount of scatter is to be expected because the fluid cushions provide little constraint, allowing the specimen to fail in a brittle manner. This brittle failure is dependent on random

weak areas within each specimen; when the weakest portion fails, the entire specimen fails in the absence of any means of stress redistribution. Clearly, three-fold or even four-fold replication would have been preferable in this biaxial test series. Because the entire supply of specimens from Batches 2 and 4 had been exhausted, further testing, however much warranted, was impossible.

For the unlaxial stress path (stress ratio of 0:3), only one successful test was performed using cubes from Batches 2 and 4. Because the supply of cubes had been exhausted, a specimen from Batch 3 was tested in order to provide indirect supportive data. This specimen failed at a stress of approximately 4200 psl as compared to the strength of 4550 psi observed for the specimen from Batch 2 (Test 1A in Table 7). It was previously mentioned that Batch 3 has roughly 10 percent less strength than Batches 2 and 4. This strength difference seems to have been preserved in these tests as well.

Table 7.

STRESS	BATCH 2,4		BATCH 3	
RATIO	TEST	σ <sub>lf</sub>	TEST	σ <sub>lf</sub>
	NUMBER	(psi)	NUMBER	(psi)
0:3	1.A	4550	1C	4200
1.7	2B	8400	2A	6900
1:3	2C	7500	20	6700
Average		7950		6800
	3A	6900		
2:3	38	9000		
	3C	9000		
Average		8300		
	4A	6300	1	
3:3	4E	7250		
Average		6775		

Another indication that the single failure point obtained for uniaxial loading is reasonable comes from the previous study. Results of that study indicate that the uniaxial strength of concrete as measured in the cubical cell is approximately 90 percent of the strength as measured using 6 in. by 12 in. cylinders in a conventional testing machine. The strength of 4550 psi measured in the cubical cell is nearly 90 percent of the cylinder strength mentioned previously. This evidence suggests that a fair amount of confidence can be placed in this data point.

Similar supportive data from Batch 3 specimens has been provided for the biaxial tests with a stress ratio of 1:3. Table 7 shows that the average strength of the specimens from Batch 3, expressed as the major principal stress at failure, is 15 percent less than the strength of specimens from Batches 2 and 4. This would suggest that the strength of 8400 psi measured in Test 2B is a reasonable upper limit to the actual strength value.

The two equi-biaxial tests (stress ratio of 3:3) performed show similar stress-strain behavior despite the 1000 psi difference in strengths. It must be noted that Test 4A was never completed due to the rupture of one of the fluid cushions. An extrapolation of the volumetric strain curve would indicate a vertical slope within one or two more load steps. Therefore, the maximum principal stress at the point at which the test was stopped is taken to be the failure stress, although it is more likely that the actual failure stress is a few hundred psi greater.

The average of the biaxial test results is shown in Figure 15a as the solid curve above the equi-biaxial line. Because of the large amount of scatter of the few data points available, which are indicated by the open

circles below the equi-biaxial line, this curve should be looked upon more as just a mathematical average than a representation of the average properties of the concrete. For convenience, however, this average curve has been reproduced in Figure 15b along with the results from the previous testing program. The higher ratios of biaxial strengths to unlaxial strength in the present study are due, in part, to the higher concrete strength and different failure criterion mentioned previously.

Because of the limited amount of data, it is impossible to determine what effect the 100 psi reference stresses had on the strength results. Research is presently underway, however, which will duplicate the biaxial tests performed in the previous study using an identical concrete mix. These tests will be performed with the 100 psi reference state, thus allowing a determination of its effects. An addendum to this report will be provided once the research is completed.

# RESIDUAL TENSILE STRENGTH STUDY TEST PROCEDURES

The original goal of this portion of the testing program was to obtain an NX-size core along the intermediate principal stress axis and to subdivide this core into four 1-inch thick disks. When actual coring was begun, however, it was found that insufficient intact material existed at the points of entry and exit of the coring bit to allow use of the entire 4-inch length of the core. As the core was cut into disks using a masonry saw which had a kerf of slightly more than 1/8 inch, further reduction in the amount of usable length of the core occurred. In order that the disks would have as great of a cross-sectional area as possible while still

providing a measure of redundancy in the testing program, it was decided that three disks would be taken from each core rather than four. Each of these disks would have a one-inch thickness as was originally proposed. Two of the disks from each core were tested immediately and the third was held in reserve. Once all of the disks had been tested, those held in reserve were used to fill any gaps in the data resulting from clearly erroneous results (such as a compressive mode of failure in a disk) and to provide another data point in those instances where the response was not well-defined by only two data points.

Another problem came to light during the coring operation involving the quality of the core geometry. Because of the heterogeneity of the concrete, the coring bit would tend to wander, first in one direction and then in another, depending on the direction which offered the least resistance to cutting. If there were a number of pieces of hard aggregate on one side of the bit but only mortar on the opposing side, the bit would move toward the mortar. The result of the bit taking this "path of least resistance" was a core with irregular sides. Any attempt to perform a tensile splitting test on these disks would result in point loads being applied only at the highest points on the circumference.

It has been estimated (7) that the actual loaded area in the tensile splitting test is approximately 3/16 inch wide for this size core. To eliminate the irregularities along the sides of the disks, a 1/4 inch wide flat was ground on each side of the disk as shown in Figure 16a. This was the narrowest flat which would eliminate all of the irregularities. The work was performed on a milling machine to ensure that the flats would be exactly perpendicular to the desired loading axis. With these flats on the disks, the testing procedure recommended by the International Society of

Rock Mechanics (8) could no longer be used. Instead, the tests would be performed per ASTM C-296 which specifies that the load be applied through an inch-wide strip of wood or masonite which extends over the length of the disk. It was anticipated that any anomalies in the stress field resulting from the shape of the loading area would disappear a short distance into the disk, according to St. Venant's principle, leaving a predominantly tensile stress field across most of the remaining diameter.

Preliminary testing of these modified disks indicated, by the mode of failure of the disks, that a compressive stress regime existed in the loaded disks. The mode of failure observed is illustrated in Figure 16b. Because some of the disks had already been provided with flats, any further modifications to provide tensile splitting had to incorporate the flats. It was decided that a line load would be applied at the center of the flats (and thus exactly in the plane of splitting) by means of a length of 1/8-inch square aluminum key stock. Figure 16c illustrates this method of loading and the resulting failure surface in the disks, which indicates that a tensile splitting failure mode had indeed been established.

Because of this unconventional method of testing, the results of this portion of the testing program cannot be compared to tensile splitting tests performed at the University of New Mexico on cast concrete cylinders. It is possible, however, to compare the results of these tests to each other as all disks were ground and loaded identically using the same key stock and the same rate of loading. In addition, tensile splitting tests on disks taken from previously unloaded specimens were provided as a firm basis for comparison of the tensile splitting strength results.

In order to keep track of the orientation of the tensile failure surfaces with respect to the previous load histories of the specimens, a

notation convention has been established which is based on an arbitrary but fixed orientation of the specimen in physical space. The coordinate axes used to describe physical space are shown in Figure 17a along with the Cartesian coordinate system from which is was adapted. This coordinate system adheres to the right-hand rule of Cartesian coordinates with x, y and z replaced by 1, 2 and 3, respectively. Prior to the beginning of a testing program, the specimens are assigned an orientation in physical space. In this program, for example, the vertical axis of the cubes while still in the molds was designated the 1-axis. The long axis of the molds was chosen to define the 3-axis, and the direction perpendicular to the long axis of the molds in the horizontal plane was designated the 2-axis. This is shown in Figure 17c.

The orientation of the measured tensile splitting strength is denoted within this coordinate framework by  $t_{ij}$  (i,j = 1,2,3), the residual tensile strength in the j-direction of a specimen originally subjected to a major principal stress in the i-direction. If the principal stresses are applied in directions which adhere to a right-hand rule, describing the axis of the specimen on which the major principal stress acts automatically reveals the axes of the specimen on which the intermediate and minor principal stresses act.

The advantage of this convention lies in its ability to describe the direction in which tensile strength is measured relative to not only the directions in which stresses were applied during a previous load history but also relative to any directions of inherent anisotropy. A difference between  $t_{13}$  and  $t_{31}$  would be relevant if, for example, the specimens were inherently stronger in the 1-direction.

Because the specimens in this study exhibit negligible anisotropy, and because the specimens were always cored in the direction of the intermediate principal stress, no attempt will be made to distinguish between  $t_{13}$  and  $t_{31}$  or  $t_{11}$  and  $t_{33}$ . Instead, for simplicity, the tensile strength in the direction of the previously applied major principal stress will be denoted by  $t_{11}$  and the tensile strength in the direction of the previously applied minor principal stress will be denoted  $t_{13}$ .

# RESIDUAL TENSILE STRENGTH STUDY TENSILE SPLITTING TEST RESULTS

As a control measure, tensile splitting tests were performed on nine disks cut from three specimens which had not been subjected to previous loads. The results of these nine tests, which had an average strength of 433 psi, are given in Table 9. In order to give a qualitative meaning to the tensile splitting test results, all splitting strengths are normalized with respect to this average control strength. These normalized strengths,  $t_{11}/t_c$  and  $t_{1j}/t_c$ , can be viewed as measures of the percentage of strength remaining in a specimen after loading. Conversely, the quantity  $(1 - t/t_c)$  expresses the relative amount of degradation resulting from the loading. Table 10 lists all of the splitting test results from specimens which had been loaded triaxially. The results are also expressed in this table as the ratio of the tensile splitting strength in the direction of the major principal stress to the splitting strength in the direction of the minor principal stress,  $t_{11}/t_{1j}$ . This strength ratio is, in effect, a measure of the amount of stress-induced anisotropy.

Because the failure states for any one triaxial test type are almost identical, it would be expected that the splitting test results within any

NEW MEXICO ENGINEERING RESEARCH INST ALBUQUERQUE F/G 13/13 REINFORCED CONCRETE BEAMS UNDER COMBINED AXIAL AND LATERAL LOAD—ETC(U) JAN 82 G E LANE F29601-76-C-0015 AD-A114 375 JAN 82 G E LANE NMERI-SSR-71 AFWL-TR-81-99 UNCLASSIFIED NL 2 or 3 40.4 1:4375 - <u>,</u>

one test type would also be similar. The results in Table 10, however, show considerable scatter. This large amount of scatter can also be seen in the splitting strengths of the control disks. The primary reason for this is the small size of the disks. Because the thickness of the disks is only 2 or 3 times the maximum aggregate size, the percentage of the cross-sectional area occupied by aggregate can vary widely. The amount of aggregate the failure surface must pass through is a controlling factor in the tensile splitting strength of the disk because the tensile strength of the aggregate particles far exceeds the tensile strength of the mortar. Examination of the failure surfaces after the disks had been split showed that in almost every disk the aggregate-mortar bonds were still intact; the failure surface did, indeed, pass through the aggregate.

Because of this variability and the small number of specimens available for testing, any relationships to be established must necessarily be general.

Table 9.

Tensile Splitting Strengths of Control Disks

DISK	STRENGTH	DISK	STRENGTH	DISK	STRENGTH
1 a	298	2a	350	3a	529
b	436	b	360	ь	468
С	412	c	513	c	534
avg.	382	avg.	408	avg.	510

Mean Strength = 433 psi

Stnd. Dev. = 80 psi (18.5% of the mean)

Table 10.

TEST TYPE	TEST NUMBER	+11/+c	†ij/†c	+11/+13
70	5A*	0.67	0.62	1.08
TC 3750	5B	0.64	0.60	1.07
	5C	0.48 0.55		0.87
Ave	rage	0.5	0.59	
66	6A	0.82	0.80, 0.96	1.03, 0.85
\$\$ 3750	6B	0.94	0.79, 0.71	1.33, 1.19
	6C	0.86	0.88, 0.69	1.26, 0.98
Ave	rage	0.8	1	1.11
	7A*	0.73	0.90, 0.68	1.08, 0.82
	7B	0.88, 0.86	0.81	1.07, 1.09
TE 3750	7C*	1.12, 0.89 0.96		0.93, 1.17
3/50	7D <b>*</b>	0.78 0.73		1.07
	7F	1.23, 0.74	0.76	0.98, 1.59
	7G	0.76 0.76		0.99
Ave	rage	0.85		1.08
<b>T</b> 0	8A*	0.52, 0.61	0.57	1.07, 0.92
TC 5000	8B	NA	NA	NA
	8E	0.89	0.91	0.97
Ave	rage	0.70	0.70	
66	9A	0.82	0.92, 1.09	0.76, 0.90
\$\$ 5000	9C	0.82	0.74, 0.58	1.43, 1.12
Average		0.83	0.83	
	10A	NA	0.58	NA
TE 5000	10B*	NA	NA	NA
	1 OC	1.17, 1.02	0.81	1.25, 1.44
Ave	rage	0.90	)	1.35

<sup>\*</sup> Specimens from Batch 3

Examining the average values of  $t/t_c$  listed in Table 10 without differentiating between  $t_{i,j}$  and  $t_{i,j}$ , it appears that for a given test type, the residual tensile strength increases (and conversely, the amount of degradation decreases) as the hydrostatic stress level reached prior to deviating in the octahedral plane increases. One possible explanation for this is that the octahedral shear stress at failure, when normalized with respect to the octahedral normal stress, is lower for tests in the 5000 psi octahedral plane than in the 3750 psi octahedral plane. Table 11 lists the average splitting strength results for each triaxial test performed along with the ratio of  $\tau_{\mbox{\scriptsize oct}}$  to  $\sigma_{\mbox{\scriptsize oct}}$  at failure. By plotting the average residual rensile strength  $t/t_c$  as a function of the ratio  $\tau_{oct}/\sigma_{oct}$ , as shown in Figure 18, a fairly good correlation is established which shows a regular decrease in the residual tensile strength (and conversely an increase in the amount of degradation) with increasing relative shear stress. The open circles in this figure represent test results from Batch 2 and 4 specimens and the solid circles indicate the results from tests performed on Batch 3 specimens. The linear relation indicated in the figure, which was found by a linear regression analysis of the data points pertaining to Batches 2 and 4, is meant only to show that a decreasing trend exists. The actual functional relation would most likely not be linear because the residual tensile strength cannot exceed 1.0 (t =  $t_c$ ). Scematically the relation might be as shown in Figure 19 with the function asymptotically approaching  $t/t_c = 1.0$ . Further triaxial testing in higher octahedral planes would be needed to determine the actual relation.

Table 11.

TEST TYPE	TEST NUMBER	Toct Toct	†/†c	† <sub>11</sub> /† <sub>c</sub>	† <sub>ij</sub> /† <sub>c</sub>	+11/+13
TC	5A*	0.98	0.65	0.67	0.62	1.08
3750	5B	1.06	0.62	0.64	0.60	1.07
	5C	1.04	0.52	0.48	0.55	0.87
cc	6A	0.75	0.86	0.82	0.88	0.94
SS 37 50	6B	0.79	0.81	0.94	0.75	1.26
	6C	0.78	0.81	0.86	0.79	1.12
	7A*	0.64	0.77	0.73	0.79	0.95
	7B	0.64	0.85	0.87	0.81	1.08
TE	7C*	0.58	0.99	1.01	0.96	1.05
37 50	7D <b>*</b>	0.53	0.76	0.78	0.73	1.07
	7 <b>F</b>	0.68	0.91	0.99	0.76	1.29
	7 <b>G</b>	0.68	0.76	0.76	0.76	0.99
	8A*	0.88	0.57	0.57	0.57	1.00
TC 5000	8B	0.98	NA	NA	NA	NA
	8E	0.98	0.90	0.89	0.91	0.97
	9A	0.73	0.94	0.82	1.01	0.83
SS 5000	9C	0.75	0.71	0.82	0.66	1.28
	10A	0.61	NA	NA	0.58	NA
TE 5000	10B*	0.64	NA	NA	NA	NA
•	1 OC	0.66	1.00	1.10	0.81	1.35

<sup>\*</sup> Specimens from Batch 3.

It is interesting to note that the data points corresponding to Batch 3 specimens generally fall below those of Batch 2 and 4 specimens. The splitting strengths of the Batch 3 disks were normalized with respect to the average splitting strengths of the control disks, all of which were cored from Batch 2 and 4 specimens. Therefore, this data would also suggest that Batch 3 had less strength than Batches 2 and 4.

Figures 20a and 20b show the individual relations  $t_{ij}$  vs.  $\tau_{oct}/\sigma_{oct}$ and  $t_{ij}$  vs.  $\tau_{oct}/\sigma_{oct}$  The slightly different slopes of the trend lines suggest that the residual tensile strength in one direction is affected more than in the other, which is equivalent to saying that stress-induced anisotropy does exist and may vary with the relative amount of shearing produced by the previous load history. The amount of stress-induced anisotropy (expressed as the ratio  $t_{ij}/t_{ij}$ ) is plotted against  $\tau_{oct}/\sigma_{oct}$  in Figure 21. The low value of the correlation coefficient suggests that either no correlation exists between stress-induced anisotropy and previous shear stress history or that there is insufficient data available to clearly establish a trend. If the indicated trend does have some significance, however slight, it appears, quite surprisingly, that the amount of stress-induced anisotropy actually decreases as the amount of previous shearing increases. This phenomenon can be better explained by examining the variation in the tensile strength ratio between the different test types.

Figure 22 shows the individual test results and averages of  $t_{ij}/t_{ij}$  for the different test types. There is a regular progression in the amount of anisotropy from the triaxial compression test through the simple shear to the triaxial extension test. It is possible to explain these changes from one test type to another in terms of the mechanics involved in each

test. In the triaxial compression test, one of the specimen axes is loaded and the other two are relieved once the octahedral plane is reached. Thus, energy is being applied in one direction and dissipated in two directions as the specimen expands against the decreasing forces. Equate this with the specimen having two "degrees of freedom". In the triaxial extension test, two axes are loaded and only one is relieved. Let this represent one "degree of freedom". It would be suspected that a greater amount of expansion would have to occur on the one unloaded axis of a triaxial extension test than would be necessary on each of the two unloaded axes of a triaxial compression test. This is, of course, obvious from the rates of expansion shown by the stress-strain curves of the different tests. As the specimen expands, cracks propagate within planes which are perpendicular to the direction of expansion. The greater the amount of expansion, the more the cracks propagate, and the more these cracks propagate, the less intact material remains to support a tensile stress. Thus, the greater amount of crack propagation associated with lower "degrees of freedom" can be equated with lower tensile strengths in the direction of the unloaded axes. The result of this would be that the amount of anisotropy exhibited by specimens subjected to triaxial extension loading would exceed that exhibited by specimens subjected to triaxial compression histories. Because the simple shear test includes one axis which is neither loaded nor unloaded, the amount of anisotropy should be halfway between those of the other two tests. These are exactly the results shown in Figure 22. Thus It would appear that the energy distribution (force x displacement) rather than just the force distribution may be what produces stress-induced anisotropy.

The tensile splitting test results from specimens tested biaxially are given in Table 12. With such a small number of data points, the results could not be analyzed using regression analysis. Instead, bar charts are shown in Figures 23 and 24 which indicate the average results of each test type. For the 1:3 stress ratio tests, the Batch 3 results are included and indicated by an asterisk. Their average is shown by the dashed horizontal line while the solid horizontal line shows the average from Batch 2 and 4 specimens.

In Figure 23 there is no apparent trend relating residual strength to stress ratio. It does appear, however, that the residual strength of the biaxially-loaded specimens is consistently above 90 percent of the control disk strengths, a level achieved by only three of the triaxially-loaded specimens. This greater residual strength may relate to the lower stress levels achieved in biaxial testing.

Figure 24 also shows no apparent trends. It is interesting to note, however, that the tensile strength ratio of the one uniaxial test indicates that more damage was done in the direction of the major principal stress than was done in the minor principal stress direction. This test has the highest degree of freedom, as defined before, of the biaxial tests and, in fact, the uniaxial test represents exactly two degrees of freedom, as did the triaxial compression test. The tensile strength ratio of the TC test also indicated that slightly more damage had been done in the major principal stress direction. The remaining biaxial stress ratios show tensile strength ratios above unity (if the one very low value is discarded) but there is no regular increase in the tensile strength ratio from test to test.

Table 12

TEST NUMBER	STRESS RATIO	† <sub>11</sub> /†c	† <sub>1</sub> j/†c	+11/+13
1 A	0:3	0.90, 0.79	1.06	0.85, 0.75
2A*		0.79	0.87	0.91
28		1.03	0.88, 1.09	1.17, 0.94
2C	1:3	1.23, 0.76	0.82	1.50, 0.93
20*		0.95	1.17, 0.77	0.81, 1.23
3A		1.26	1.23	1.02
38	2:3	0.65	0.64	1.02
3C		0.68	1.32	0.52
4E		1.35	1.27	1.06

<sup>\*</sup> Specimens from Batch 3.

### CONCLUSION

It is felt that sufficient reproducibility of triaxial stress-strainstrength behavior has been achieved to allow material characterization
based on the results of these tests. Unfortunately the biaxial test series
did not include enough successful tests that as high of a level of
confidence can be had in its results. Comparisons between the results of
this test program and those of the previous program may be made, however
the differences in concrete strengths and the slightly different failure
criterion must be kept in mind.

The results of the tensile splitting test series have shown that load histories do affect the residual tensile strength of a specimen and the amount of stress-induced anisotropy, indicating future research along these lines is warranted. Specifically, research utilizing a greater number of specimens is needed to more completely investigate the trends suggested here. The effects of the "degrees of freedom" of a test on the relative amount of stress-induced anisotropy can be better studied using more triaxial stress paths to fill in the gaps between those paths used in this program. Further biaxial testing with more stress ratios would also be helpful since the concept of energy distribution based on "degrees of freedom" also extends to biaxial tests. Similarly, additional triaxial testing at higher octahedral stress values would more clearly establish the relationship between the amount of octahedral shear stress relative to the level of octahedral normal stress and the amount of residual tensile strength. Triaxial testing at lower octahedral normal stress levels would

also aid in this investigation, however failure states cannot yet be achieved in lower octahedral planes because the failure envelope extends beyond the compression-compression octant of stress space. A multiaxial testing cell with tension capabilities is being developed at the present time which could aid in such a study.

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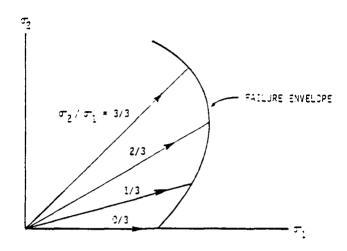


Figure 1. Biaxial Stress Paths

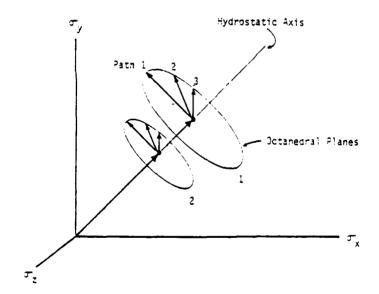


Figure 2. Triaxial Stress Paths in two octanedral planes.

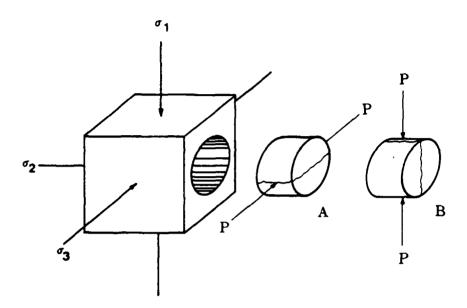


Figure 3. Orientation of tensile splitting test disks cored from cubical cell specimens. Disk A - Tensile splitting in the direction of previously applied major principal stress. Disk B - Tensile splitting in the direction of previously applied minor principal stress.

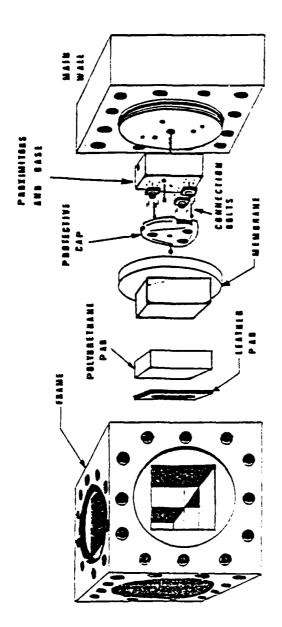


Figure 4. Exploded view of the cubical cell frame and one wall.

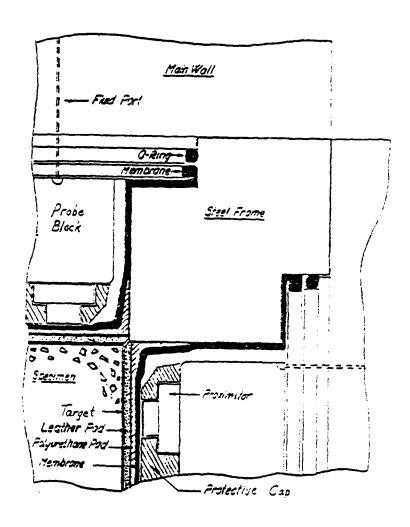


Figure 5. Section through one corner of the assembled cubical cell.

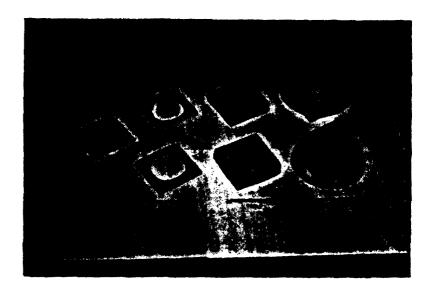


Figure 6. Photograph of (in order of insertion into pressure vessel) brass probe target (far left), protective leather pad, protective polyurethane pad, and fluid cushion membrane. (Bottom half of photo shows components as viewed from within the cubical cell, upper half shows components as viewed from the inside face of the walls)

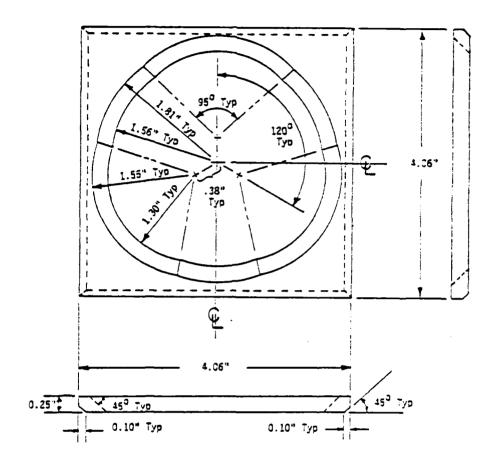


Figure 7. Specifications for the leather pads showing beveled center hole and beveled eages.

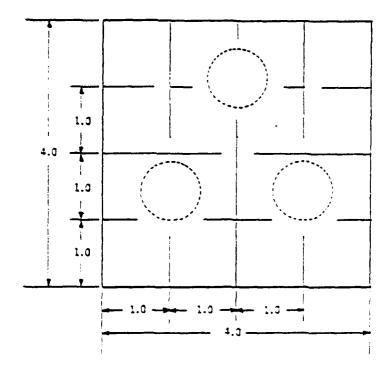


Figure 8. Pattern of slits cut in probe targets to allow flexibility.

(Dashed circles show the areas at which the proximitor probes aim.)

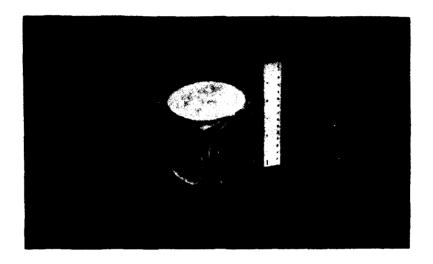


Figure 9. Cubical cell concrete specimen ready for testing.

(Note circular patches on each face)

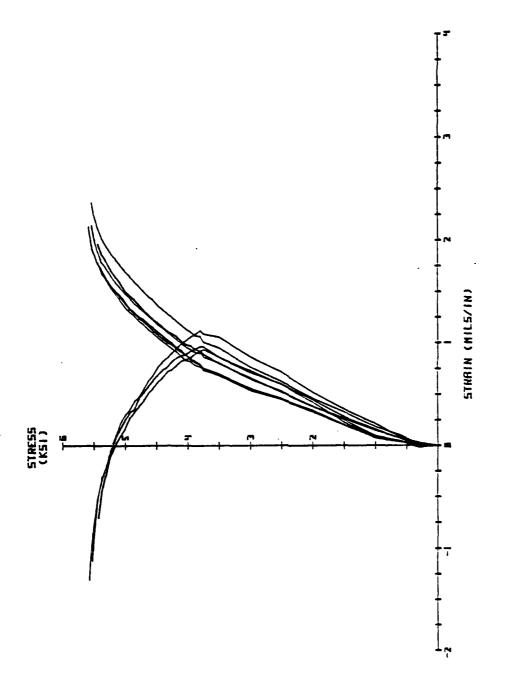


Figure 10. Stress-strain curves from all three triaxial extension tests on specimens from Batch 3.

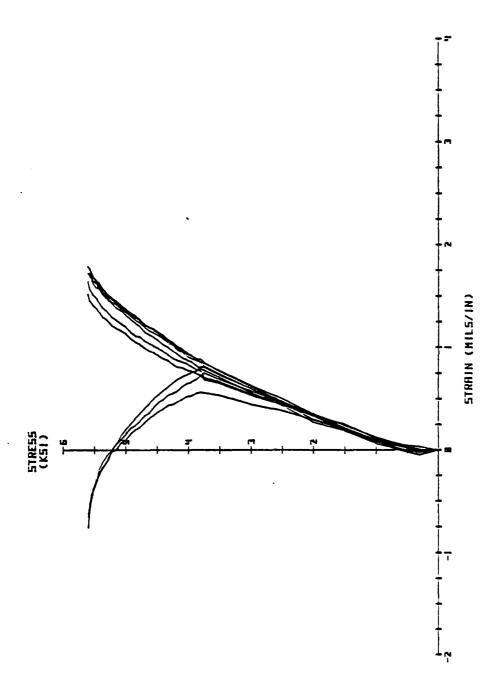


Figure 11. Stress-strain curves from all three triaxial extension tests on specimens from Buiches 2 and 4.

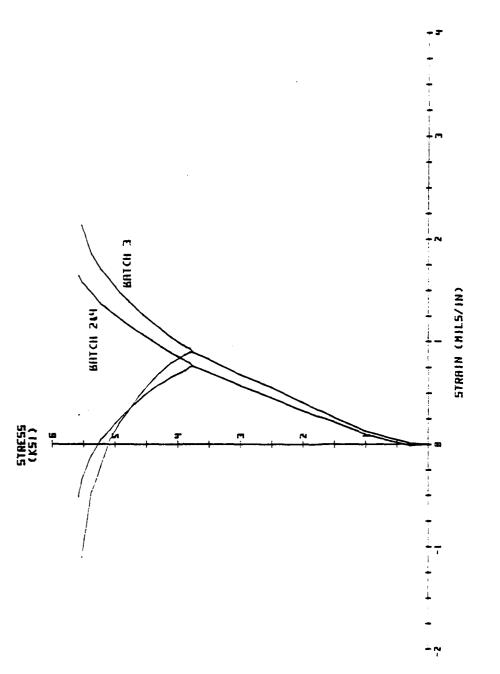


Figure 12. Average behavior in triaxial extension of specimens from Batch 3 and specimens from Batches 2 and 4.

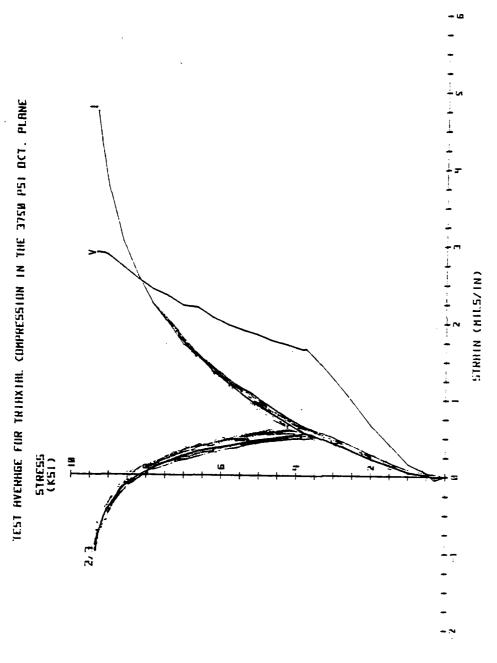
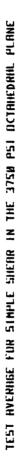


Figure 13a. 10 3750



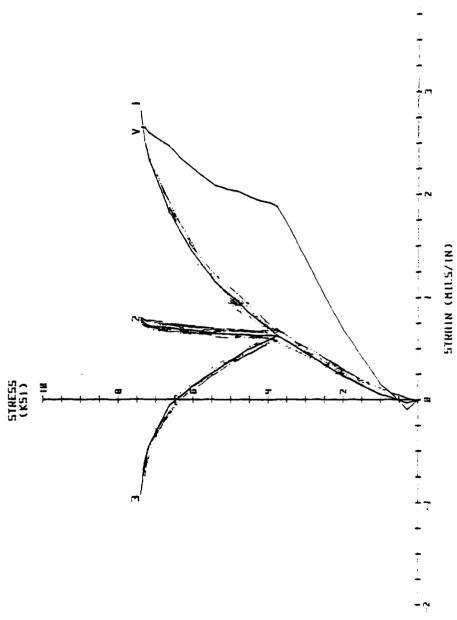


Figure 13b. 55 3750



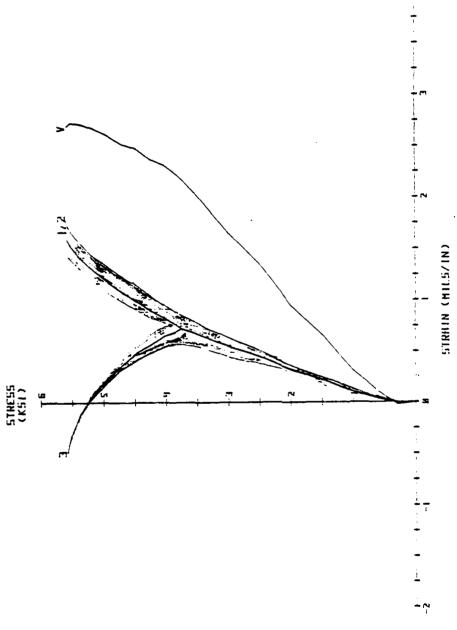


Figure 13c. 1f 3750

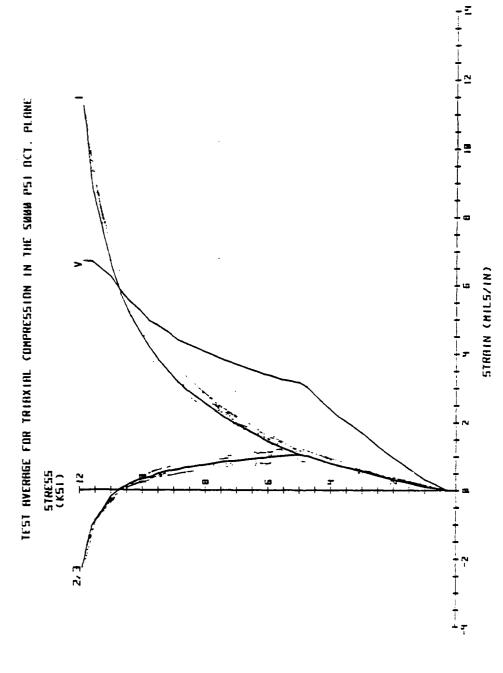


Figure 13d. IC 5000

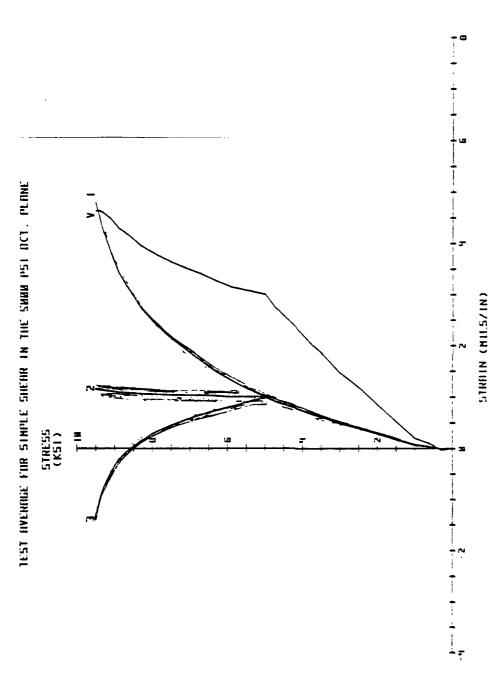


Figure 13e. 55 5000

TEST HVERREE FOR TRIBXIAL EXTENSION IN THE SUBUR PSI DCT. PLANE

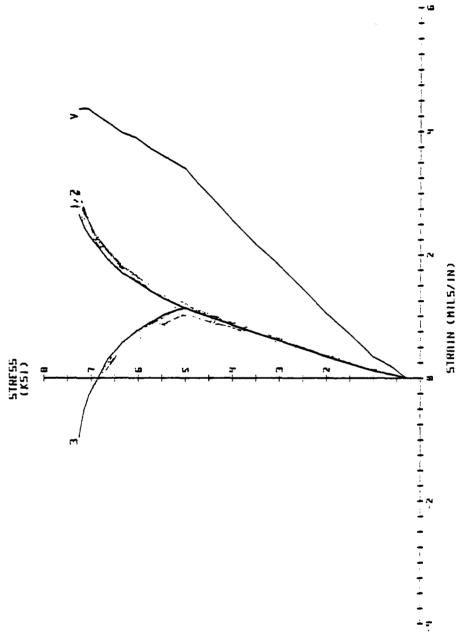


Figure 13f. 1t 5000

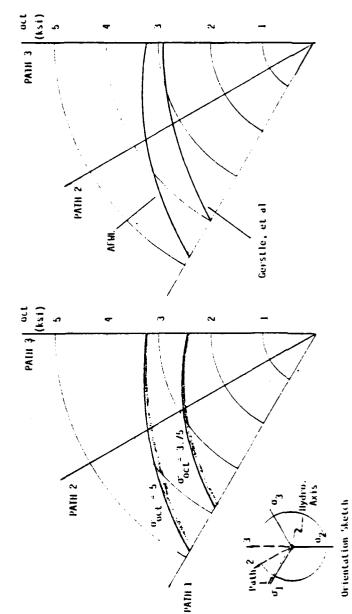


Figure 14a. Failure envelopes in the  $\sigma_{\rm oct}$  = 5 ksi  $\,$  Figurand out = 3.75 ksi octahedral planes.

Figure 14b. Tailure envelopes from this study and fluid cushion testing by Gerstle, et al.

in the  $\sigma_{oct} = 5$  ksi octahedral plane.

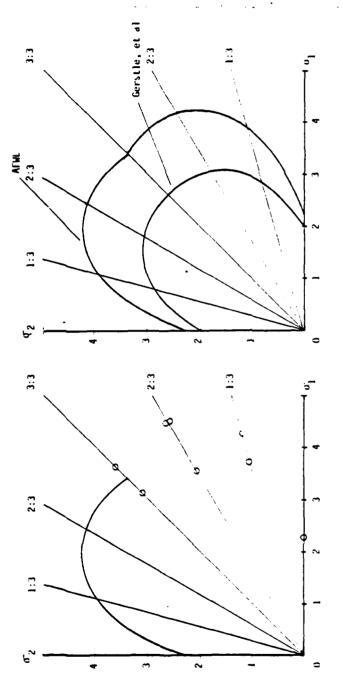


Figure 15b. Biaxial strength results from this study and fluid cushion testing by Gerstle, et al.

Figure 15a. Biaxial compressive strength results

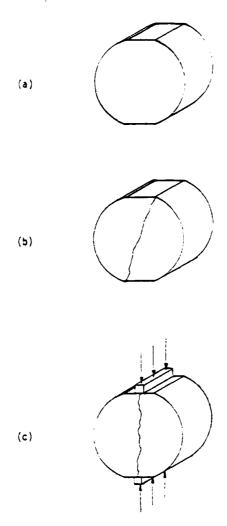


Figure 16. (a) Modification of tensile splitting test disk specimen; (b) Compressive failure mode of modified disk: (c) Use of steel bars to ensure a line load in the plane of splitting.

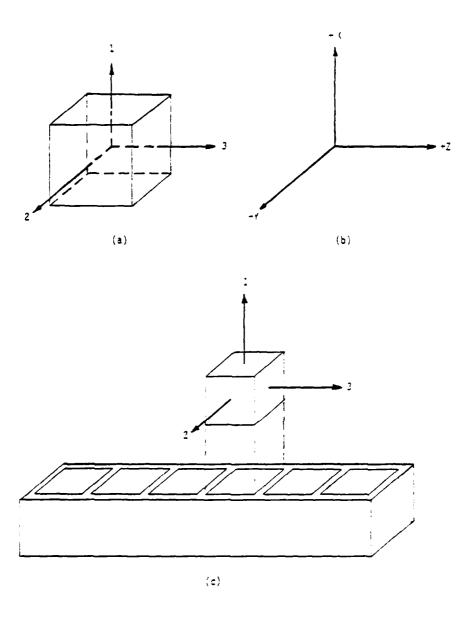


Figure 17. (a) The 1,2 and 3 coordinate axes used to describe physical space and (b) the x,y and z axes of lartesian coordinates; (c) specimen axes chosen to relate to the axes of the concrete molds.

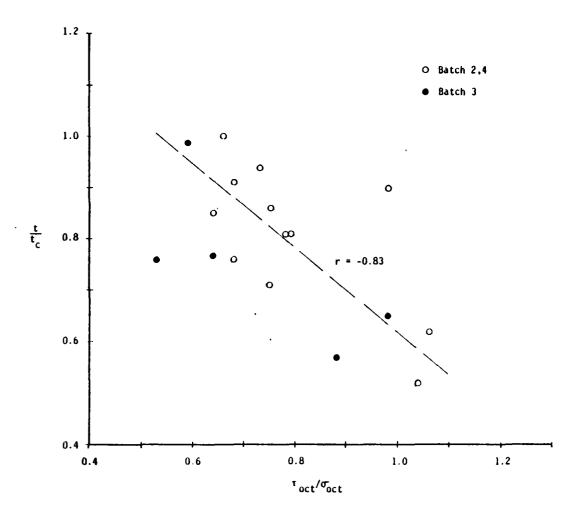


Figure 18. Residual tensile strength as a function of the normalized shear stress at failure.

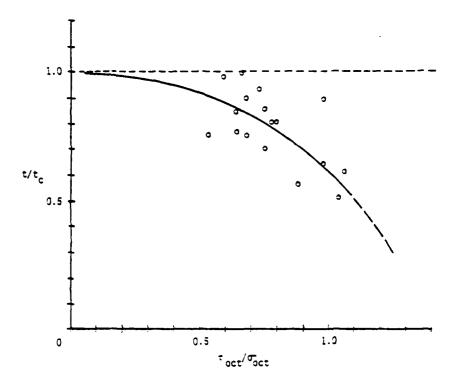


Figure 19. A possible relationship between residual tensile strength and the normalized octahedral shear stress at failure.

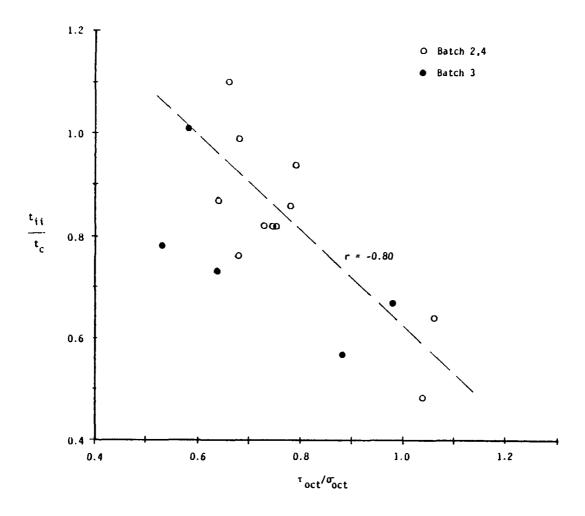


Figure 20a. Residual tensile strength in the direction of the previously applied major principal stress as a function of the normalized octahedral shear stress at failure.

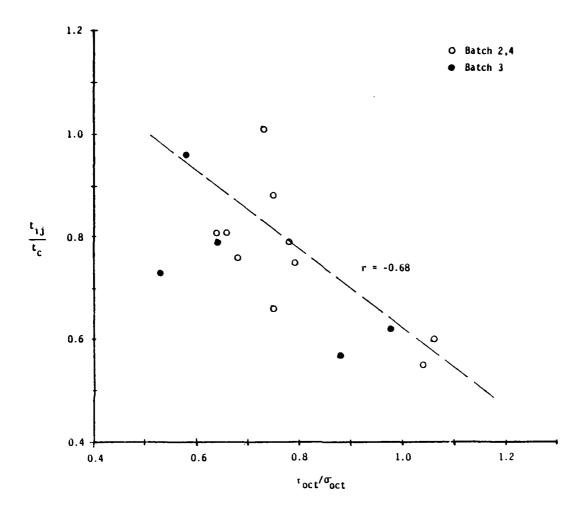


Figure 20b. Residual tensile strength in the direction of the previously applied minor unincipal stress as a function of the normalized octahedral shear stress at failure.

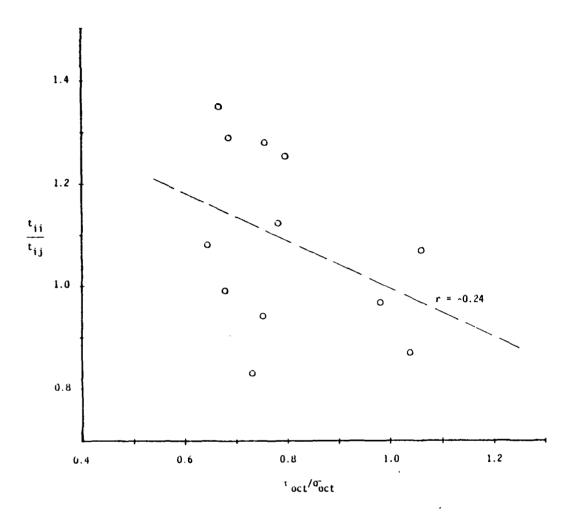
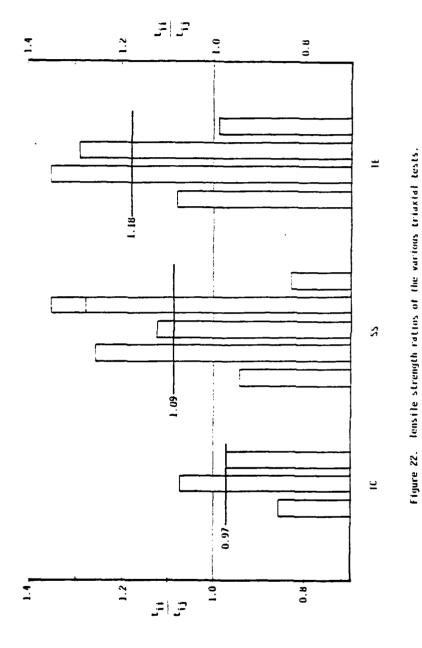


Figure 21. Tensile strength ratio as a function of the normalized octahedral shear stress at failure.



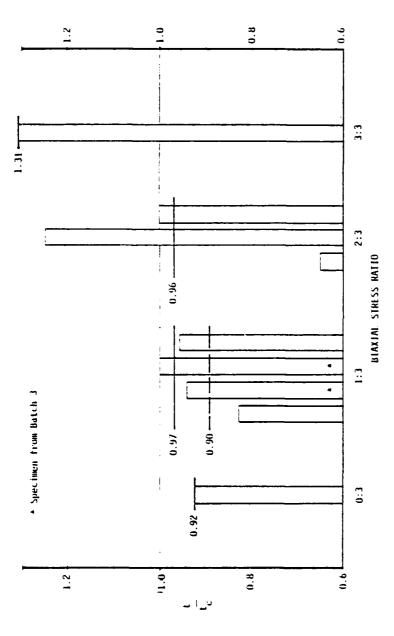


Figure 23. Residual Lensile strengths of the various biaxial tests.

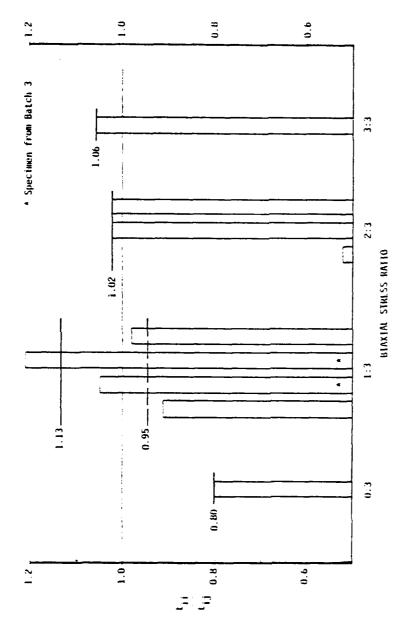


Figure 24. Tensile strength ratios of the various biaxial tests.

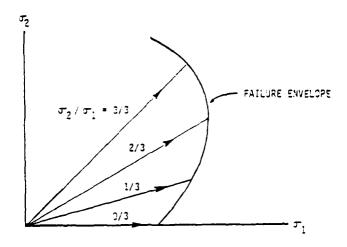


Figure 1. Biaxial Stress Paths

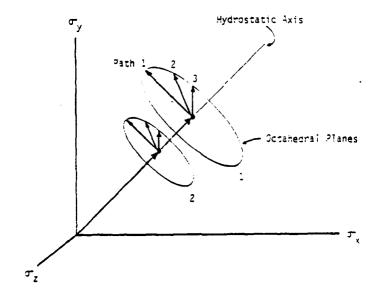


Figure 2. Triaxial Stress Paths in two octanedral planes.

#### APPENDIX A.

#### STRESS-STRAIN DATA FOR TRIAXIAL TESTS

This appendix contains the stress-strain data for each successful triaxial test. The data sheets are arranged in order of test number beginning with Test 5A. The axes which head the columns are the axes of the cubical cell. Stresses are given in psi and strains are given in mils/in. 1 mil/in = 0.1% strain =  $10^{-3}$  in/in.

### STRESS - STRAIN DATA

STRESS STRAIN STRESS STRAIN ST (PSI) (MILS/IN) (PSI) (MILS/IN) (P)	RESS STRAIN Blo (MILS/IN)
500         3.0531         600         0.0558           1000         0.1330         1           1500         0.2527         1           2000         0.2527         1           2000         0.3468         2           2500         0.4448         2500         0.4803           3500         0.5713         3000         0.7620           3750         0.7338         3750         0.8196           3750         0.7290         3700         0.8330           3700         0.7290         3700         0.8330           3700         0.7290         3700         0.8330           3700         0.7290         3700         0.8330           3700         0.7290         3700         0.8330           3700         0.7291         3500         0.7851           3400         0.7655         3500         0.7851           3400         0.7620         3.7188         5           3200         0.6551         3200         0.7980         5           3200         0.6572         3200         0.6530         5           2200         0.5938         5         5           <	0.0000           0.

## TENSILE STRENGTHS

IN THE DIRECTION OF THE MANIMUM PRINCIPAL STRESS = 290 PSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 260 PSI

# STRESS - STRAIN DATA

X-AMIS		Y-AXIS		Z-AXIS	
STRESS (PSI)	STRAIN (MILS/IN)	STRESS .FSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
99999999999999999999999999999999999999	09775734784899761031816342401748040385343 09778119712853124698148179895299927724 0907811234659814835218405171608814693 09077771753108655219855218405171608814693 090999855555544448332211988823453 09099988888888888888888888888888888888	99999999999999999999999999999999999999	999375899333444313588255544422229892753789948927552893333444313588255444222298927537899489275328994481123895554164355318951439892753789948999999999999999999999999999999999	99999999999999999999999999999999999999	0866913333867696398989886781194398139331654788889339444177139887288893347257774886757225408888934725777488675722541512088888888878541214111111111111111111111111111111111

7387 58 ... TO STED 9980108N 020 8870H 2 12025 90

#### (CONTINUED)

X-AXIS		Υ	Y-AXIS		Z-AXIS	
STRESS	STRAIN	STRESS	STRAIN	STRESS	STRAIN	
(PSI)	(MILS/IN)	(PSI)	(MILS/IN)	(PSI)	(MILS/IN)	
900	-0.9343	900	-1.1035	9450	4.9961	
850	-1.2160	850	-1.3669	9550	5.4689	
800	-1.6508	800	-1.7982	9650	6.1700	

### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAXIMUM PRINCIPAL STRESS  $\approx$  278 PSI IN THE BIRECTION OF THE MINIMUM PRINCIPAL STRESS  $\approx$  260 PSI

# STRESS - STRAIN DATA

X-AMIS		Y-AXIS		Z-AXIS	
STRESS PSI/	STRAIN KALSAINA	STRESS .291)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
99999999999999999999999999999999999999	07001833366300313855925979071141500675444350070070018333663003138592597907114150067544435000033396530035592597907114150067544435000000000000000000000000000000000	99999999999999999999999999999999999999	0.000000000000000000000000000000000000	39999999999999999999999999999999999999	0.00355322633199035387005531803322979 0.0036427661332263319903543543543631723479 0.0035561235433990749799 0.003556123543990749799 0.00365563631723435430337445 0.003666513322633114632334363331445 0.0036665133226331445 0.0036665133226331445 0.00366651332263331445 0.00366651332263331445 0.00366651332263331445 0.00366651332263331445 0.00366651332263331445 0.00366651332263331445 0.00366651332263331445 0.00366651332263331445 0.003666513322633314635 0.00366651332263331463314633146331463314633146331

TEST FO ... TO STED SPECIMEN A4, SATCH 4 1 05.51

#### (CONTINUED)

. W-ANIS		Y-AXIS		Z-AXIS	
STRESS (PSI)	STRAIN (MILS/IM)	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
900	-1,3653	900	-1.4788	9450	5.5258

#### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAXIMUM PRINCIPAL STRESS = 208 PSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 240 PSI

grande vietnas jakoris ir

### STRESS - STRAIN DATA

X	-AXIS	Y 	-AKIS		-AXIS
STRESS (PSI)	STRAIN (MILS/IN)	STRESS .PSI)	STRAIN KMILSZIN)	STRESS (PSI)	STRAIN (MILS/IN)
99999999999999999999999999999999999999	044335699100959865194456550096770381732038094335699100958628674356509626821732038099626977899568557943568079962682173203809999999999999999999999999999999999	99999999999999999999999999999999999999	06664729535541420990036403248664479124340445644529555541206388364038549555209445588832178538209938598018555520000112345554444333221113845352357901	39999999999999999999999999999999999999	0.04       6.09         0.05       5.09         0.05       5.09         0.09       6.09         0.09

# TENSILE STRENGTHS

IN THE DIRECTION OF THE MAMIMUM PRINCIPAL STRESS = 408 FSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 325 PSI

\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	-AKIS	7	-AXIS	Z	-AXIS
STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
\$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$	97367917727489327226234287777125848592318 98172113687211222244431444367428684682333357 981721123687777774489327 98123456777777777777777777777788888888883333356 98123456777777777777777777777788888888333333688888888	99999999999999999999999999999999999999	0311106966886988463878268767618468472532 04159959168861126044537384956946380739739 0600123456986112604133649569478067633597396 060012345686112604133649569478033597396 06001234569861337384956947800335996 060012345698698888876767899999999999999999999999	99999999999999999999999999999999999999	08408520586587750111580083446861794195800967800967800967800967800967800967800967800967800967800967800967800967800967800967800900909090909090909090909090909090909

TEST SC ... 95 0750 SPECIMEN D2+ BATCH 3 1-28 51

#### · CONTINUED)

X	-AXIS	Y-AXIS			Z-AXIS	
STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)	
3750	a.8792	50	-0.9354	7450	2.7949	

#### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAXIMUM PRINCIPAL STRESS = 373 PSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 340 PSI

R	-ANIS	Υ	-AXIS	2	-AKIS
STRESS (PSI)	STRSIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
99999999999959595959595959595959595959	0       0	99999999995959595959595959595959595959	9       5       1       2       3	00000000000000000000000000000000000000	000-00071744741502534010476050019053001 000623146516933212790231697424163342 000623146516933212790231697424163342 00062314650000077-752614823569193535 000000000077-752614823569193535 00000000000077-752614823569193535 0000000000000000000000000000000000

### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAKIMUM PRINCIPAL STRESS = 318 FS1 IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 295 PS1

33	-AMIS	9	-A%[8	2-	-ANI3
37 <b>95</b> 88 ( <b>331</b> )	STRAIN (MILS:IN)	STRESS JESIJ	STRAIH (MILS/IN)	STRESS (PSI)	STRAIN MILSZIN)
99999999999999999999999999999999999999	97795434598839692661839643815243682956295434598839692661839643815243682 96779543459883969266183994599 985298326394595716898224599 981223555524444437312221198991122455 9899911224557	99999999999595959595959595959595959595	04       05 <td< td=""><td>00000000000000000000000000000000000000</td><td>0.003753858963717772871948211931896963985844779718772871944821197188193189696.77815441689999646523661115931289696969696969911111111111111111111111</td></td<>	00000000000000000000000000000000000000	0.003753858963717772871948211931896963985844779718772871944821197188193189696.77815441689999646523661115931289696969696969911111111111111111111111

#### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAKIMUM PRINCIPAL STRESS = 374 PSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 350 PSI

13	-ALIS	í,	-AXIS	2	-AXIS
37R <b>E</b> S3	STRAIN	STRESS		STRESS	STRAIN
(2 <b>51</b> )	CHILS/IN/	(PSI)		(PSI)	(MILS/IN)
00000000000000000000000000000000000000	97.8119245948037889357749954888293859568324594872375359548882 93856835159125537545454545237934 93856889996937547249434955834 938688999699111123334455567792	00000000000000000000000000000000000000	04898368244848937470513874012992720010836982413468532257582172323251632555502172323163255550217233231632555502172332316325555000000000000000000000000000000000	00000000000000000000000000000000000000	0.00533490365309657548593935073844790063534903630965775485939350738444790063523449920254409351662874392549513096565754859393507384479
3500	3.0392	5500	2.2652	250	-0.8556
5525	2.1448	5525	2.3650	200	-1.1154

#### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAKIMUM PRINCIPAL STRESS = 437 FSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 415 FSI

	H-A1115		-AKIS	Ξ	-A'13
378 <b>5</b> 33 (881)	STRAIN (MILS/IN/	378 <b>5</b> 55 (881)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS IN)
\$	0779369215749118880730411913667330440109779369215749118880730411191366725304401097793692553041576887844545869258370446555007900023467889258001111112222333445555577	99999999999595959595959595959595959595	98525387289316951974989558643967886 91491997289316951974985558643967886 91234694855752492985558647198772493 91234694855724492364714927872493 91233449278492491111111111111111111111111111111111	02222222222222222222222222222222222222	00010000000000000000000000000000000000

#### TENSILE STRENGTHS

IN THE DIPECTION OF THE MAXIMUM PRINCIPAL STRESS = 432 PSI IN THE DIPECTION OF THE MINIMUM PRINCIPAL STRESS = 123 PSI

 	-A1113	. 7	-AXIS	2	-AX13
STRESS (FSI)	STRAIN KMILS/IN/	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
\$	######################################	\$	0484291947243568146697580593866968066500234254104724356805245127334307806696806650023842541045023580524512733443078066500610023897361893680360036000360003715803592663592	99989999999999999999999999999999999999	9554436935147629716329114495316155123396691 98178123166627762773563523551837545668334 9999276528641753961633235959596377368324 999923456662776273564443332359595377368324 999999999999999999999999999999999999

# TENSILE STRENGTHS

IN THE DIRECTION OF THE MANIMUM PRINCIPAL STRESS = 327 PSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 338 PSI

g-	-AMIS	پ 	-AXIS	Z	-AX15
97 <b>RE</b> 99 (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)	978538 (PSI)	STRAIN •MILS/IN/
39999999999999999999999999999999999999	97.839.64943.6366463312513559356939         92.5938.77537.4569319265573582449237         92.51236738173853172943557358249237         92.512367381738531729435575254719237         93.62345738111111199943575254719237         93.63396738111111111111111111111111111111111111	99999999999999999999999999999999999999	035919729794553998536259344628017739197297994049225934462462801235919729175529940492286512352866300000000000000000000000000000000000	99999999999999999999999999999999999999	037703295044333488871440353008873200399045235554886714403553088732001 02229927263740418669019316355347631 000023563740041866200415468374531 00002356391335578024601303364445636 1000236360011111111223333344456801

#### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAXIMUM PRINCIPAL STRESS = 244 PSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 245 PSI

X-A).15	γ-	-AKIS	Z	-AXIS
STRESS STRAIN SFSID (MILSVIN		STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
0.0349 0.0349 0.0349 0.03349 0.03349 0.13349 0.12349 0.12349 0.3349 0.3349 0.3349 0.4500 0.4500 0.4500 0.4500 0.4500 0.77123 0.65547 0.65547 0.65547 0.65547 0.65547 0.65552 0.65547 0.655	3350 3250 3250 3250 3250 3250 3250 3250	06664092526595321662893331684893253280931681768489352532809317682893317133647455334558931713366640931713345568933174397542995174380245831171339011234556893177766666555443924583217901133901334556893177766666555443321100036363525011334556783777766666555544332110003636352501133455678377776666655554433211000000000000000000000000000000000	99999999999999999999999999999999999999	02277700800524407455580562218875530022246524669 0032841222144745004436678001725412273912274662409 003284136017513884066780017254127395474562409 0032846017513884066780017388887667954743139 0030000011111111112322233334455681112

### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAXIMUM PRINCIPAL STRESS = 385 ASI IN THE DITECTION OF THE MINIMUM PRINCIPAL STRESS = 196 ASI

3	-ANIS	7	-AXIS	2.	-AXIS
STRESS	STRAIN	STRESS	STRAIN	STRESS	STRAIN
(PSI)	(MILS/IN)	(PSI)	(MILS/IN)	.PSI)	• MILS: IN:
99999999999999999999999999999999999999	0 6 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	99999999999999999999999999999999999999	8383838381338898918364956486981888483 83157458426683711577836899263181458 8278856777996523486295151461458369 828812345577788887777662951544332188269 8288888888888888888888888888888888	00000000000000000000000000000000000000	01004999995629824990247475236996976051243452344497522994334733999667269910051245262344975229943347339966726991000012455691100000000000000111111111111111222222233
5000	0.8734	900	-0.5012	9100	3.5545
5000	0.8858	700	-0.8623	9300	4.0249
5000	0.8969	600	-1.1123	9400	4.2744
5000	0.9059	500	-1.4951	9500	4.5641

#### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAKIMUM PRINCIPAL STRESS = 150 ASI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 484 ASI

 $\langle \mathbf{x} \rangle$ 

#### STRESS - STRAIN DATA

M-A819		Y-AXIS		Z-AXIS	
STRESS (PSI)	STRAIR (MILS/IN)	3TRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
2 999999999999999999999999999999999999	3324755976486281127778399721683985 8155517791648628112778359853391655 81559177916924935471788683391255257 816935269211189996867777667899812255257 811123466779889968677778868998121111111111111111111111111111111	2 999999999999999999999999999999999999	7 036573772030:450719662921:225234:9 033542271672354350719662921:226234083356 03265331672354350719662921:226234083356 032653316723294495831065149273962934083356 030657673346833577776665149273962934083376767	7 999999999999999999999999999999999999	7 00037822399469452923999254993315398139935949 0015378222399469452923999254993315398139935949 0015313222399469455398199933481239355949 001531322233355949 001531311111111111111111111111111111111
5000 5000	1.3725 1.4036 1.4287	400 300	-1.7023 -2.2243	9500 9700	4.8414 5.1882

#### TENSILE STRENGTHS

<sup>19</sup> THE BIRECTION OF THE MAY DOWN PRINCIPAL STRESS = 356 FBC D. THE BIRECTION OF THE MINIMUM PRINCIPAL STRESS = 284 PE.

X-AXIS		Y-AXIS		Z-AXIS	
STRESS	STRAIN	STRESS	STRAIN	STRESS	STRAIN
(PSI)	(MILS/IN)	.PSI)	(MILS/IN)	(PSI)	(MILS/IN)
00000000000000000000000000000000000000	0537.46950421673416017527076377799130 037.52012233938937493457189542355000 02625791450637347040415533365515403 0012346730637344455556573395415403 000000000000111111111111111111111111	99999999999999999999999999999999999999	0005681440594107979565059839162121764057671405941079795650598391621217640050000000000000000000000000000000000	00000000000000000000000000000000000000	0.000000000000000000000000000000000000
7250	2.7998	7250	3.0504	500	-1.1514
7350	2.9686	7350	3.3856	300	-2.1678

### TENSILE STRENGTHS

19 THE DIRECTION OF THE MAGIMUM PRINCIPAL STRESS = 0 PSI 19 THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 253 PSI

100

#### STRESS - STRAIN DATA

X-ANIS		Y-AXIS		Z-AXIS	
STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
99999999999999999999999999999999999999	0999511591828304183521916141402001372 003721159328304183521916141402001351593516935559964163516935 00.12472132830418556955996416317973 00.124721335169355216916959964163517973 00.121111111100000000000000000000000000	00000000000000000000000000000000000000	0.0057400714208599001578007142085990015780071420859900155330000433222841 00.00540071420859043333684 00.0056613777200401534000045373514 00.005661377200401534000045374502513775 00.0056000011334000000000000000000000000000000	99999999999999999999999999999999999999	0.0038465518371951837624017739519304003846551837624017739519384954349543495434954349543495434954349

### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAXIMUM PRINCIPAL STRESS = 0 FSI IN THE DIRECTION OF THE MINJMUM PRINCIPAL STRESS = 0 PSI

STRESS STRAIN STRES (PSI) (MILS/IN) (PSI	S STRAIN STRESS STRAIN (MILS/IN) (PSI) (MILS/IN)
0       0.0249       300         600       0.0249       300         600       0.0249       100         1000       0.1477       100         1000       0.2488       150         2000       0.2488       200         2000       0.4775       200         2000       0.6010       300         2000       0.7158       450         4500       0.7158       450         4500       0.7158       450         4500       0.7158       450         4500       0.7158       450         4500       0.7158       450         4500       0.7158       555         4500       1.0159       475         5000       1.1578       525         5015       525       525         5025       1.2499       575         5035       1.4695       525         50450       1.5603       525         50750       1.5603       525         50750       1.7233       525         50750       1.7233       525         50750       1.725       525         50750 <t< td=""><td>~0.0245</td></t<>	~0.0245

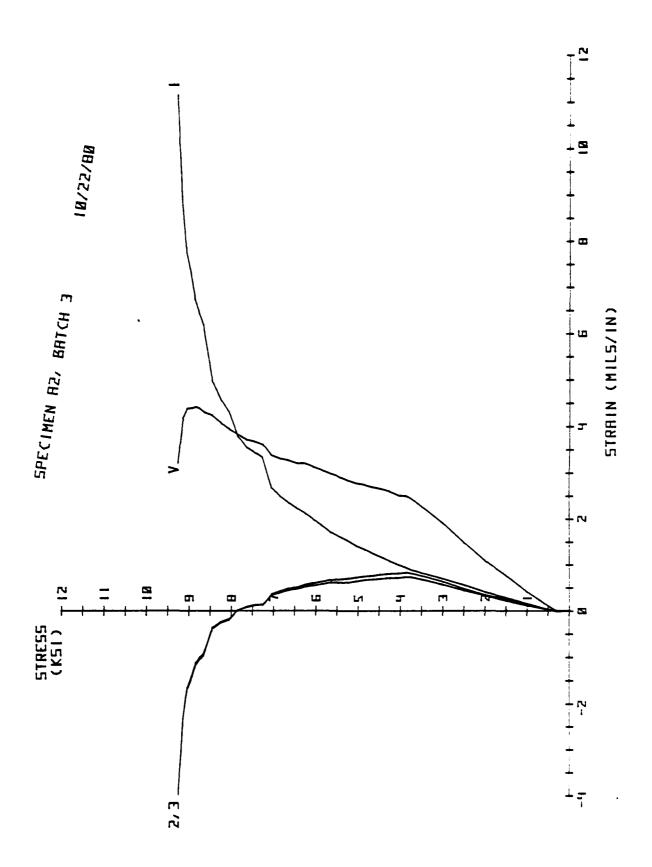
#### TENSILE STRENGTHS

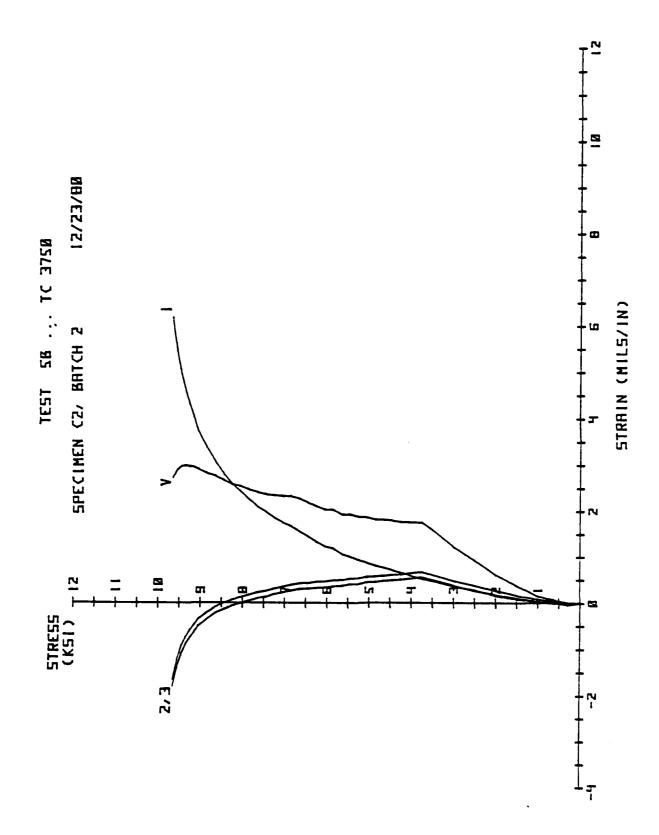
19 THE DIRECTION OF THE MEMIMUM PRINCIPAL STRESS = 473 FSC to THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 351 FSC

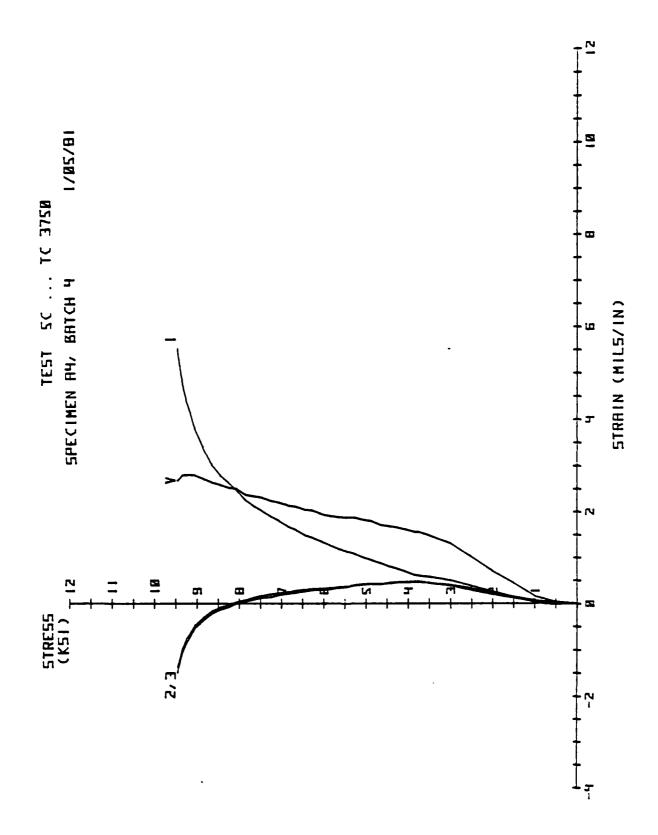
#### APPENDIX B.

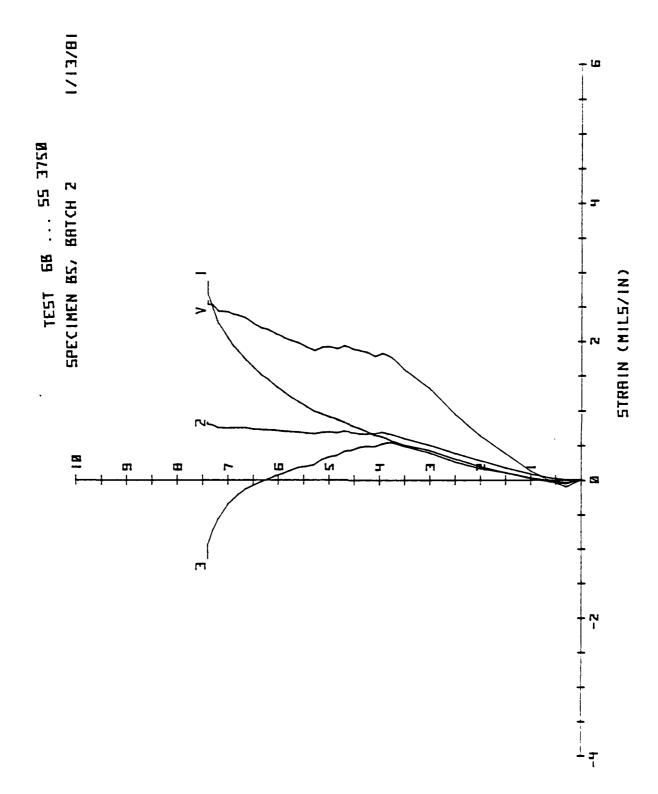
#### STRESS-STRAIN CURVES FOR TRIAXIAL TESTS

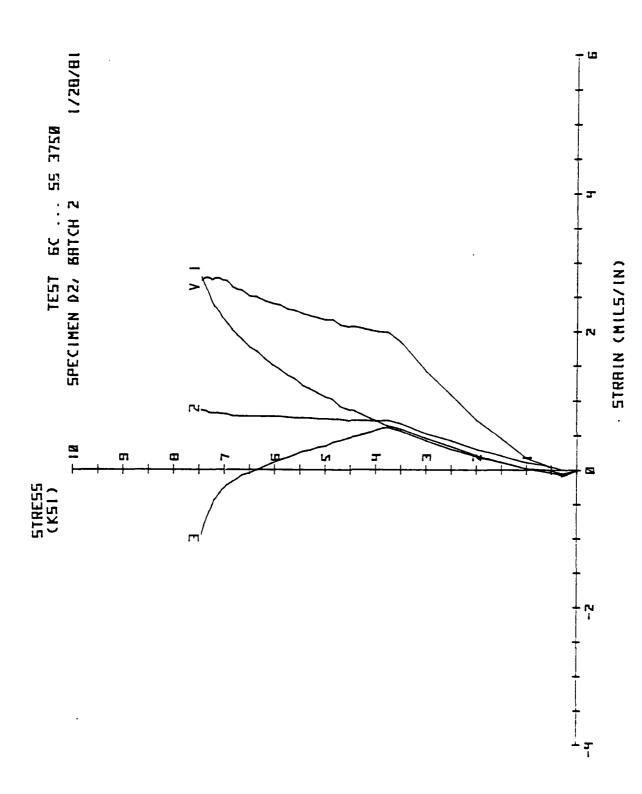
This appendix contains the stress-strain curves generated during each successful triaxial test. The ordinate values are mils/in. of strain and the values on the abscissa are the maximum principal stress in ksi. The numbers 1, 2 and 3 marked on the curves represent the principal strains and the curve marked "V" is the volumetric strain curve.

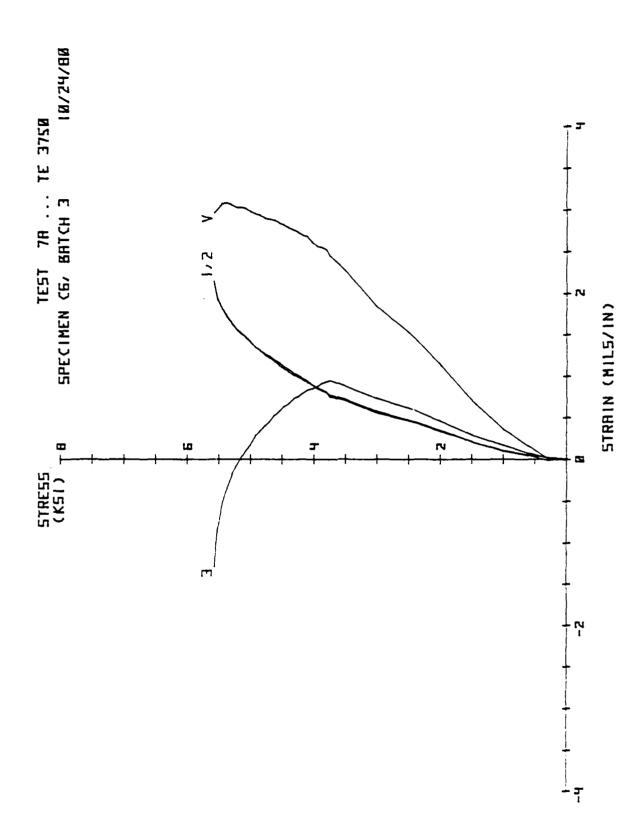


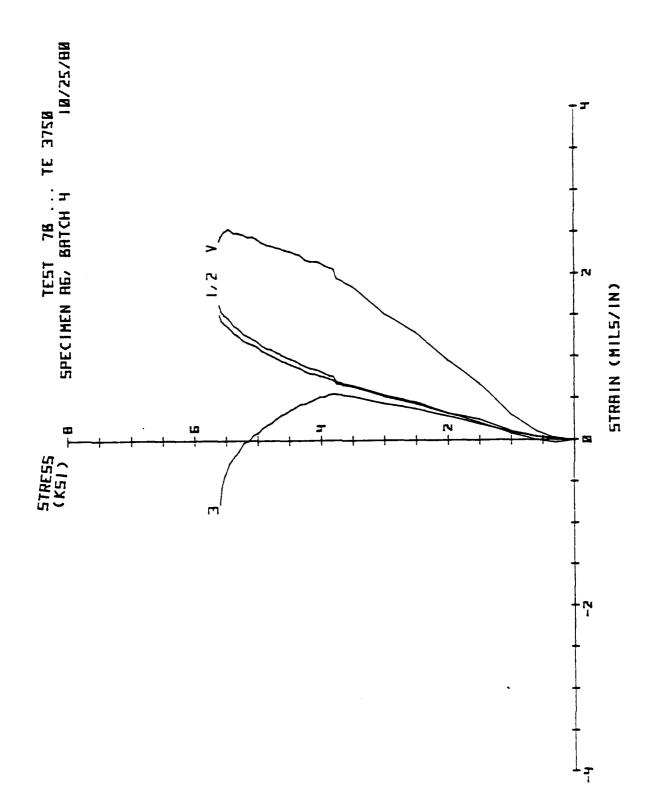


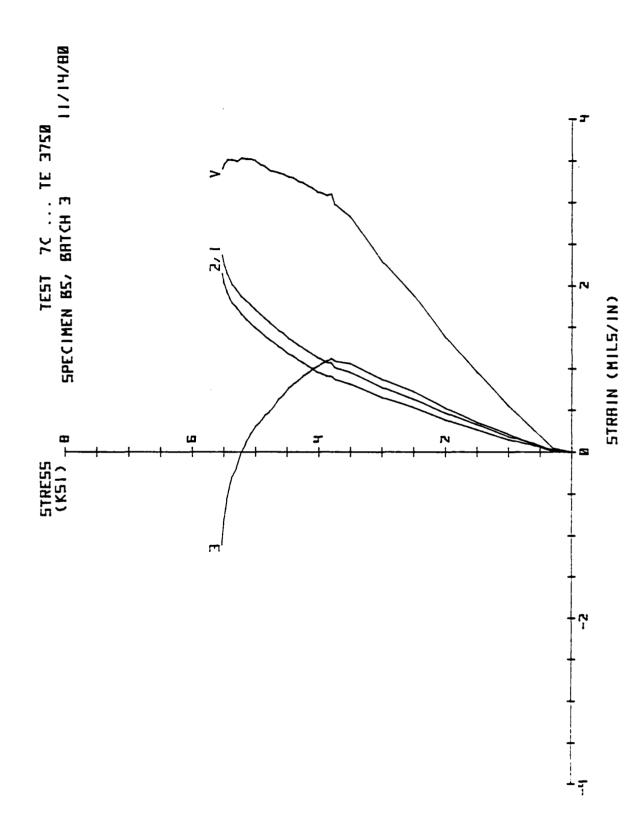


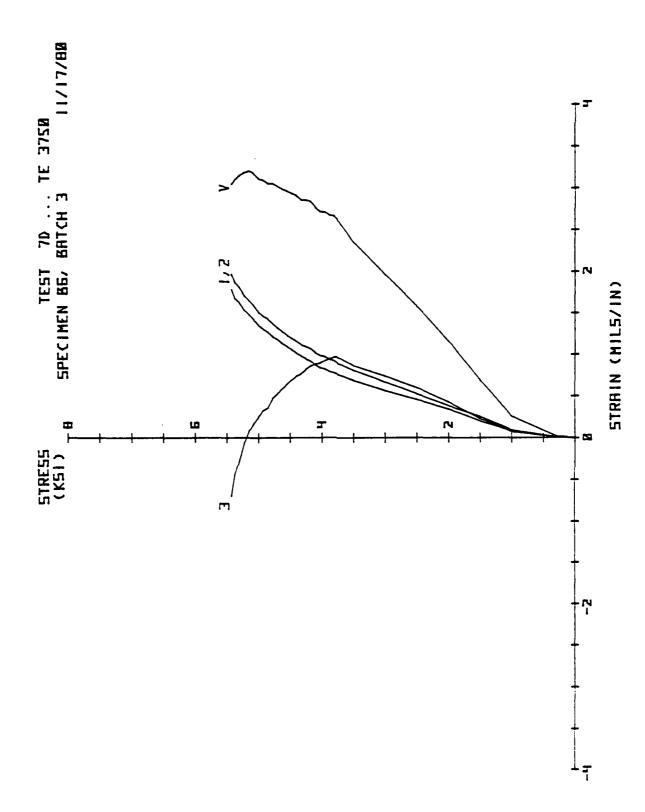


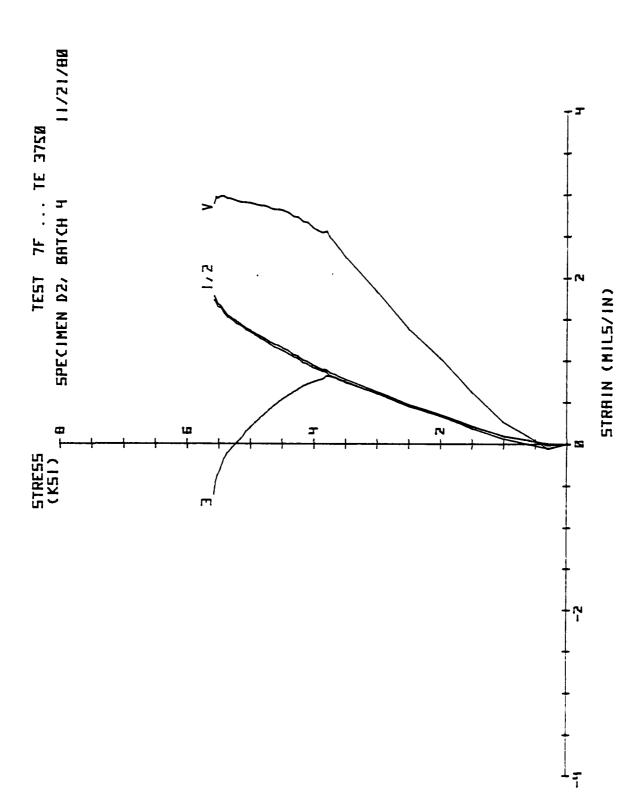


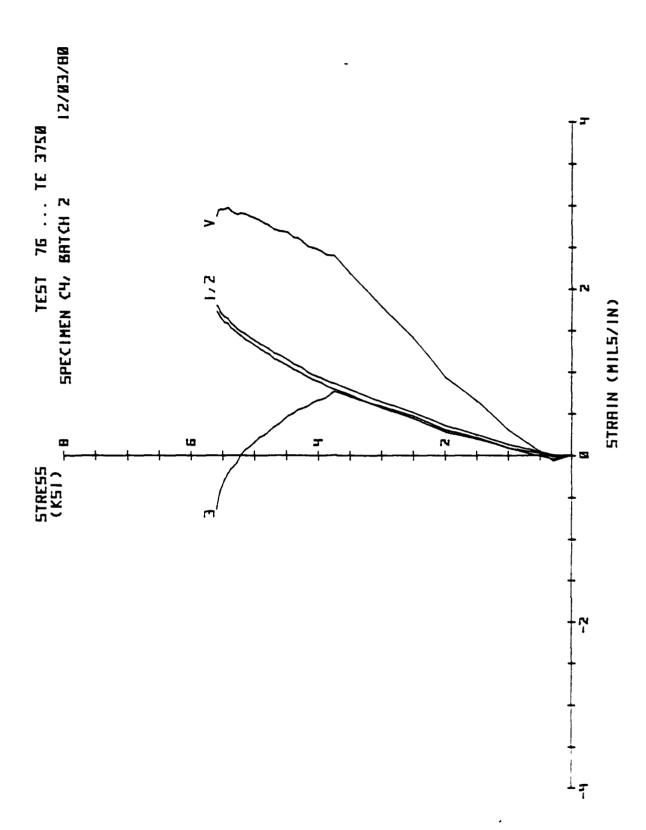


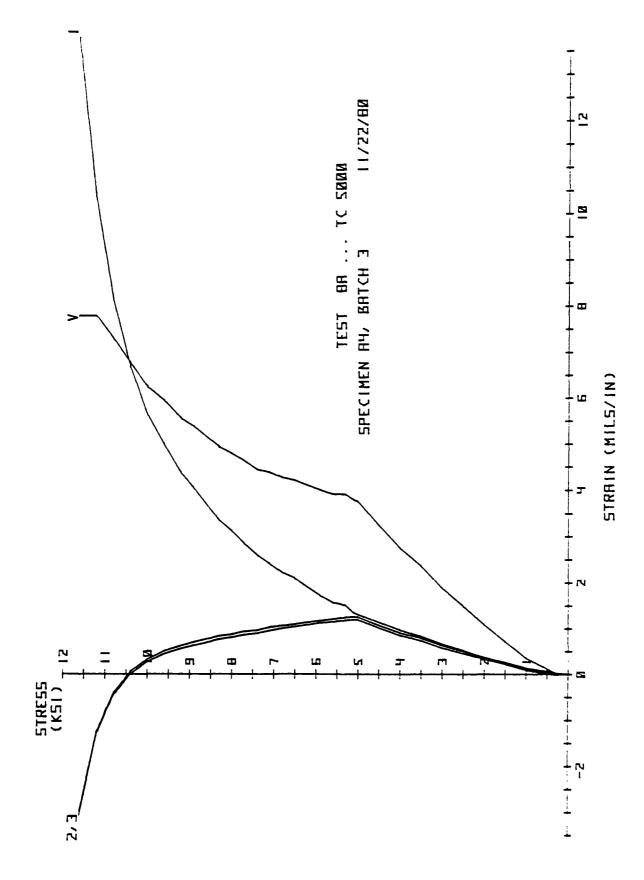


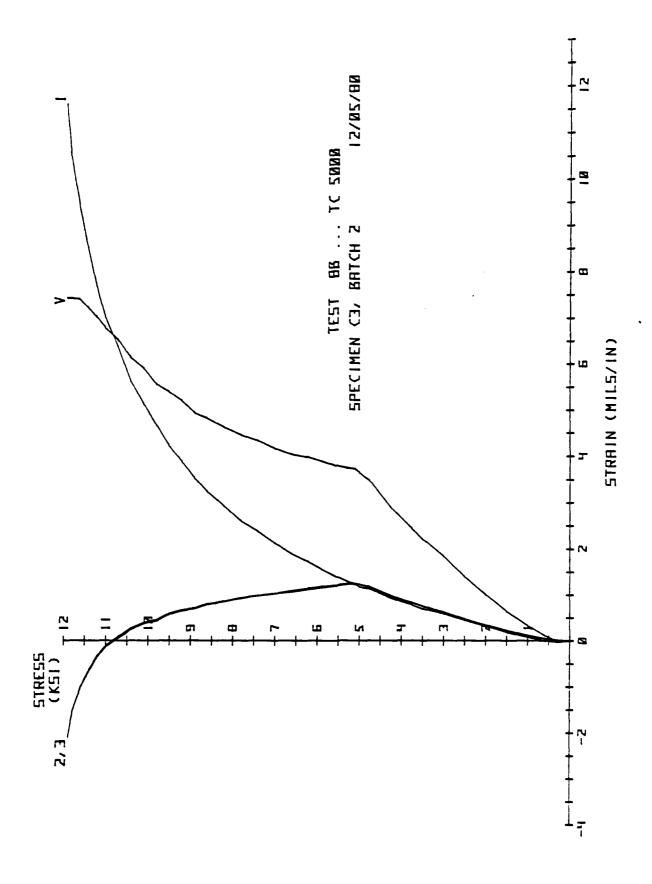


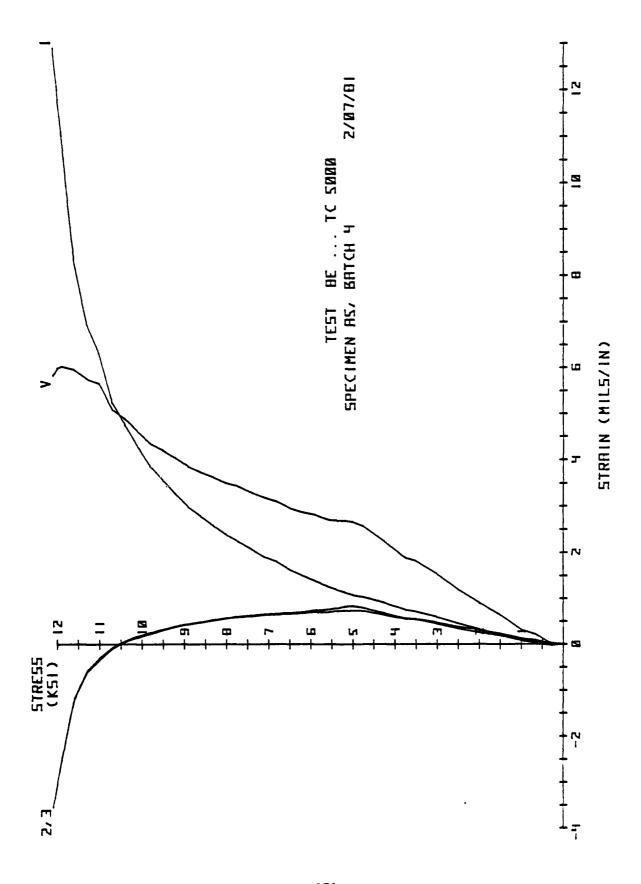


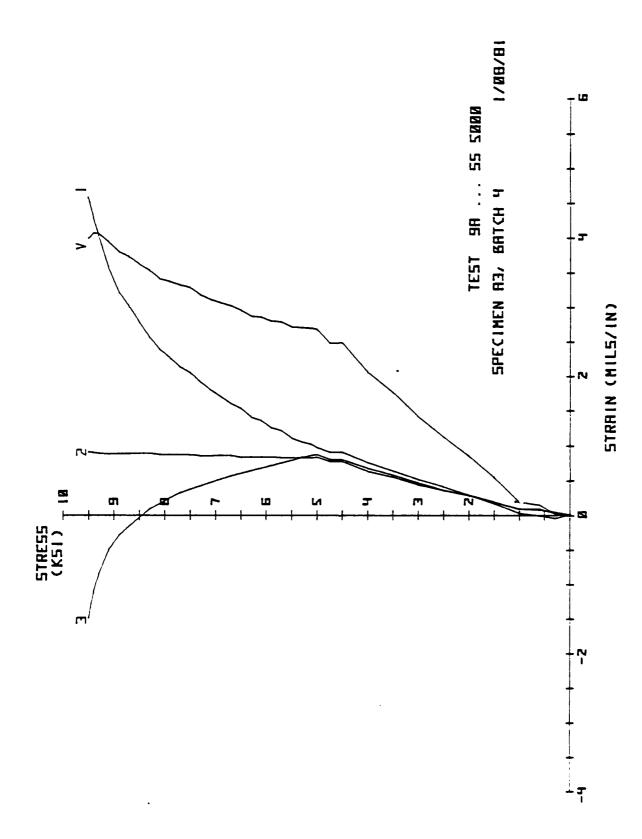


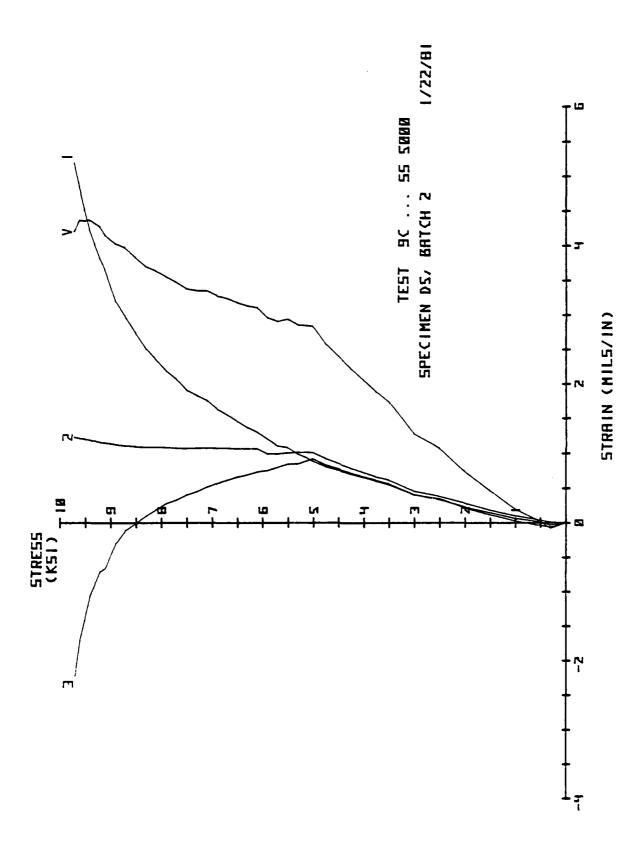


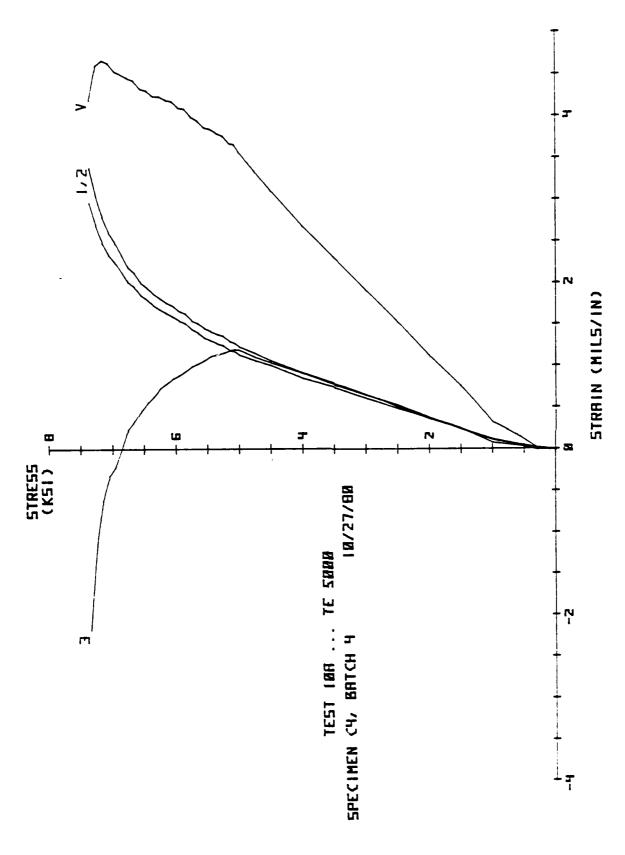


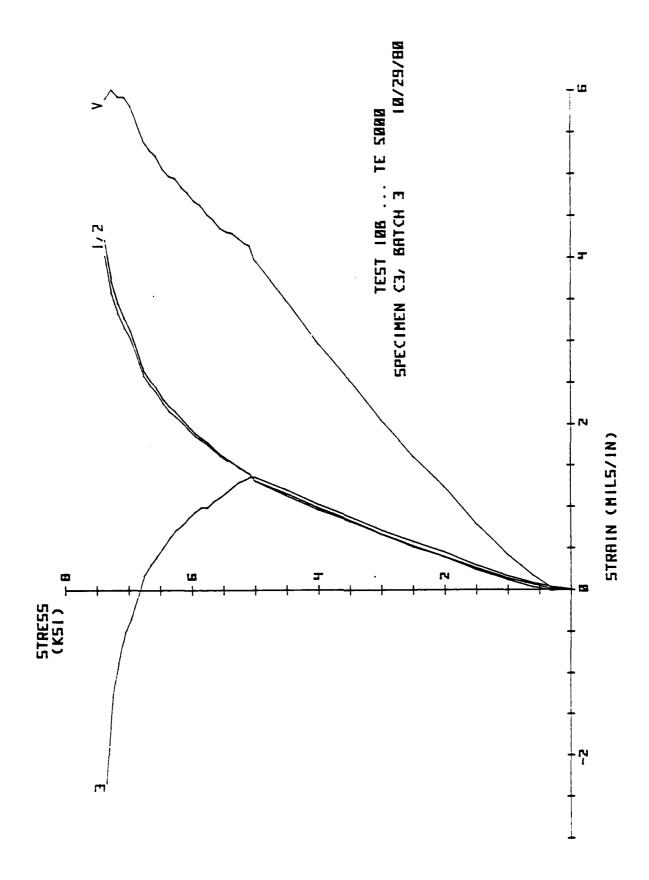


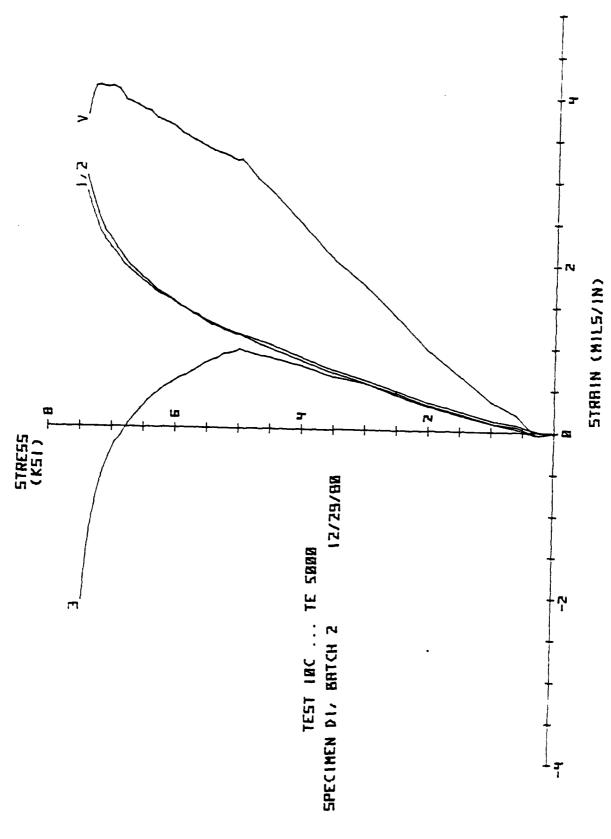












#### APPENDIX C.

#### STRESS-TRAIN DATA FOR BIAXIAL TESTS

This appendix contains the stress-strain data for each successful biaxial tests. The data sheets are arranged in order of test number. The axes which head the columns are the axes of the cubical cell. Stresses are given in psi and strains are given in mils/in. 1 mil/in. = 0.1% strain =  $10^{-3}$  in/in.

X-ANIS		Y-AXIS		Z-AMIS	
STRESS PSI)	STRAIN (NILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN • MILS/IN)
ବ୍ରବ୍ୟବର୍ଷ୍ଟ୍ର ବ୍ରବ୍ୟବର୍ଷ୍ଟ ବ୍ରବ୍ୟବର୍ଷ୍ଟ ବ୍ରବ୍ୟବର୍ଷ୍ଟ୍ର ବ୍ରବ୍ୟବର୍ଷ୍ଟ ବ୍ୟବ୍ୟ ବ୍ୟବ୍ୟବର୍ଷ୍ଟ ବ୍ୟବ୍ୟ ବ୍ୟ	9441551257397533777425991145699116994944512573975337777425991145699915799944551233456788999133444679227941877792789991334457927774259991334456999133444679227941877792799999999999999999999999999999999	ගතවල ම නිතිත කියින ම නිතිත	98586698528672829449429249129235529663918998528672829449429249129823552 98839189964931744646985921799875999 9899999999999999999999 9999999999	99999999999999999999999999999999999999	976598681336348793285383424773523 999744995667824629912734588929431 9933124949566782462891273458829431 99999111132334455667889991234677531 999999999999999999999999999999999999

#### TENSILE STRENGTHS

In the direction of the maximum principal stress = 301 ps: In the direction of the minimum principal stress = 374 ps:

## STRESS - STRAIN DATA

X-ANIS		Y-AXIS		Z-AXIS	
37RE53 (PSI)	STRAIN (NILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
ତ୍ର ତିବିକ ବିକିତ୍ର ଦିବିକ ବିକିତ୍ର ଦିବିକ ବିକିତ୍ର ଦିବିକ	000000071200494324438370716000402580000112386483759984847766 00000000112386486789834847766 00000000000000001111111238 00000000000000001111111238 000000000000000000000000000000000000	ବ୍ରତ୍ତ୍ର ବ୍ରତ୍ତ୍ର ବ୍ରତ୍ତ୍ର ବ୍ରତ୍ତ୍ର ବ୍ରତ୍ତ୍ର ବ୍ରତ୍ତ୍ର	0.00468 0.00468 0.00468 0.004087 0.004087 0.00408 0.00408 0.005335 0.005335 0.00535 0.00535 0.00535 0.00535 0.005	99999999999999999999999999999999999999	944586798111723116738123915991599129798223934459854231 91966639121734452393459854231 9196639129734452393459854231 91966394384452393459854231 919663943844555666778994384 9196639888888888888888888888888888888888
ପ ସ ପ ପ	-0.2866 -0.3557 -0.4721 -0.5534	ତ ଡ ଡ	-0.2846 -0.3361 -0.4227 -0.4843	3950 4100 4250 4400	1.2752 1.2954 1.5140 1.6213

### TENSILE STRENGTHS

in the direction of the maximum principal stress = 358 PSI in the direction of the minimum principal stress = 271 PSI

X-Axis	Y-AXIS		Z-AMIS	
STRESS STRAIN (PSI) (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
0       0	99999999999999999999999999999999999999	0.0001 0.0001 0.1368 0.2063 0.2063 0.4042 0.57023 0.57023 1.4233 1.7693 1.9476 2.7180 2.7180 2.7180 4.290	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	00133365800565334430070000000000000000000000000000000

### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAXIMUM PRINCIPAL STRESS = 366 PSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 308 PSI

X-AXIS		Y-AXIS		Z-AXIS	
STRESS	STRAIN	STRESS	STRAIN	STRESS	STRAIN
(PSI)	(MILS/IN)	(PSI)	(MILS/IN)	(PSI)	(MILS/IN)
ଉପ୍ତର୍ଭ ବିଷ୍ଟିବ୍ର ବିଷ୍ଟିବ୍ୟ ବିଷ୍ଟ ବି	\$\$\text{\$\	00000000000000000000000000000000000000	0659929820343387775258029219486777412105587298203433877752580292194867774121056490357892921948677741210909090909090909090909090909090909090	99999999999999999999999999999999999999	091698844002922300917955350556227124         02382626376400292230091795533503462005465         052382637640087960066109465         06526493197640         0600000000000000000000000000000000000
ବ	+2.2580	2850	0.2171	8550	3.8465
ବ	+2.5498	2900	0.2303	8700	4.0831
ପ	+2.9607	2950	0.2326	8850	4.4112

## TENSILE STRENGTHS

IN THE DIRECTION OF THE MANIMUM PRINCIPAL STRESS = 363 PSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 349 PSI

X-AMES		7-AXIS		Z-AMIS	
STRESS (PSI)	STPAIN (MILS IN)	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
ପର୍ବ ବିଷ୍ଟ ବ	00000000000000000000000000000000000000	99999999999999999999999999999999999999	0007-64-685-49-15-4-625-125-9-29-5-6-9-9-9-8-8-8-8-8-8-8-8-8-8-8-8-8-8-8-8	33993999999999999999999999999999999999	07151818104402298396594942098331469443544333326252594942098331469442098333262525949420960741000667557356339484413006674111111111111113333333333333333333333

# TEMSILE STRENGTHS

14 THE DIPECTION OF THE MAXIMUM PRINCIPAL STRESS = 353 PS1 14 THE DIPECTION OF THE MINIMUM PRINCIPAL STRESS = 292 PS1

X-AXIS	Y-AXIS		Z-AKIS	
	TRESS PSI) (M		STRESS (PSI) (	STRAIN :MILS/IN)
99514726115484747792518335777744433991313172611548477477925183357777744433999999999999999999999999999		0.0548 -0.0548 -0.0548 -0.0549 -0.0229 -0.03931 -0.023931 -0.120337 -0.120337 -0.3765 -0.3766 -0.5237	99999999999999999999999999999999999999	981144625869354469923119419347.9.949277887467438581529129957.9.35.0.011849858467438581529129957.9.3.444687.78398123567943297.59.3.456778398123567943297.59.3.444687.783981111111112222222222222

### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAXIMUM PRINCIPAL STRESS = 446 PSI In THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 389 PSI

X-AXIS		Y-AXIS		ZHAXIS	
STRESS (PSI)	STRAIN (MILS/IN)	STRESS .PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
550000000000000000000000000000000000000	973246547397352166939316187842545593931618784253576593931618784253576593931618784253576593931618784253576593931618784253576593931618784253576536939393161878425357653495669393445844626563344588446265633447869338478693383	88888888888888888888888888888888888888	02283764018898323421264131962453858 022729667375410886047240845123445385 000000001151304462044740831236451244813 000000000000000000000000000000000000	2222333444555556677778883388	03955133263023004335921306537619550006336444004656561670707019390502215990024554949075280567709241933902471224770000455567709041245700024704913577090445700004491357709044570000044444444
2 2 2	-4.9243 -5.2924 -5.7538	6100 6200 6300 6400	4.3036 2.4628 2.5583 2.6808	9150 9300 1 9450 9600	5.1070 5.5535 5.7730 6.0894

#### TENSILE STRENGTHS

IN THE DIFECTION OF THE MADIMUM PRINCIPAL STRESS = 328 ASI IN THE DIFECTION OF THE MINIMUM PRINCIPAL STRESS = 227 ASI

X-AXIS		: .: ;	-AXIS	Z-AMIS	
STRESS	STRAIN	STR <b>e</b> ss	STRAIN	STRESS .	STRAIN
(PSI)	(MILS/IN)	(PSI)	(MILS/IN)	(PSI)	MILS/IN)
୍	7 048963899771364836875141010096 20134741049417864836875141010096 201347410494178648368751441010096 2013570235702372863476314010096 20135702359372868751410100996 20135702359372868751410100996 20135702359372868751410100996 20135702359372868751410100996 20135702359372868751410100996 20136703648368751410100996	. 999999999999999999999999999999999999	0461 0461	7 999999999999999999999999999999999999	97329617339177032682005277074570 92416496542541655252114367225956 90.1236644554166522114367225956 90.1236644554166522114367225956 90.1366445541665221143672255956 90.1466962443577074570 90.23696214869624435358786 90.236962446722223333444
ଡ଼ି	-3.6236	5900	1.8547	3850	5.3602
ବ	-4.4185	6000	2.0053	9000	5.9588
ବ	-5.5367	6000	2.1709	9150	6.3900

## TENSILE STRENGTHS

IN THE DIRECTION OF THE MAXIMUM PRINCIPAL STRESS = 191 PSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 467 FSI

X-ANIS		Υ	Y-AXIS		Z-AXIS	
STRESS (PSI)	STRAIN (MILS//IN)	STRESS (PSI)	STRAIN (MILS/IN/	STRESS (PSI)	STRAIN (MILS/IN)	
ପର୍ଚ୍ଚ ବର୍ଷ ବର୍ଷ ବର୍ଷ ବର୍ଷ ବର୍ଷ ବର୍ଷ ବର୍ଷ ବର୍ଷ	00757841800696576884500274217868002412806965768884502742178686482527576888450274217868648296965768864829869696576888450027421786886482986965768884500274217868848298696976767688848489869697677878868484888845002742178688482988848988489884898848988489884898	99999999999999999999999999999999999999	0.000000000000000000000000000000000000	99999999999999999999999999999999999999	0295320753371565055392500035848075337156509494766470838060558480190250409494766470838000025504094947664708380000011350000371475044755	

#### TENSILE STRENGTHS

IN THE DIRECTION OF THE MAKIMUM PRINCIPAL STRESS = 343 PSI IN THE DIRECTION OF THE MINIMUM PKINCIPAL STRESS = 255 PSI

#### STRESS - STRAIN DATA

X-ANIS		Y-AXIS		Z-AXIS	
STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)	STRESS (PSI)	STRAIN (MILS/IN)
00000000000000000000000000000000000000	099 097438 077438 077437 077437 077437 077437 07743 07	99 99 99 99 15 99 12 18 18 18 18 18 18 18 18 18 18 18 18 18	0.0035 0.0035 0.0035 0.0035 0.1397 0.1397 0.1397 0.1397 0.23977 0.355 0.63133 0.93314 0.93314 1.355 1.	ବ୍ରବ୍ରବ୍ରବ୍ରବ୍ରବ୍ରବ୍ରବ୍ରବ୍ରବ୍ରବ୍ରବ୍ରବ୍ରବ	0.0000 -0.0168 -0.0168 -0.02762 -0.02765 -0.0964 -0.1288 -0.12861 -0.29444 -0.36166 -0.42866 -0.42866 -0.75539 -0.75539 -1.47763 -1.47763 -2.5977 -2.5977

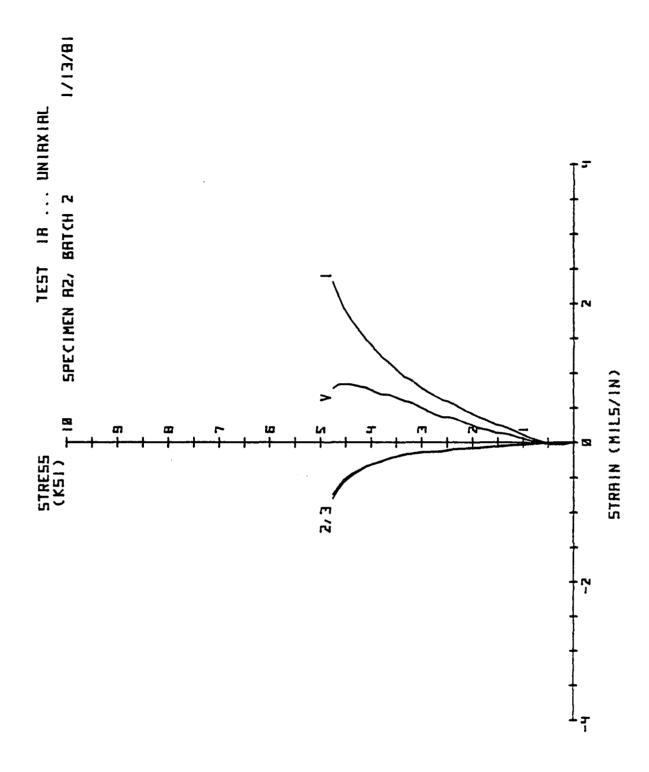
## TENSILE STRENGTHS

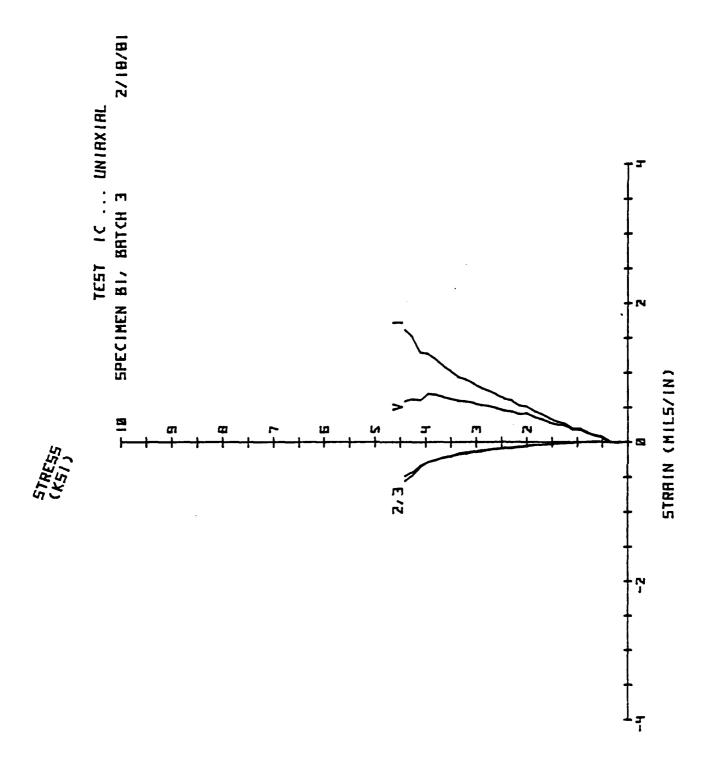
IN THE DIRECTION OF THE MAXIMUM PRINCIPAL STRESS = 475 PSI IN THE DIRECTION OF THE MINIMUM PRINCIPAL STRESS = 303 PSI

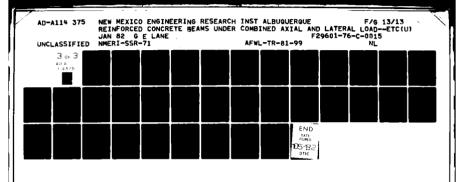
#### APPENDIX D.

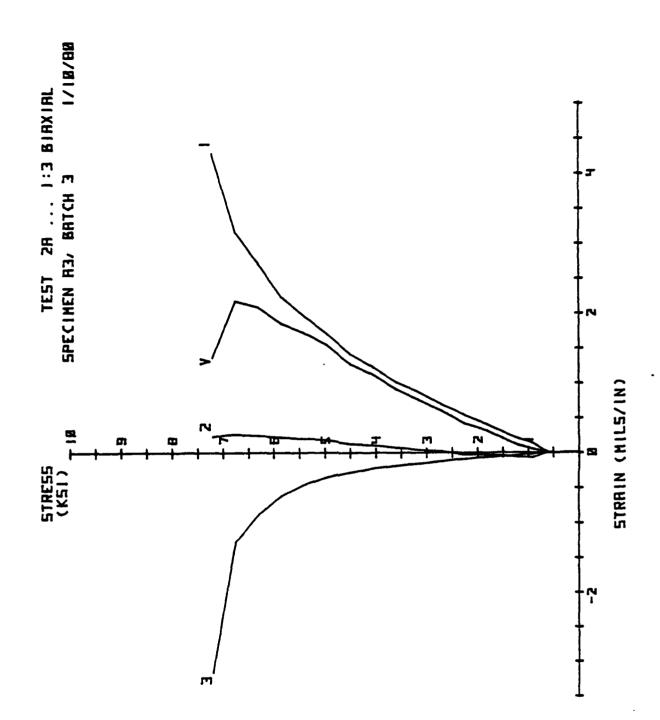
#### STRESS-STRAIN CURVES FOR BIAXIAL TESTS

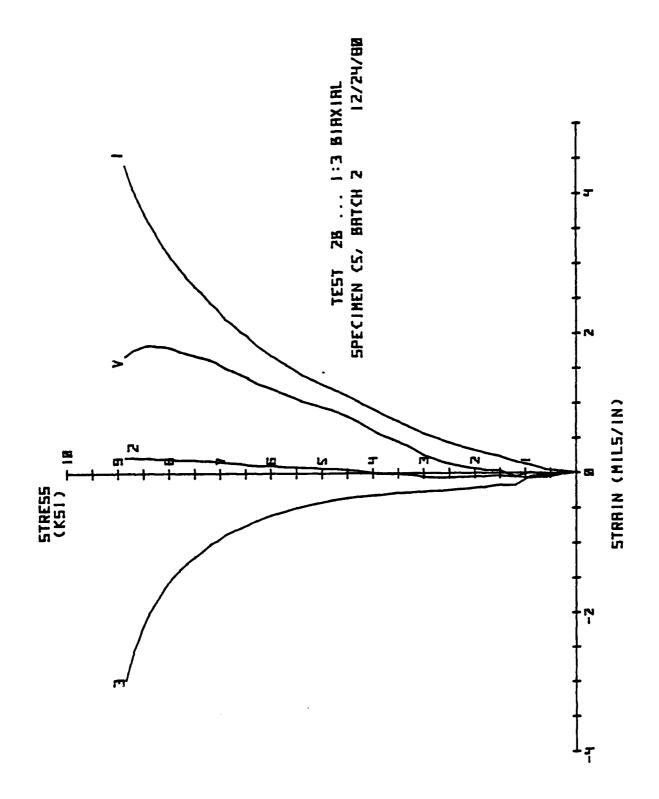
This appendix contains the stress-strain curves generated during each successful biaxial test. The ordinate values are mils/in. of strain and the values on the abscissa are the maximum principal stress in ksi. The numbers 1, 2 and 3 marked on the curves represent the principal strains and the curve marked "V" is the volumetric strain curve.

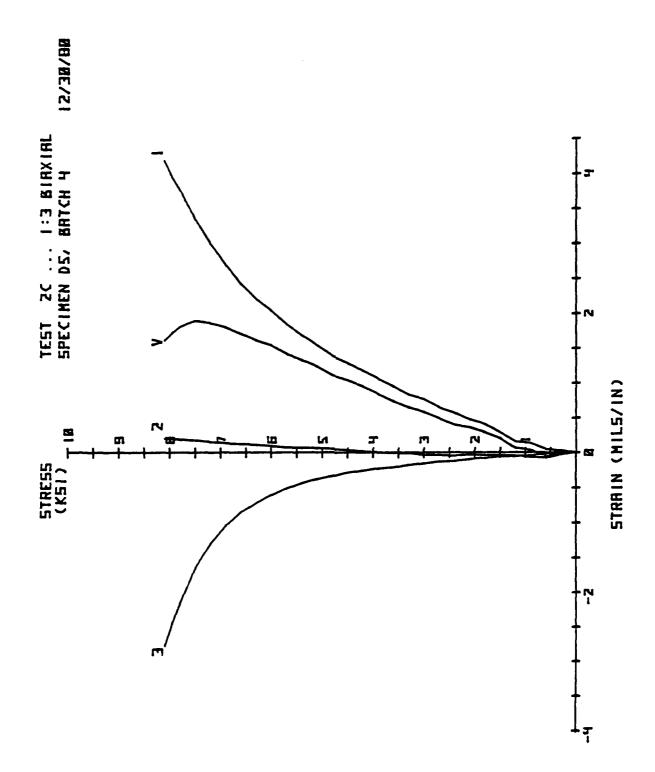


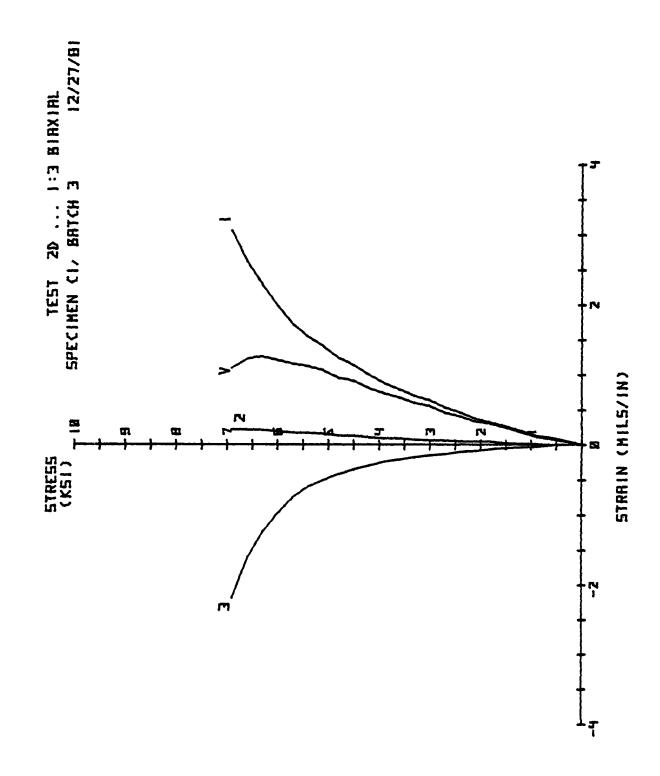


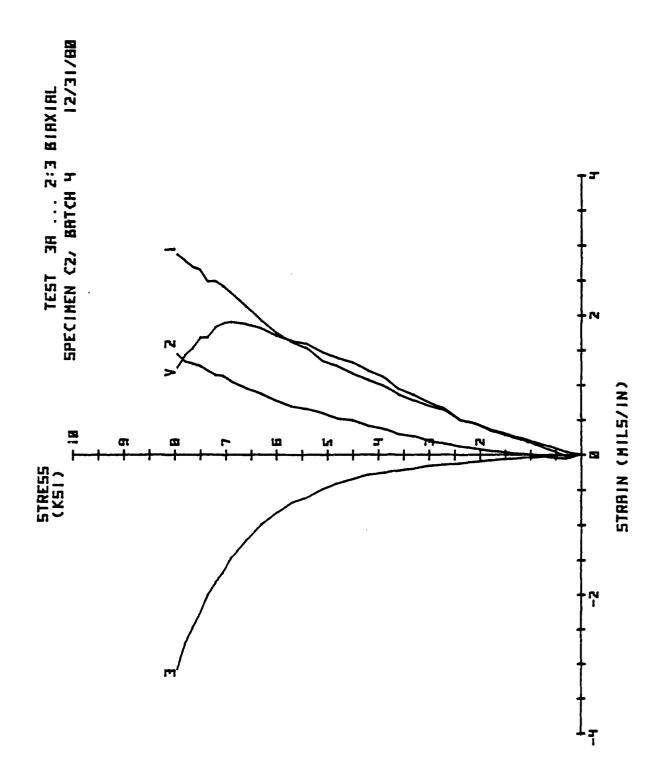


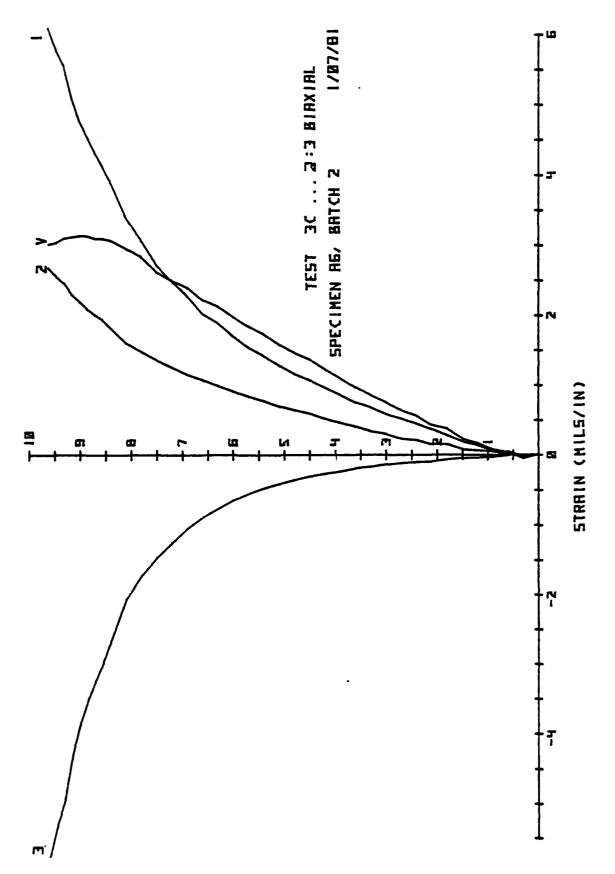


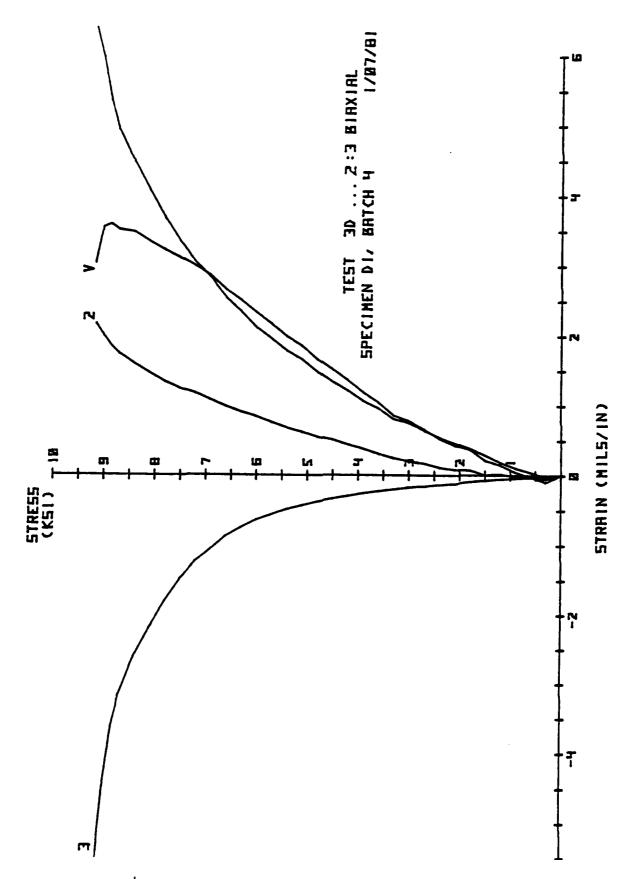


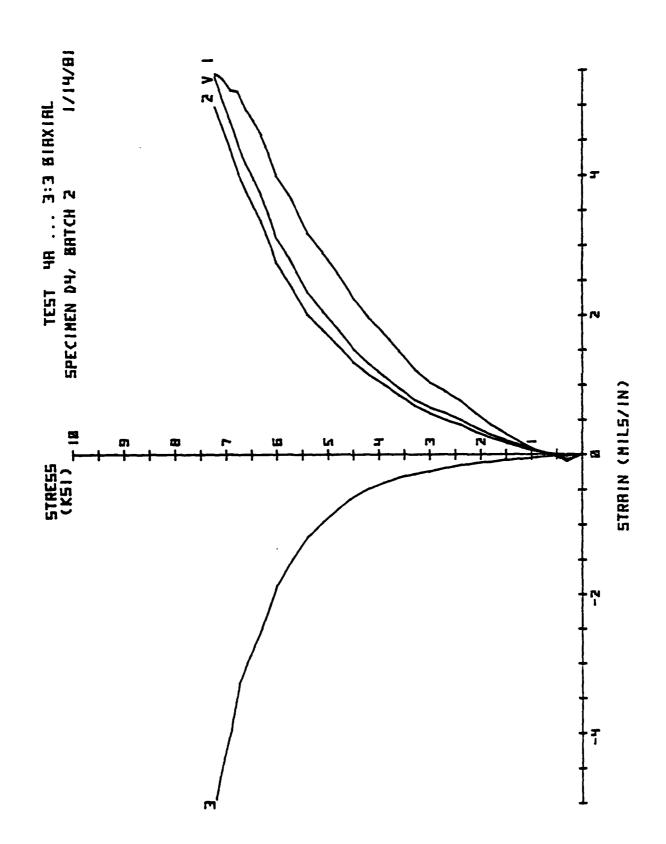


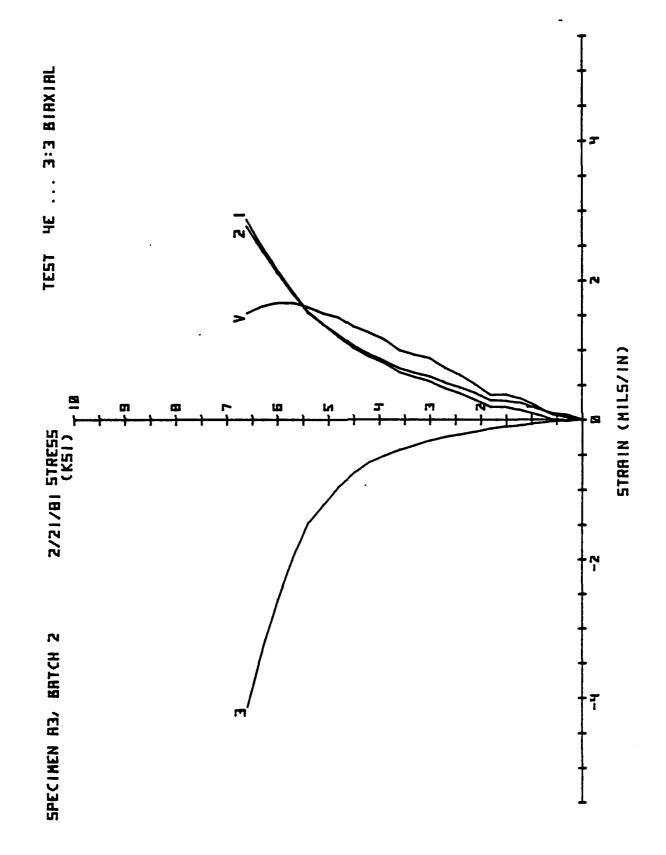












#### APPENDIX C

#### PLAIN CONCRETE PRISM TESTING

DR. G. KRISHNAMOORTHY

SUBMITTED BY

SAN DIEGO STATE UNIVERSITY

SAN DIEGO, CALIFORNIA

TO

NEW MEXICO ENGINEERING RESEARCH INSTITUTE

UNIVERSITY OF NEW MEXICO

ALBUQUERQUE, NEW MEXICO

Presented to: Dr. Golden E. Lane
June 8, 1981

Note: This appendix is a self-contained document, provided for the reader's information, with its own figures, tables, and appendixes.

#### Note:

The San Diego State work consisted of testing twenty-four 152- by 305-mm plain concrete cylinders under displacement control. The testing was conducted in a modified Riehle testing machine with a 1.33-MN capacity. This machine can accommodate up to 3-m specimens. The Riehle machine has a 300K MTS load cell and electronic instrumentation for imposing a specified rate of deformation and for automatic data logging, including a facility for X-Y recording along with digital readout for direct monitoring of tests.

The concrete cylinders were tested by imposing a deformation rate of 0.51 mm/min. Four linear variable-differential transformers (LVDT) were mounted in a circle around the specimen, 90 deg apart, to measure the deformations. The signals from the diametrically opposite LVDT's were combined and averaged to eliminate rotation of the loading platten. Signals from the MTS load cell were obtained to measure the load. These signals were fed into signal conditioners and amplifiers to obtain the load-deformation plots. To obtain the initial slopes of the plots accurately, extremely sensitive Hewlett-Packard X-Y recorders were used.

			<del>                                     </del>	
BATCH NO.	SPECIMEN	TYPE OF	STRENGTH	INITIAL MODULUS
	NO.	LOADING	PSI	10 <sup>+6</sup> LB/IN <sup>2</sup>
1	2	MONOTONIC	5036	2.92
	3		4902	2.68
	4 .	•	4775	3.08
	5	"	5185	2.82
	6	"	4746	2.80
	MEAN		4929	2.86
	ST, DEV.		184	0.15
2	1 MONOTONIC		4909	2.52
	2	**	5482	2.66
	3	**	5199	2.66
	. 4	CYCLIC	5256	2,62
	5	•	5227	2.64
	6	*	5341	2.72
	MEAN		5236	2.64
	ST. DEV.		190	.07
3	1	MONOTONIC	5447	2.58
	2	CYCLIC	5567	2.64
	3	**	5220	2.90
	4	MONOTONIC	5624	2.80
}	5	•	5022	2.42
	6	CYCLIC	5227	2.66
	MEAN		5351	2.67
	ST. DEV.		233	0.17
4	1	MONOTONIC	4782	2.60
	2	•	5160	2.66
	3	CYCLIC	5447	3.50
	4	#	4761	3.42
	5	MONOTONIC	4952	3.66
1	6	CYCLIC	5079	3.14
	MEAN		5030	3.16
	ST. DEV.		258	0.45

